

### Are neutrinos completely neutral?

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### 1937 Nuovo Cimento 14 171-184



### TEORIA SIMMETRICA DELL'ELETTRONE E DEL POSITRONE

Nota di Ettore Majorana

Sunto. - Si dimostra la possibilità di pervenire a una piena simmetrizzazione formale della teoria quantistica dell'elettrone e del positrone facendo uso di un nuovo processo di quantizzazione. Il significato delle equazioni di DIRAC ne risulta alquanto modificato e non vi è più luogo a parlare di stati di energia negativa; nè a presumere per ogni altro tipo di particelle, particolarmente neutre, l'esistenza di « antiparticelle » corrispondenti ai « vuoti » di energia negativa.

We show that it is possible to achieve complete formal symmetrisation in the electron and positron quantum theory by means of a new quantization process. The meaning of Dirac equations is somewhat modified and it is no more necessary to speak of negative-energy states; nor to assume, for any other type of particles, especially neutral ones, the existence of antiparticles, corresponding to the "holes" of negative energy.

## An unpleasant asymmetry

The new approach allows to "not only to give a symmetric form to the electron-positron theory, but also to build a substantially novel theory for the particles deprived of electric charge (neutrons and hypothetical neutrinos)"

.....it is probably "not yet possible to ask to the experience to decide between this new theory and the simple extension of the Dirac equations to the neutral particles"

B. M. Pontecorvo. The infancy and youth of neutrino physics: some recollections. Journ. de Phys. **12** (1982) vol. 43, p. c8-221

"For the benefit of the young reader who from the beginning of his activity has been used to hear not only of electric charge but also of other types of "charge" (baryon, lepton,...) I would like to underline that in 1937 only electric charge was known. Now Majorana, **first**, invented explicitly truly neutral fermions or Majorana particles, that is fermions which are identical to their own antiparticles."

### **Completely neutral particles**

Definition neutrino = neutral particle produced in  $\beta^+$  decay anti-neutrino = neutral particle produced in  $\beta^-$  decay

### **Completely neutral: antiparticle = particle**

All "charges" (electric, colour, lepton number, baryon number) = 0

#### Bosons

can be mass-less:  $\gamma$ or massive:  $Z^0$ , H,  $\pi^0$ ,  $\eta$ ,....

Fermions

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must be massive: v? neutralino?
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The bi-spinor  $\psi(x) = \begin{pmatrix} \psi_1 \\ \psi_2 \\ \psi_3 \\ \psi_2 \end{pmatrix} = \begin{pmatrix} \varphi \\ \chi \end{pmatrix}; \quad \varphi = \begin{pmatrix} \varphi_1 \\ \varphi_2 \end{pmatrix}; \quad \chi = \begin{pmatrix} \chi_1 \\ \chi_2 \end{pmatrix}$  In the Dirac theory the  $\varphi$  and  $\chi$  components have different transformation properties

Question: is it possible to find a spinor X constructed with the components of  $\varphi$  only (and hence without further degrees of freedom), which transforms like a  $\chi$  instead than a  $\varphi$ and that can consequently take its place in the Dirac equation? And similarly a spinor  $\Phi$ transforming like a  $\varphi$ ?

The answer, found by Majorana, is

$$\Phi = i\sigma_2 \chi_M^* \qquad i\sigma_2 = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$$
$$X = i\sigma_2 \varphi_M^*$$

Dirac equation 
$$\begin{aligned} & \left(E + \vec{p} \cdot \vec{\sigma}\right) \chi - m\varphi = 0 \\ & \left(E - \vec{p} \cdot \vec{\sigma}\right) \varphi - m\chi = 0 \end{aligned} \end{aligned} \qquad \text{Majorana equation} \begin{aligned} & \left(E + \vec{p} \cdot \vec{\sigma}\right) \chi - im_a \sigma_2 \chi^* = 0 \\ & \left(E - \vec{p} \cdot \vec{\sigma}\right) \varphi - im_b \sigma_2 \varphi^* = 0 \end{aligned}$$

•Majorana equations are decoupled, one for  $\varphi$  and one for  $\chi$  spinor (possibly two masses) •If m=0, Dirac equation = Majorana equation •Nature has chosen m≠0, hence differences between the two theories exist

### 1937 Nuovo Cimento 14 323



### SULLA SIMMETRIA TRA PARTICELLE E ANTIPARTICELLE

Nota di GIULIO RACAH

We show that the symmetry between particles and antiparticles leads to some formal modifications of the Fermi theory of the  $\beta$  radioactivity and that the physical identity between neutrinos and antineutrinos leads directly to Majorana theory.

Sunto. - Si mostra che la simmetria tra particelle e antiparticelle porta alcune modificazioni formali nella teoria di FERMI sulla radioattività  $\beta$ , e che l'identità fisica tra neutrini ed antineutrini porta direttamente alla teoria di E. MAJORANA.

If neutrinos obey Dirac equation, neutrinos emitted in a  $\beta^-$  decay can induce only a  $\beta^+$  process and vice versa If they obey Majorana equation, any neutrino can produce both electrons and positrons



Neutrons cannot obey Majorana equation for two reasons

- 1. Neutron has a magnetic moment
- 2. Neutrons would decay  $\beta^-$  into protons and  $\beta^+$  into antiprotons with equal probabilities

1939 Physical Review 56 1184

**DECEMBER** 15, 1939

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#### On Transition Probabilities in Double Beta-Disintegration

W. H. FURRY

Physics Research Laboratory, Harvard University, Cambridge, Massachusetts (Received October 16, 1939)

The phenomenon of double  $\beta$ -disintegration is one for which there is a marked difference between the results of Majorana's symmetrical theory of the neutrino and those of the original Dirac-Fermi theory. In the older theory double  $\beta$ -disintegration involves the emission of four particles, two electrons (or positrons) and two antineutrinos (or neutrinos), and the probability of disintegration is extremely small. In the Majorana theory only two particles—the electrons or positrons—have to be emitted, and the transition probability is much larger.



The Racah proposal to distinguish between Dirac and Majorana neutrinos cannot be realized in practice

The Furry proposal can be followed, but unfortunately "the transition probability" is not "much larger", but rather **much smaller** For two elements unknown to Furry: •CC weak current is V-A •neutrino masses are very small



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### 1946 Report PD-205, Chalk River, Canada.

W. Pauli: "I have done a terrible thing. I have postulated a particle that cannot be detected."



B. Pontecorvo. Try with

 $v + {}^{37}\text{Cl} \rightarrow {}^{37}\text{Ar}^* + e^-$ 

Use low background proportional counter to detect X ray from Ar\* de-excitation

Report was classified. Method might be used to detect nuclear submarines

Neutrino or antineutrino?

# **1958. R. Davis. Neutrino≠antineutrino?**

Several improvements of the Cl Ar method proposed by L. Alvarez in 1949 Use C<sub>2</sub>Cl<sub>4</sub>, He-sweep for extraction, LN2 cooling of the trap, etc.

R. Davis. Attempt to detect antineutrinos from a nuclear reactor by the  ${}^{37}Cl(v,e^{-}){}^{37}Ar$  reaction. Phys. Rev. 97 (1955) 766. @ the Brookhaven reactor No signal, but due to the insufficient sensitivity: flux too low + background too high Theory: 2 10<sup>-44</sup> cm<sup>2</sup>/atom; limit <2 10<sup>-42</sup> cm<sup>2</sup>/atom



R. Davis. *An attempt to observe the capture of reactor neutrinos in Chlorine-37*. Unesco Conference **1958**. Paris. Vol. 1 p. 728 At Savannah River the sensitive was enough (factor 5)

Neutral particles from a reactor do not induce Pontecorvo reaction

 $\overline{v}_{a} + {}^{37}\text{Cl} \rightarrow {}^{37}\text{Ar}^{*} + e^{-}$ 

Neutrino has different reactions than antinutrino

The conclusion: neutrino and antineutrino are different particles, made in the SM, is premature

Alvarez L. Univ. Calif. Lab. Rep. 328 (1949)

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# **1956 Science 124 103** Detection of the Free Neutrino: a Confirmation

C. L. Cowan, Jr., F. Reines, F. B. Harrison, H. W. Kruse, A. D. McGuire

Frederick REINES and Cycle COVAN Box 1663, LOS ALAHOS, New Marico Thanks for menage. Everyting comes to him who know how to wait. Paul:

NB "Free ?? neutrinos". But Fermi 1933: electrons do not exist before the decay "On the contrary they are created together with a **neutrino**, similarly to the creation of a light quantum that goes with a quantum jump of an atom A. Bettini. LSC and Padova

# 1957 JINR Preprint P-95

B. Pontecorvo "Fifty years of neutrino physics: a few recollections" Neutrino 1980 Conf. Now at the time I was told in a wrong way about such experiment. A delegation came to Moscow and someone (I do not remember who) told me that R. Davis got a positive signal in his *experiment* (interpreted by Davis as bakground from cosmogenic <sup>37</sup>Cl(p,n)<sup>37</sup>Ar). *Such result at* the time seemed to me fantastic (and rightly so!). Wrong rumours sometimes are useful. I tried to find a way out and invented neutrino oscillations of the type



B.M.P. considers an analogy with the  $K^0 \overline{K}^0$  system  $v_e \rightleftharpoons \overline{v}_e$ 

...neutrino and antineutrino are.... symmetrical and antisymmetrical  $v_1 = \frac{1}{\sqrt{2}} (v + \overline{v})$ combinations of two truly neutral *Majorana particles*  $v_1$  *and*  $v_2$ .

 $v_2 = \frac{1}{\sqrt{2}} \left( v - \overline{v} \right)$ 

It follows that neutrinos in vacuum can transform themselves in antineutrinos and viceversa....So, a beam of neutral leptons from a reactor which first consists mainly of antineutrinos will change in composition and at a certain distance...will be composed of neutrinos and antineutrinos in equal quantities

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### Neutrino flavour mixing

**1956** Sakata model. Fundamental particles are p, n and  $\Lambda$ 

1957-8 Parity violation. V-A structure

**1959** Gamba, Marshak and Okubo **baryon-lepton fundamental symmetry**  $(v, e, \mu) - (p, n, \Lambda)$ 

**1960** Maki et al. Nagoya model. "Ur" matter  $B^+$  and  $p = vB^+$   $n = e^-B^+$   $\Lambda = \mu^-B^+$ 

**1962** Second neutrino, lepton-baryon symmetry lost

Try to recover: **Katayama et al**. and **Maki et al.** advanced two hypothesis 1. are not the "true" neutrinos, but linear mixtures, of them

$$v_1 = v_e \cos \delta + v_\mu \sin \delta$$
  $v_2 = v_e \cos \delta - v_\mu \sin \delta$  The true ones

2. only  $v_2$ , for not explained reasons, couples to the  $B^+$ Maki et al. mentioned also the possibility of "transmutation" between neutrino flavours Katayama et al. advanced the hypothesis that a 4<sup>th</sup> "Sakaton" might exist

N.B. If it were true neutrino and quark (Cabibbo) mixing angles would have to be equal

**1962** Lipkin et al. notice that the observation of  $\overline{p}p \rightarrow K_L^0 K_S^0$  at rest falsifies Sakata model

August 20, 13

# Neutrino oscillations 50 years of BSM physics

### 1963.

John Bahcall starts building the Solar Standard Model





**11 August 1967**. R. Davis writes to Fowler "Dear Willy, I do have a preliminary result from our first good run. The sample was taken June 22<sup>nd</sup> and counting has continued until today. I am now removing the sample and will rerun background. So we do have a result and during the last few weeks I have told a few people that are interested.".

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### **Neutrino oscillations**

**9** June 1967 (two months before the letter of Davis to Fowler) B. Pontecorvo sends a paper to *Zhurnal Eksperim. noi i Teoreticheskoi Fiziki*.

Considers  $v_e \rightleftharpoons \overline{v}_e$ ,  $v_\mu \rightleftharpoons \overline{v}_\mu$ ,  $v_e \rightleftharpoons v_\mu$  assuming eigenstates to be Majorana

From an observational point of view the ideal object is the sun. If the oscillation length is smaller than the radius of the sun effectively producing neutrinos (let us say, one tenth of the solar radius...for the <sup>8</sup>B neutrinos)....the only effect on the earth surface must be two times smaller than the total flux

B.M.P. was almost but not quite right. Boron neutrinos do not change flavour by oscillations but by adiabatic transition in matter (MSW effect).

L. Wolfenstein (1978) Oscillations in matter

S. P. Mikheyev, A. Yu. Smirnov (1985) Adiabatic transition in matter

### **Chirality and Helicity**

States of definite chirality are the eigenstates of  $\gamma_5$ , L for the eigenvalue –1, R for +1 Neutrino field has negative chirality. Neutrinos and antineutrinos are left

$$\psi_L = \frac{1}{2} (1 - \gamma_5) \psi, \qquad \gamma_5 \psi_L = -\psi_L$$

 $\gamma_5$  does not commute with the mass term of the Hamiltonian Chirality is not an observable, we measure helicity instead

Both neutrinos and anti have **positive** (+) and negative (-) helicity components. For *E>>m* 

$$\varphi = v \approx \frac{m}{E} v_L^+ + v_L^- \qquad \qquad \chi = \overline{v} \approx v_L^+ + \frac{m}{E} v_L^-$$

If m=0 neutrinos are pure h=- states, antineutrinos pure h=+ states If Majorana, "neutrino" is the state with h=-1; "antineutrino" is the state with h=+1

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## *Ονββ* **Decay**

Majorana neutrino couples to *W* exactly as Dirac neutrino The SM violation is in the propagator



The status created at one vertex has definite flavour, hence is a superposition of mass eigenstates

Mass eigenstates do not have definite helicity, are superpositions of Majorana neutrinos and antineutrinos At one vertex the antineutrino component matters, the neutrino component at the other vertex

$$M_{ee} = \left| \sum_{i} U_{ei}^{2} m_{i} \right| \approx \left| 0.67 m_{1} + 0.30 m_{2} e^{i2\alpha} + 0.03 m_{3} e^{i2(\beta - \delta)} \right|$$

$$v_e = U_{e1}v_1 + U_{e2}v_2 + U_{e3}v_3$$

$$\boldsymbol{v}_i \approx \frac{m_i}{E} \boldsymbol{v}_{iL}^+ + \boldsymbol{v}_{iL}^-$$

### Majorana vs Dirac at relativistic energies





The V–A structure of the charged weak currents + smallness of neutrino mass are sufficient to explain experimental observations No need to invoke lepton number conservation No need to have neutrino different from antineutrino

The experimental challenge  

$$\left(T_{1/2}^{0\nu^2}\right)^{-1} = G_{0\nu}g_A^4 \left|M_{0\nu}\right|^2 \left|\frac{M_{ee}}{m_e}\right|^2 \qquad g_A = 0.6-1.25$$

Barea J, Kotila J and Iachello F 2012 Phys. Rev. Lett. 109 042501

#### **Experiments measure the sum energy of the two electrons**

If background index b, sensitive mass M, live time T and energy resolution  $\Delta E$ 

sensitivity to 
$$\frac{1}{M_{ee}} \propto F_M = \left(\varepsilon \frac{ia.}{A}\right)^{1/2} \left(\frac{MT}{b\Delta E}\right)^{1/4}$$
 2.0  
If *b*=0 during *T*, in an energy window  
of about  $\Delta E$  sensitivity to  $M_{ee}$   
 $F_M \propto \varepsilon \frac{ia.}{A} \sqrt[2]{MT}$   
Energy resolution and almost zero  
background are the key factors  
 $0.0 = \frac{1.5}{0.2} = \frac{1.6}{0.2} = \frac{1.6}{0.4} = \frac{1.6}{K_{ee}/Q_{BB}}$ 

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### The landscape



Running experiments  $T_{1/2}$  several 10<sup>25</sup> yr  $M_{ee} = 200-300$  meV If the limits from cosmology on poutring mass are taken parioual

neutrino mass are taken seriously, we need to reach

 $M_{ee} = 50 \text{ meV}$  $T_{1/2}$  several  $10^{26} \text{ yr}$  $1 \text{ kmol} = 6 \times 10^{26} \text{ nuclei}$ 

Is it possible?

Need M>1 t isotope FWHM energy resolution < 1% BI≈10<sup>-4</sup>/(keV kg yr) Adapted from R.G. H. Robertson. arXiv: 1301.1323

# Which isotope? See Barabash for full review



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### GERDA (and MAJORANA) GE diodes see Bezrukov



### **GERDA** (and MAJORANA)



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### EXO-200 Liquid Xe TPC



see Belov



### KamLAND-ZEN. Xe dissolved in LScintillator





a  $\approx 0.91$   $f_{act}=0.62$   $\epsilon a f_{act} = 0.46$   $M_{Xe} \approx 300 \text{ kg}$   $M_{act} = 186 \text{ kg}$   $M_{act} t = 89.5 \text{ kg yr}$   $\Delta E = 175 \text{ keV}$ BI = 5 10<sup>-3</sup>/(keV kg yr)  $T_{1/2} > 1.9 \ 10^{25} \text{ yr}$ NB. 2 $\vee 2\beta$  contribution to BI = 0.7 10<sup>-4</sup>/(keV kg yr)

$$M_{Xe}t = \frac{M_{act}t}{f_{act}} = \frac{11}{0.62} = 18 \text{ t yr}$$

However, reduction of the BI may require reduction of  $f_{act}$ Self shielding is expensive, being done of enriched Xe

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### NEXT. High pressure Xe TPC



![](_page_27_Figure_0.jpeg)

Present MonteCarlo + screening gives BI= 5 10<sup>-4</sup>. Assume **BI= 10<sup>-4</sup>/(keV kg yr)** 

ε=0.35

**ΔΕ=10 keV** 

Exposure needed for S/N = 4 at  $M_{ee}$ =50 meV  $N_{ee} \left(4.4 \cdot 10^{26}\right) = \varepsilon \cdot 7 \cdot Mt (t yr) = 2.5 \cdot Mt (t yr)$   $S / N = \frac{1}{\sqrt{1}} \sqrt{Mt} = 1\sqrt{Mt}$   $N_b = \Delta E \cdot BI \cdot Mt = 10 \cdot 10^{-4} \cdot 10^3 \cdot Mt = 1 \cdot Mt$   $Mt \left(4.4 \cdot 10^{26}\right) = \left(\frac{4}{2.5}\right)^2 = 2.6 t yr$ 

![](_page_28_Figure_0.jpeg)

Exposure needed for S/N = 4 at  $M_{ee}$ =50 meV Assume BI= 3 10<sup>-3</sup>/(keV kg yr);  $\varepsilon f_{230} f_{act}$ =0.7  $N_{ee} (3 \cdot 10^{26}) = \varepsilon \cdot 10 \cdot M_{130} t (t \text{ yr}) = 7 \cdot M_{130} t (t \text{ yr})$   $N_b = \Delta E \cdot BI \cdot M_{130} t = 6 \cdot 12 \cdot 10^{-3} \cdot 10^3 \cdot M_{130} t = 72 \cdot M_{130} t$   $S / N = \frac{7}{\sqrt{72}} \sqrt{M_{130} t} = 0.82 \sqrt{M_{130} t}$   $M_{130} t (3 \cdot 10^{26}) = (\frac{4}{0.82})^2 = 24 \text{ t yr}$ August 20, 13 A. Bettini, LSC and Padova

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### **Conclusions**

•Is it now "possible to ask to the experience to decide between this new theory and the simple extension of the Dirac equations to the neutral particles"?

•Enormous progress has been done, both in the theory and in the experiments. It is now possible to ask, but no answer yet

•Theory (+experiment) should clarify the  $g_A$  issue, and more

•Experiments taking data or close to do so will reach 150-100 meV sensitivity in this decennium

•Reaching 50 meV discovery will need

- •Ton scale isotope mass
- •Energy resolution FWHM <1%
- •a major effort to achieve BI of 10<sup>-4</sup> / (keV kg yr)

•Tags of the final state (SS vs MS, track images,....)

•Other ideas, not discussed here, are being pursued at R&D level

•Nature may be kind with us, once more (LMA,  $\theta_{13}$ ), choosing a not too small Majorana mass

### **THANKS**

### Sakata forbidden

$$p\overline{p} \to K_L^0 K_S^0$$

The decay can happen only from negative parity states

**Argument for pedestrians**. In the Sakata model the neutral kaons are made of neutrons and  $\Lambda$ 's and their antiparticles and contain no protons nor antiprotons. The charged pions and kaons all contain a proton or antiproton. Thus a proton-antiproton system can become two charged pions or kaons by creating a single additional neutron- antineutron or  $\Lambda$ -anti- $\Lambda$  pair which combines with the initial proton and antiproton to form the two final mesons. This cannot occur for the neutral kaon pair final state

**SU3 based argument**  $\Lambda \overline{\Lambda} \rightarrow \pi^+ \pi^-$  forbidden for odd parity  $I(\pi \pi) = I(\Lambda \overline{\Lambda}) = 0$   $\pi \pi$  space wave function must be symmetric, even parity

In the Sakata model there is an SU(3) transformation  $p \Leftrightarrow \Lambda$  $\pi^{-}(\bar{p}n) \Rightarrow K^{0}(\bar{\Lambda}n)$  $\pi^{+}(p\bar{n}) \Rightarrow \bar{K}^{0}(\Lambda\bar{n})$ 

and the selection rule becomes

 $p\overline{p} \rightarrow K^0 \overline{K}^0$  forbidden for odd parity

In the quark model  $u \Leftrightarrow s \qquad \Lambda \Leftrightarrow \Sigma$ 

Lipkin Prog.Theor.Phys.Suppl.167:155-162,2007

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SNO+

Planning to dissolve natural Te in liquid scintillator

![](_page_32_Figure_2.jpeg)

M. Mottran @ EPS HEP 2013