

# Do we have the explanation for the families and their properties, for the scalar Higgs and Yukawa couplings and for the gauge vector fields?

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- *Modern Phys. Lett.* **A 10**, 587-595 (1995),
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More than **30 years ago** the **standard model** offered an elegant new step in understanding the origin of fermions and bosons.

**It postulated, stimulated by the observations:**

- The existence of the **massless family members**;  
**coloured quarks and colourless leptons**,  
the **left handed members** distinguishing from the **right handed ones** in the **weak** and **hyper charges**.
- The existence of **families**.

$\alpha$ name	hand- edness $-4iS^{03}S^{12}$	weak charge $\tau^{13}$	hyper charge $Y$	colour charge	elm charge $Q$
$u_L^i$	-1	$\frac{1}{2}$	$\frac{1}{6}$	colour triplet	$\frac{2}{3}$
$d_L^i$	-1	$-\frac{1}{2}$	$\frac{1}{6}$	colour triplet	$-\frac{1}{3}$
$\nu_L^i$	-1	$\frac{1}{2}$	$-\frac{1}{2}$	colourless	0
$e_L^i$	-1	$-\frac{1}{2}$	$-\frac{1}{2}$	colourless	-1
$u_R^i$	1	weakless	$\frac{2}{3}$	colour triplet	$\frac{2}{3}$
$d_R^i$	1	weakless	$-\frac{1}{3}$	colour triplet	$-\frac{1}{3}$
$\nu_R^i$	1	weakless	0	colourless	0
$e_R^i$	1	weakless	-1	colourless	-1

Members of each of the  $i = 1, 2, 3$  massless families before the electroweak break.

And the **anti-fermions** to each family and family member.

- Three **massless vector fields**, the gauge fields to the observed **charges** of the family **members**, before the **electroweak break**.

name	hand- edness	weak charge	hyper charge	colour charge	elm charge
hyper photon	0	0	0	colourless	0
weak bosons	0	triplet	0	colourless	triplet
gluons	0	0	0	colour octet	0

They all are vectors in  $d = (1 + 3)$ , in the adjoint representations with respect to the weak, colour and hyper charges.

Elm. charge = weak charge + hyper charge.

- The existence of one **scalar field**, the **Higgs** (and the **anti Higgs**),  
**chosen** to be a **weak doublet**, (like **fermions**) with the appropriate hyper charge in order to "dress" **right handed family members** with the weak and the hyper charge of their **left handed partners**  
and to assure the appropriate mass ratios of **weak bosons**.
- **The existence** of the **Yukawa couplings**,

$$Y^\alpha \frac{v}{\sqrt{2}}$$

taking care of the masses of **fermions**, together with the **Higgs**.

- The Higgs field, the scalar in  $d = (1 + 3)$ , with  $P_R = (-1)^{2s+3B+L} = 1$ .

name	hand- edness	weak charge	hyper charge	colour charge	elm charge
0· Higgs <sub>u</sub>	0	$\frac{1}{2}$	$\frac{1}{2}$	colourless	1
$\langle \text{Higgs}_d \rangle$	0	$-\frac{1}{2}$	$\frac{1}{2}$	colourless	0

name	hand- edness	weak charge	hyper charge	colour charge	elm charge
$\langle \text{Higgs}_u \rangle$	0	$\frac{1}{2}$	$-\frac{1}{2}$	colourless	0
0· Higgs <sub>d</sub>	0	$-\frac{1}{2}$	$-\frac{1}{2}$	colourless	-1

## Let us summarize the standard model assumptions

- All fermions have all the charges, which are not singlets, in the fundamental representations of the charge groups.
- All gauge bosons have all the charges, which are not singlets, in the adjoint representations of the corresponding groups. The singlet values are all zero for all the gauge fields.
- Higgs scalars are doublets with respect to the weak charge.
- Yukawa couplings carry the family quantum numbers.



**The *standard model* assumptions have been confirmed without offering surprises.**

**The last unobserved field, the **scalar Higgs**, detected in June 2012, was confirmed in March 2013.**

**What questions should one urgently ask so that the answers would help to make the right next step beyond the standard model?**

- **Why there exist families at all? Or rather: What is the origin of families?**  
How many families are there? And what are their properties if there are more than the so far observed ones?
- **Why family members – quarks and leptons – manifest so different properties if they all start as massless?**

- How is the **origin of the scalar field** (the Higgs) and the **Yukawa couplings connected with the origin of families?** **How many scalar fields** determine properties of the so far (and others possibly to be) observed fermions and masses of bosons?
- **Why are all the scalar fields doublets with respect to the weak charge?** What are their **representations with respect to the family quantum numbers?**
- Where does the **dark matter originate?**
- Where do the **charges and correspondingly the so far (and others possibly be) observed gauge fields originate?**
- What is the dimension of the space?  $(1 + 3)?$ ,  $(1 + (d - 1))?$   
What is  $d$ ?

- **What** is the role of the **symmetries**: **discrete, continues, global and gauge, fermion-antifermion asymmetry?**
- And many others.

## My statement:

- **Next trustable step beyond the standard model must offer answers to several open questions not only to one.**
- **There exist not yet observed families, gauge fields, scalar fields.**  
**The appearance of Yukawa couplings speaks for several scalar fields.**
- **Dimension of the space is large than 4.**



In the literature **NO explanation for the existence of the families can be found**. Several extensions of the **standard model** are, however, proposed, like:

- **A tiny extension**: The inclusion of the right handed neutrinos into the family.
- The  $SU(3)$  group is assumed to describe – not explain – the existence of three families.
- Like Higgs has the charge in the fundamental representation of the group, also Yukawas are assumed to be scalar fields, in the bi-fundamental representation of the  $SU(3)$  group.
- Supersymmetric theories assuming the existence of partners to the existing fermions and bosons, with charges in the opposite representations.

**The spin-charge-family-theory does offer  
a possible explanation for the existence of families,  
offering answers besides to the "urgent" open questions  
also to many of the "not so urgent" open  
questions, presented above.**

## Content of the talk

- A brief introduction into the **spin-charge-family-theory**.
- Achievements of the **spin-charge-family-theory** so far.
- Some new predictions for the measurements.
- **Problems in this theory to be solved.**



The **Spin-Charge-Family-Theory** is offering **the explanation for:**

- The **existence of families and family members.**
- The **origin of several scalar fields**, which offer the (hopefully right) explanation for the **origin of mass matrices of fermions, correspondingly for the origin of Yukawa couplings and masses of gauge fields.**
- The **origin of charges.**
- The **origin of gauge fields.**
- The **origin of dark matter.**
- **And...**



# Is the spin-charge-family theory the right way at least as a first step beyond the standard model?

- **Spinors** carry in  $d \geq (1 + 13)$  **two kinds of the spin**. No charges.  
In  $d = (1 + 3)$  the **Dirac spin** ( $\gamma^a$ ) takes care of **the spin and the charges of quarks and leptons**.  
The **second kind of the spin** ( $\tilde{\gamma}^a$ ) **generates families**.
- **Spinors** couple correspondingly to **vielbeins** and to two kinds of **spin connection fields**.  
In  $d = (1 + 3)$  the **spin-connection fields** together with the **vielbeins** manifest as the **gauge vector fields** and the **scalar fields**. The vacuum expectation values of the **scalar fields** determine masses of **fermions** on the tree level.

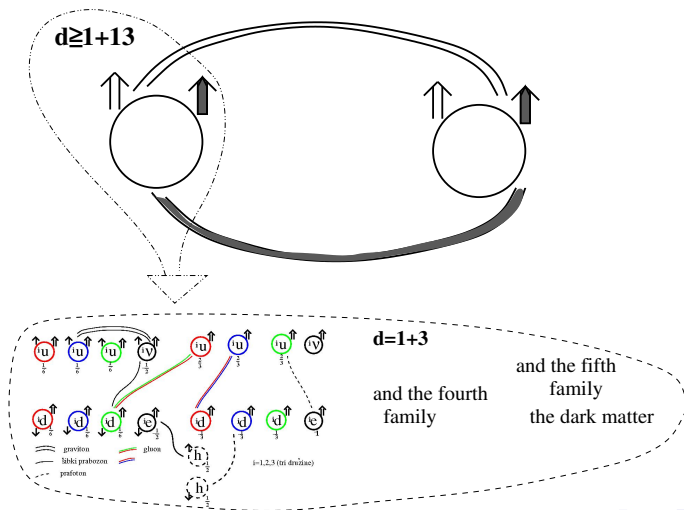
- A simple action in  $d = (1 + 13)$  for **spinors** and **spin connections and vielbeins** manifests in  $d = (1 + 3)$ , after appropriate breaks of the starting symmetry, the **standard model action**
  - 1 for **fermions** – predicting the fourth **family** coupled to the so far observed three and the **dark matter family**,
  - 2 for **gauge fields**, predicting new ones,
  - 3 for **scalar fields**, which take care of **mass matrices** of **fermions** and **masses of weak bosons**, predicting several ones.



- All **vector boson fields** have all the **charges** in the **adjoint representations**.
- The **scalar fields** have the **family charges** in the **adjoint representations**, while they are **doublets** with respect to the **weak charge**.
- All **family members of all families** have all the charges in the **fundamental representations of the corresponding groups**.
- **No supersymmetry is predicted** at low energy regime.



## Introduction



## There are two kinds of the Clifford algebra objects (only two):

- The **Dirac  $\gamma^a$  operators** (used by Dirac 80 years ago).
- The **second one:  $\tilde{\gamma}^a$** , which I recognized.

$$\{\gamma^a, \gamma^b\}_+ = 2\eta^{ab} = \{\tilde{\gamma}^a, \tilde{\gamma}^b\}_+,$$

$$\{\gamma^a, \tilde{\gamma}^b\}_+ = 0,$$

$$(\tilde{\gamma}^a \mathbf{B} : = \mathbf{i}(-)^{n_B} \mathbf{B} \gamma^a) |\psi_0 \rangle,$$

$$(\mathbf{B} = a_0 + a_a \gamma^a + a_{ab} \gamma^a \gamma^b + \dots + a_{a_1 \dots a_d} \gamma^{a_1} \dots \gamma^{a_d}) |\psi_0 \rangle$$

$(-)^{n_B} = +1, -1$ , when the object  $B$  has a Clifford even or odd character, respectively.

$|\psi_0 \rangle$  is a vacuum state on which the operators  $\gamma^a$  **apply**.

$$\mathbf{S}^{ab} := (\mathbf{i}/4)(\gamma^a \gamma^b - \gamma^b \gamma^a),$$

$$\tilde{\mathbf{S}}^{ab} := (\mathbf{i}/4)(\tilde{\gamma}^a \tilde{\gamma}^b - \tilde{\gamma}^b \tilde{\gamma}^a),$$

$$\{\mathbf{S}^{ab}, \tilde{\mathbf{S}}^{cd}\}_- = \mathbf{0}.$$

- $\tilde{\mathbf{S}}^{ab}$  define the equivalent representations with respect to  $\mathbf{S}^{ab}$ .

My recognition:

- If  $\gamma^a$  are used to describe **the spin and the charges of spinors**,  
 $\tilde{\gamma}^a$  can be used to describe families of spinors..

**Must be used!!**



A simple action for a **spinor** which carries in  $d = (1 + 13)$  only **two kinds of a spin** (no charges) and for **the gauge fields**

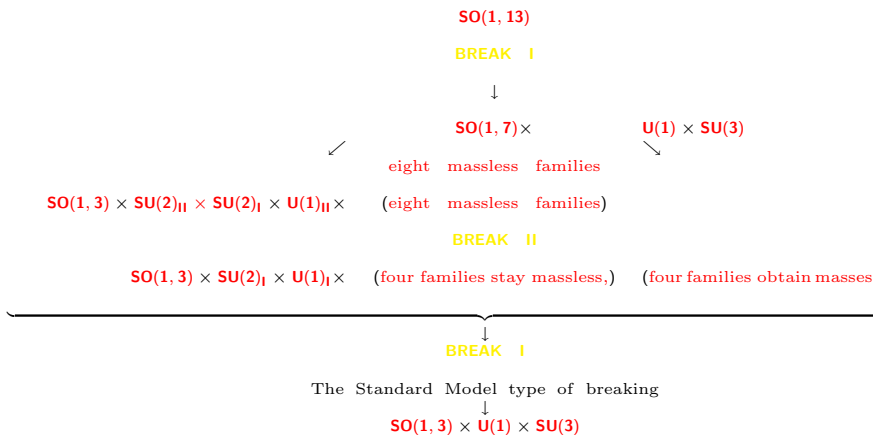
$$\mathbf{S} = \int d^d x E \mathcal{L}_f + \int d^d x E (\alpha R + \tilde{\alpha} \tilde{R})$$

$$\mathcal{L}_f = \frac{1}{2} (E \bar{\psi} \gamma^a p_{0a} \psi) + h.c.$$

$$p_{0a} = f^\alpha{}_a p_{0\alpha} + \frac{1}{2E} \{p_\alpha, E f^\alpha{}_a\} -$$

$$\mathbf{p}_{0\alpha} = \mathbf{p}_\alpha - \frac{1}{2} \mathbf{S}^{ab} \omega_{ab\alpha} - \frac{1}{2} \tilde{\mathbf{S}}^{ab} \tilde{\omega}_{ab\alpha}$$

- The only internal degrees of freedom of **spinors** (fermions) are the **two kinds of the spin**.
- The only **gauge fields** are the **gravitational ones** – **vielbeins and two kinds of spin connections**.

Breaks of symmetries when starting with **massless spinors**



- The action for spinors at the low energy regime

$$\mathcal{L}_f = \bar{\psi} \gamma^m (p_m - \sum_{A,i} g^A \tau^{Ai} A_m^{Ai}) \psi +$$

$$\left\{ \sum_{s=[7],[8]} \bar{\psi} \gamma^s p_{0s} \psi \right\} +$$

the rest ,

$$p_{0m} = f_m^\mu (p_\mu - \sum_A g^A \vec{\tau}^A \vec{A}_\mu^A),$$

$$p_{0s} = f_s^\sigma (p_\sigma - \sum_B g^B \vec{\tau}^B \vec{A}_\sigma^B - \sum_B \tilde{g}^B \vec{\tau}^B \tilde{\vec{A}}_\sigma^B).$$

$$\tau^{Ai} = \sum_{a,b} c^{Ai}_{ab} S^{ab}, \quad \tilde{\tau}^{Ai} = \sum_{a,b} \tilde{c}^{Ai}_{ab} \tilde{S}^{ab},$$

## Before the last two breaks, BREAK II and Break I, of symmetries there are eight massless families of fermions.

- It is the term  $\bar{\psi} \gamma^s p_{0s} \psi$ ,  $s \in \{[7], [8]\}$  which determines massess of fermions on the tree level.
- Before the electroweak break ( BREAK I) the four out of eight families remain massless. Four of the eight gain masses.
- The lowest among the **decoupled** upper, massive after the  $SU(2)_{II} \times U(1)_{II}$  break, four families is the **candidate** for forming the **dark matter** clusters.



## Our technique to represent spinors works elegantly.

- *J. of Math. Phys.* **43**, 5782-5803 (2002), hep-th/0111257,
- *J. of Math. Phys.* **44** 4817-4827 (2003), hep-th/0303224,  
both with H.B. Nielsen.

$$\begin{matrix} \text{ab} \\ (\pm \mathbf{i}) \end{matrix} : = \frac{1}{2}(\gamma^{\mathbf{a}} \mp \gamma^{\mathbf{b}}), \quad \begin{matrix} \text{ab} \\ [\pm \mathbf{i}] \end{matrix} := \frac{1}{2}(1 \pm \gamma^{\mathbf{a}}\gamma^{\mathbf{b}})$$

$$\text{for } \eta^{aa}\eta^{bb} = -1,$$

$$\begin{matrix} \text{ab} \\ (\pm) \end{matrix} : = \frac{1}{2}(\gamma^{\mathbf{a}} \pm \mathbf{i}\gamma^{\mathbf{b}}), \quad \begin{matrix} \text{ab} \\ [\pm] \end{matrix} := \frac{1}{2}(1 \pm i\gamma^{\mathbf{a}}\gamma^{\mathbf{b}}),$$

$$\text{for } \eta^{aa}\eta^{bb} = 1$$

with  $\gamma^{\mathbf{a}}$  which are the usual **Dirac operators**





$$\begin{aligned}
 \mathbf{S}^{ab}(\mathbf{k}) &= \frac{k^{ab}}{2}(\mathbf{k}), & \mathbf{S}^{ab}[\mathbf{k}] &= \frac{k^{ab}}{2}[\mathbf{k}], \\
 \tilde{\mathbf{S}}^{ab}(\mathbf{k}) &= \frac{k^{ab}}{2}(\mathbf{k}), & \tilde{\mathbf{S}}^{ab}[\mathbf{k}] &= -\frac{k^{ab}}{2}[\mathbf{k}].
 \end{aligned}$$



$\gamma^a$  transforms  $\binom{ab}{k}$  into  $[-k]$ , never to  $\binom{ab}{k}$ .

$\tilde{\gamma}^a$  transforms  $\binom{ab}{k}$  into  $\binom{ab}{k}$ , never to  $[-k]$ .





$S^{ab}$  generate **all the members of one family**. The eightplet (the representation of  $SO(1, 7)$ ) of quarks of a particular colour charge

i		$ \psi_i\rangle$	$\Gamma^{(1,3)}$	$S^{12}$	$\Gamma^{(4)}$	$\tau^{13}$	$\tau^{23}$	$Y$	$\tau^4$
		Octet, $\Gamma^{(1,7)} = 1$ , $\Gamma^{(6)} = -1$ , of quarks							
1	$u_R^c1$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ (+i)(+) &   & (+)(+) &    & (+)(-) & (-) & (-) & \end{matrix}$	1	$\frac{1}{2}$	1	0	$\frac{1}{2}$	$\frac{2}{3}$	$\frac{1}{6}$
2	$u_R^c1$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ [-i] & [-] &   & (+)(+) &    & (+)(-) & (-) & \end{matrix}$	1	$-\frac{1}{2}$	1	0	$\frac{1}{2}$	$\frac{2}{3}$	$\frac{1}{6}$
3	$d_R^c1$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ (+i)(+) &   & [-] & [-] &    & (+)(-) & (-) & \end{matrix}$	1	$\frac{1}{2}$	1	0	$-\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{6}$
4	$d_R^c1$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ [-i] & [-] &   & [-] & [-] &    & (+)(-) & (-) \end{matrix}$	1	$-\frac{1}{2}$	1	0	$-\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{6}$
5	$d_L^c1$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ [-i] & (+) &   & (-)(+) &    & (+)(-) & (-) & \end{matrix}$	-1	$\frac{1}{2}$	-1	$-\frac{1}{2}$	0	$\frac{1}{6}$	$\frac{1}{6}$
6	$d_L^c1$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ (+i) & [-] &   & [-] & (+) &    & (+)(-) & (-) \end{matrix}$	-1	$-\frac{1}{2}$	-1	$-\frac{1}{2}$	0	$\frac{1}{6}$	$\frac{1}{6}$
7	$u_L^c1$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ [-i] & (+) &   & (+)[-] &    & (+)(-) & (-) & \end{matrix}$	-1	$\frac{1}{2}$	-1	$\frac{1}{2}$	0	$\frac{1}{6}$	$\frac{1}{6}$
8	$u_L^c1$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ (+i) & [-] &   & (+)[-] &    & (+)(-) & (-) & \end{matrix}$	-1	$-\frac{1}{2}$	-1	$\frac{1}{2}$	0	$\frac{1}{6}$	$\frac{1}{6}$

$\gamma^0 \gamma^7$  and  $\gamma^0 \gamma^8$  transform  $u_R$  of the 1<sup>st</sup> row into  $u_L$  of the 7<sup>th</sup> row, and  $d_R$  of the 4<sup>rd</sup> row into  $d_L$  of the 6<sup>th</sup> row,

doing what the Higgs and  $\gamma^0$  do in the Stan. model.





**In the standard model** the families exist by assumption.

In the **spin-charge-family-theory the families are created.**

- $\gamma^a$  transforms  $\binom{ab}{k}$  into  $[-k]$ , never to  $\binom{ab}{k}$ .  
 $S^{ab}$  transform one family member into another one.
- $\tilde{\gamma}^a$  transforms  $\binom{ab}{k}$  into  $\binom{ab}{k}$ , never to  $[-k]$ .  
 $\tilde{S}^{ab}$  transform a family member into the same family member of another family.

**Eight families** of  $u_R$  with the spin 1/2 of a particular colour and of a **colourless**  $\nu_R$  :

$I_R$	$u_R^{c1}$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 10 & 11 & 12 & 13 & 14 \\ (+i) & [+ ] &   & [+ ] & (+) &    & (+) & [- ] & [- ] \end{matrix}$	$\nu_R$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 10 & 11 & 12 & 13 & 14 \\ (+i) & [+ ] &   & [+ ] & (+) &    & (+) & (+) & (+) \end{matrix}$
$II_R$	$u_R^{c1}$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 10 & 11 & 12 & 13 & 14 \\ [+i] & (+) &   & [+ ] & (+) &    & (+) & [- ] & [- ] \end{matrix}$	$\nu_R$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 10 & 11 & 12 & 13 & 14 \\ [+i] & (+) &   & [+ ] & (+) &    & (+) & (+) & (+) \end{matrix}$
$III_R$	$u_R^{c1}$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 10 & 11 & 12 & 13 & 14 \\ (+i) & [+ ] &   & (+) & [+ ] &    & (+) & [- ] & [- ] \end{matrix}$	$\nu_R$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 10 & 11 & 12 & 13 & 14 \\ (+i) & [+ ] &   & (+) & [+ ] &    & (+) & (+) & (+) \end{matrix}$
$IV_R$	$u_R^{c1}$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 10 & 11 & 12 & 13 & 14 \\ [+i] & (+) &   & (+) & [+ ] &    & (+) & [- ] & [- ] \end{matrix}$	$\nu_R$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 10 & 11 & 12 & 13 & 14 \\ [+i] & (+) &   & (+) & [+ ] &    & (+) & (+) & (+) \end{matrix}$
$V_R$	$u_R^{c1}$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 10 & 11 & 12 & 13 & 14 \\ (+i) & (+) &   & (+) & (+) &    & (+) & [- ] & [- ] \end{matrix}$	$\nu_R$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 10 & 11 & 12 & 13 & 14 \\ (+i) & (+) &   & (+) & (+) &    & (+) & (+) & (+) \end{matrix}$
$VI_R$	$u_R^{c1}$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 10 & 11 & 12 & 13 & 14 \\ (+i) & (+) &   & [+ ] & [+ ] &    & (+) & [- ] & [- ] \end{matrix}$	$\nu_R$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 10 & 11 & 12 & 13 & 14 \\ (+i) & (+) &   & [+ ] & [+ ] &    & (+) & (+) & (+) \end{matrix}$
$VII_R$	$u_R^{c1}$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 10 & 11 & 12 & 13 & 14 \\ [+i] & [+ ] &   & (+) & (+) &    & (+) & [- ] & [- ] \end{matrix}$	$\nu_R$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 10 & 11 & 12 & 13 & 14 \\ [+i] & [+ ] &   & (+) & (+) &    & (+) & (+) & (+) \end{matrix}$
$VIII_R$	$u_R^{c1}$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 10 & 11 & 12 & 13 & 14 \\ [+i] & [+ ] &   & [+ ] & [+ ] &    & (+) & [- ] & [- ] \end{matrix}$	$\nu_R$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 10 & 11 & 12 & 13 & 14 \\ [+i] & [+ ] &   & [+ ] & [+ ] &    & (+) & (+) & (+) \end{matrix}$

Before the break of

$SO(1, 3) \times \mathbf{SU}(2)_I \times \mathbf{SU}(2)_{II} \times \mathbf{U}(1)_{III} \times SU(3)$  into

$SO(1, 3) \times \mathbf{SU}(2)_I \times \mathbf{U}(1)_I \times SU(3)$

all the eight families are massless.



At the symmetry  $SO(1, 7) \times U(1)_{II} \times SU(3)$  there are  $2^{(1+7)/2-1} (= 8)$  massless families of **fermions**

which stay massless also after the break into  $SO(1, 3) \times SU(2)_I \times SU(2)_{II} \times U(1)_{II} \times SU(3)$ .

- The **scalar fields**  $\tilde{A}_S^{\tilde{A}i}$  and  $A_S^{Bj}$ , in adjoint representations with respect to the family groups, are obviously **doublets** with respect to the weak charge group. The mass term

$$\sum_{s=[7],[8]} \bar{\psi}_L \gamma^s (\mathbf{p}_s - \sum_{\tilde{A},i} \tilde{g}^{\tilde{A}} \tilde{\tau}^{\tilde{A}i} \tilde{A}_S^{\tilde{A}i} - \sum_{B,j} \mathbf{g}^B \tau^{Bj}, \mathbf{A}_S^{Bj}) \psi_R$$

namely does what the *standard model* Higgs does:  
Transforms the right handed quarks and leptons into the left handed partners, generating the mass matrices.

- To the break of symmetries from  $SU(2)_I \times SU(2)_{II} \times U(1)_{III}$  to  $SU(2)_I \times U(1)_I$  only scalar fields which are triplets with respect to  $\vec{T}^2$  and  $\vec{N}_R$  (are assumed to) contribute.

$$\tilde{\mathbf{A}}_S^{2i}, \tilde{\mathbf{A}}_S^{\tilde{N}_R i}$$

- To the break of symmetries from  $SU(2)_I \times U(1)_I$  to  $U(1)$  both kinds of scalar fields (are assumed to) contribute, those which are triplets with respect to  $\vec{T}^1$  and  $\vec{N}_L$

$$\tilde{\mathbf{A}}_S^{1i}, \tilde{\mathbf{A}}_S^{\tilde{N}_L i}$$

and singlets

$$\mathbf{A}_S^{Y'}, \mathbf{A}_S^{Q'}, \mathbf{A}_S^Q.$$



Before the BREAK II the vielbeins (together with the spin connection fields of  $S^{ab}$ ) manifest the **massless gauge vector fields** in (1+3)

$$g^4 \tau^4 \mathbf{A}_m^4, \quad g^2 \tau^{2i} \mathbf{A}_m^{2i}, \\ g^1 \tau^{1i} \mathbf{A}_m^{1i}, \quad g^3 \tau^{3i} \mathbf{A}_m^{3i},$$

and the vielbeins together with the spin connection fields of  $\tilde{S}^{ab}$  and  $S^{st}$  manifest in  $d = (1 + 3)$  the **scalar gauge fields** of  $\tau^{Ai}$  and  $\tilde{\tau}^{\tilde{A}i}$

$$g_1^1 \tau^{1i} \mathbf{A}_s^{1i}, \quad g_1^1 \tau^{2i} \mathbf{A}_s^{2i}, \\ \tilde{g}^2 \tilde{\tau}^{2i} \tilde{\mathbf{A}}_s^{2i}, \quad \tilde{g}^1 \tilde{\tau}^{1i} \tilde{\mathbf{A}}_s^{1i}, \\ \tilde{g}^{\tilde{N}_R} \tilde{\mathbf{N}}_R^i \tilde{\mathbf{A}}_s^{\tilde{N}_R i}, \quad \tilde{g}^{\tilde{N}_L} \tilde{\mathbf{N}}_L^i \tilde{\mathbf{A}}_s^{\tilde{N}_L i}.$$

The **spin-charge-family** theory action resembles after the first of the two breaks **the standard model** action before the electroweak break.

There are also many differences, like:

- There are **several scalar fields**, with the family **charges** in the **adjoint representations**, while they all are **doublets** with respect to the **weak charge**.
- There is the operator  $\frac{1}{2}(\gamma^7 \mp \gamma^8) = (\pm)^{78}$ , which does, in the usual way, the **"dressing" job** of the **Higgs**.
- There are **twice four families** predicted at the low energy regime, **four** of them **forming families** out of which there are the **measured** ones. There is the **dark matter family** as well.



Achievements of the **spin-charge-family-theory** so far concerning:

- **Families:** Two decoupled groups of four families, three of the lowest four observed, the lowest of the upper four are expected to form the dark matter.
- **Scalar fields:** Two decoupled groups of scalar fields: contributing to the mass matrices of the twice four families.
- **Massive vector boson fields:** The  $SU(2)_{II}$  and the  $SU(2)_I$  (the weak) bosons.

- The fifth family is stable. Its elm **neutral baryons** (neutrinos also contribute) form the **dark matter**.
- **Direct measurements and cosmological evolution limit my fifth family mass** to  
 $10 \text{ TeV} < m_{q_5} c^2 < 10^3 \text{ TeV}$ .
- The dark matter baryons are opening an interesting new "fifth family nuclear" dynamics.

hep-ph/0711.4681,p.189-194; *Phys. Rev. D* **80**, 083534 (2009);

## The lowest four families

The mass matrix of any family member, of any **quark** and any **lepton**, **obeys the same symmetry** – the symmetry required by the **spin-charge-family theory** on the tree level and (almost) proven to be kept in all loop corrections.

We simplify the present study by assuming:

- The mass matrices are Hermitian and real.
- The mixing matrices are real unitary  $4 \times 4$  matrices.

The effective Lagrange density for spinors is **after the electroweak break** close to what the **standard model** assumes

$$\mathcal{L}_f = \bar{\psi} (\gamma^m \mathbf{p}_{0m} - \mathbf{M}) \psi,$$

$$p_{0m} = \mathbf{p}_m - \{ \mathbf{e} \mathbf{Q} \mathbf{A}_m + \mathbf{g}^1 \cos \theta \mathbf{Q}' \mathbf{Z}_m^{Q'} + \frac{\mathbf{g}^1}{\sqrt{2}} (\tau^{1+} \mathbf{W}_m^{1+} + \tau^{1-} \mathbf{W}_m^{1-}) + g^2 \cos \theta_2 Y' A_m^{Y'} \},$$

$$\bar{\psi} \mathbf{M} \psi = \bar{\psi} \gamma^s \mathbf{p}_{0s} \psi$$

$$p_{0s} = p_s - \{ \tilde{g}^{\tilde{N}_L} \tilde{N}_L \tilde{A}_s^{\tilde{N}_L} + \tilde{g}^{\tilde{Q}'} \tilde{Q}' \tilde{A}_s^{\tilde{Q}'} + \frac{\tilde{g}^1}{\sqrt{2}} (\tilde{\tau}^{1+} \tilde{A}_s^{1+} + \tilde{\tau}^{1-} \tilde{A}_s^{1-}) + e Q A_s + g^1 \cos \vartheta_1 Q' Z_s^{Q'} + g^2 \cos \vartheta_2 Y' A_s^{Y'} \}.$$



Mass matrices of **quarks and leptons** have after the electroweak break **after taking into account loop corrections in all orders a very determined symmetry**

$$\mathcal{M}^\alpha = \begin{pmatrix} -a_1 - a & e & d & b \\ e & -a_2 - a & b & d \\ d & b & a_2 - a & e \\ b & d & e & a_1 - a \end{pmatrix}.$$

- We take the diagonal matrix elements  $\mathcal{M}_d^\alpha$ ,  $\alpha = \{u, d, \nu, e\}$  and the mixing matrices  $V_{\alpha\beta}$  for the quark pair and the lepton pair from the experimental data, assuming that there is  $4 \times 4$  mixing matrix which is unitary.

**The unitary conditions for the  $n \times n$  matrix when applied on the  $(n - 1) \times (n - 1)$  submatrix, determine for  $n \geq 4$  the  $n \times n$  matrix uniquely.**

For an orthogonal matrix this is the case for any  $n$ .

If assuming that  $(n - 1) \times (n - 1)$  submatrix is unitary, we lose  $(2n - 1)$  informations, when the free choice of phases are taken into account  $(2n - 1)$  goes into  $(2n - 3)$ .

For an orthogonal matrix we lose in this case  $(n - 1)$  informations.

- Taking into account the invariants

$$\sum_{i=1,4} m_i^\alpha, \quad \sum_{i>j=1,4} m_i^\alpha m_j^\alpha, \quad \sum_{i>j>k=1,4} m_i^\alpha m_j^\alpha m_k^\alpha, \\ m_1^\alpha m_2^\alpha m_3^\alpha m_4^\alpha,$$

determined by the masses of the three families and depending on the fourth family mass, we reduce the number of free parameters of each mass matrix from 6 (7) to 3 (4).

- The orthogonal mixing matrix, if known for three families exactly, determines all  $6 = 3 + 3$  free parameters of the two family members.

- This would determine in the **spin-charge-family theory** the **masses and the mixing matrices of the four families of quarks and leptons uniquely** in the case, that **i.**  $b_1 = b_2$ , that **ii.** all the experimental data would be measured accurately and that **iii.** orthogonality and reality of mixing matrices would be a good assumption.
- The measured values within the **experimental accuracy enable** to determine the **intervals** of the **fourth family members masses**.
- **The accurate enough experiments** would **confirm or exclude** the **fourth family**.



## We follow the procedure:

- The diagonalizing matrices  $S^\alpha$  and  $S^\beta$ , each depending on 3 (for  $b_1 = b_2$  otherwise 4) free parameters, are for real and symmetric mass matrices orthogonal. They follow from the procedure

$$M^\alpha = S^\alpha \mathbf{M}_d^\alpha T^{\alpha\dagger}, \quad T^\alpha = S^\alpha F^\alpha S F^\alpha T^\dagger,$$

$$\mathbf{M}_d^\alpha = (m_1^\alpha, m_2^\alpha, m_3^\alpha, m_4^\alpha),$$

in two ways

$$A.: S^\beta = V_{\alpha\beta}^\dagger S^\alpha, \quad B.: S^\alpha = V_{\alpha\beta} S^\beta,$$

$$A.: V_{\alpha\beta}^\dagger S^\alpha \mathbf{M}_d^\beta S^{\alpha\dagger} V_{\alpha\beta} = M^\beta, \quad B.: V_{\alpha\beta} S^\beta \mathbf{M}_d^\alpha S^{\beta\dagger} V_{\alpha\beta}^\dagger = M^\alpha.$$

We use both ways iteratively.

With Gregor Bregar we **treat quarks and leptons in an equivalent way**:

- **Quarks** (very preliminary, intervals are not yet determined):

$$\mathbf{M}_d^u / \text{MeV}/c^2 = (1.24703, 620.141, 172\,000., 650\,000.?)),$$

$$\mathbf{M}_d^d / \text{MeV}/c^2 = (2.92494, 54.793, 2\,899., 700\,000.?)),$$

$$|V_{ud}|_{ij} = \begin{pmatrix} 0.9740 & -0.2243 & -0.0041 & \mathbf{0.0306} \\ 0.2242 & 0.9737 & -0.0409 & \mathbf{-0.0049} \\ 0.0084 & 0.0403 & 0.986 & \mathbf{0.1616} \\ \mathbf{-0.031} & \mathbf{-0.0052} & \mathbf{-0.162} & \mathbf{0.9864} \end{pmatrix}_{ij},$$

$$\mathcal{M}^u = \begin{pmatrix} 101\,630 & -46\,077 & -46\,154 & -94\,733 \\ -46\,077 & 321\,824 & 315\,685 & -46\,154 \\ -46\,154 & 315\,685 & 309\,681 & -46\,077 \\ -94\,733 & -46\,154 & -46\,077 & 98\,4880 \end{pmatrix} \quad \mathcal{M}^d = \begin{pmatrix} 36\,244 & 104\,497 & 104\,484 & -36\,223 \\ 104\,497 & 315\,176 & 315\,198 & -104\,484 \\ 104\,484 & 315\,198 & 315\,235 & -104\,497 \\ -36\,223 & -104\,481 & -104\,497 & 36\,304 \end{pmatrix}$$

- **Leptons** (very preliminary, intervals are not yet determined):

$$\mathbf{M}_d^\nu / \text{MeV}/c^2 = (5 \cdot 10^{-9}?, 1 \cdot 10^{-8}?, 5 \cdot 10^{-8}?, 60? 000,$$

$$\mathbf{M}_d^e / \text{MeV}/c^2 = (0.510998928?, 105.6583715?, 1776.82? 120 000)$$

$$|V_{\nu e}|_{ij} = \begin{pmatrix} 0.9740 & -0.2243 & -0.0041 & \mathbf{0.0306} \\ 0.2242 & 0.9737 & -0.0409 & \mathbf{-0.0049} \\ 0.0084 & 0.0403 & 0.986 & \mathbf{0.1616} \\ \mathbf{-0.031} & \mathbf{-0.0052} & \mathbf{-0.162} & \mathbf{0.9864} \end{pmatrix}_{ij},$$

$$\mathcal{M}^\nu = \begin{pmatrix} 14\,021 & 14\,968 & 14\,968 & -14\,021 \\ 14\,968 & 15\,979 & 15\,979 & -14\,968 \\ 14\,968 & 15\,979 & 15\,979 & -14\,968 \\ -14\,021 & -14\,968 & -14\,968 & 14\,021 \end{pmatrix} \quad \mathcal{M}^e = \begin{pmatrix} 28\,933 & 30\,057 & 29\,762 & -27\,207 \\ 30\,057 & 32\,009 & 31\,958 & -29\,762 \\ 29\,762 & 31\,958 & 32\,009 & -30\,057 \\ -27\,207 & -29\,762 & -30\,057 & 28\,933 \end{pmatrix}$$

**Summarizing properties of quarks and leptons** following from the **spin-charge-family** theory and **experimental data**:

- We treat **quarks and leptons in equivalent way**. Differences in the properties of quarks and leptons are due to different couplings of family members to the scalars  $A_S^Q$ ,  $A_S^{Q'}$  and  $A_S^{Y'}$ .
- **The theory predicts**, so far very preliminary, **masses of the fourth family members within some intervals, due to the inaccuracy of the experimental data.**

## Scalar fields at the electroweak break

- There are **two triplets and three singlets** with respect to the family quantum numbers. All are **doublets** with respect to the weak charge:  $\phi^{Ai} = [\tilde{\mathbf{A}}_{\pm}^{\tilde{N}_{Li}}, \tilde{\mathbf{A}}_{\pm}^{\tilde{1}i}, \mathbf{A}_{\pm}^Q, \mathbf{A}_{\pm}^{Q'}, \mathbf{A}_{\pm}^{Y'}]$
- The Lagrange density for scalars are so far assumed

$$\begin{aligned} \mathcal{L}_{sb} &= \frac{1}{2} (p_{0m} \phi^{Ai})^\dagger (p_0^m \phi^{Ai}) - V(\phi^{Ai}), \\ V(\phi^{Ai}) &= \sum_{A,i} \left\{ -\frac{1}{2} (m_{Ai})^2 (\phi^{Ai})^2 + \frac{1}{4} \sum_{B,j} \lambda^{Ai Bj} (\phi^{Ai})^2 (\phi^{Bj})^2 \right\}, \\ p_{0m} &= p_m - g^{Ai} \tau^{Ai} A_m^{Ai}. \end{aligned}$$

- The mass eigenstates  $\Phi^\beta$ :  $\Phi^{Ai} = \sum_\beta C_\beta^{Ai} \Phi^\beta$ .

$$V(\Phi^\beta) = \sum_\beta \left\{ -\frac{1}{2} (m_\beta)^2 (\Phi^\beta)^2 + \frac{1}{4} \lambda^\beta (\Phi^\beta)^4 \right\},$$

$$\frac{\partial V}{\partial \Phi^\beta} \Big|_{v_{Ai}} = 0,$$

- The **scalar fields**  $\gamma^0$  ( $\mp$ )  $\tau^{Ai} \Phi_{\mp}^{Ai}$  transform the **right handed family members** into the the corresponding **left handed partners**

$$\gamma^0 \begin{pmatrix} - \\ \end{pmatrix} \tau^{Ai} \Phi_{-}^{Ai} \psi_{(u,v)R} \rightarrow \tau^{Ai} \Phi_{-}^{Ai} \psi_{(u,v)L},$$

$$\gamma^0 \begin{pmatrix} + \\ \end{pmatrix} \tau^{Ai} \Phi_{+}^{Ai} \psi_{(d,e)R} \rightarrow \tau^{Ai} \Phi_{+}^{Ai} \psi_{(d,e)L}.$$

$$\psi_{(\mathbf{L},\mathbf{R})}^{\alpha k}, \Psi_{(\mathbf{L},\mathbf{R})}^{\alpha k'}, \quad \alpha = (u_{L,R}, d_{L,R}, \nu_{L,R}, e_{L,R}),$$

massless and massive  $k^{th}$  and  $k'^{th}$  component of the four vectors,  
 $k$  and  $k'$  are the **family** quantum numbers:

We have

$$\psi_{(\mathbf{L},\mathbf{R})}^{\alpha} = S^{\alpha} \Psi_{(\mathbf{L},\mathbf{R})}^{\alpha}$$

$$\begin{aligned} \overline{\Psi}^{\alpha} S^{\alpha\dagger} \mathcal{M}^{\alpha} S^{\alpha} \Psi^{\alpha} &= \overline{\Psi}^{\alpha} \text{diag}(m_1^{\alpha}, \dots, m_4^{\alpha}) \Psi^{\alpha}, \\ S^{\alpha\dagger} \mathcal{M}^{\alpha} S^{\alpha} &= \Phi_{\mathbf{f}}^{\alpha}. \end{aligned}$$

The (**Yukawa!!**) couplings of the scalar fields to the  $\alpha$  member of the  $k^{\text{th}}$  family

$$(\Phi_f^\alpha)_{kk'} \Psi^{\alpha k'} = \delta_{kk'} m_{k'}^\alpha \Psi^{\alpha k'}.$$

The superposition of scalar fields in the mass eigenstates basis which couple to fermions

$$\Phi_{fk}^\alpha = \sum_{\beta} D_k^{\alpha\beta} \Phi^\beta.$$



- The **scalar fields** change, when gaining a nonzero vacuum expectation values, properties of the vacuum. At the electroweak BREAK I in the vacuum the new terms appear. In our technique it is

$$\begin{aligned} \begin{matrix} 78 \\ (-) \end{matrix} \ominus_I &: = \begin{matrix} 78 & 56 & 78 \\ (-) & T_{S_{\vec{N}_L}} |([+](+)) & T_{d_{(-)\vec{\tau}^1}} || \end{matrix} \begin{matrix} 9 & 1011 & 1213 & 14 \\ [+][+][+] \end{matrix}, \\ \begin{matrix} 78 \\ (+) \end{matrix} \oplus_I &: = \begin{matrix} 78 & 56 & 78 \\ (+) & T_{S_{\vec{N}_L}} |([-](-)) & T_{d_{(+)\vec{\tau}^1}} || \end{matrix} \begin{matrix} 9 & 1011 & 1213 & 14 \\ [-][-][-] \end{matrix}. \end{aligned}$$

Here  $T_{S_{\vec{N}_L}}$  denotes a triplet with respect to the operators  $\vec{N}_L$  and a singlet with respect to  $\vec{N}_L$ , while  $([+](+)) T_{d_{(\mp)\vec{\tau}^1}}$  are the two triplets with respect to  $\vec{\tau}^1$  and doublets with respect to  $\vec{\tau}^1$ .

■ Due to

$$\begin{aligned} \tau^{1+}\tau^{1-} \begin{matrix} 78 \\ (+) \oplus_I \end{matrix} &= \begin{matrix} 78 \\ (+) \oplus_I \end{matrix}, & \tau^{1-}\tau^{1+} \begin{matrix} 78 \\ (-) \ominus_I \end{matrix} &= \begin{matrix} 78 \\ (-) \ominus_I \end{matrix}, \\ Q \begin{matrix} 78 \\ (+) \oplus_I \end{matrix} &= 0 = Q \begin{matrix} 78 \\ (-) \ominus_I \end{matrix}, \\ Q' \begin{matrix} 78 \\ (+) \oplus_I \end{matrix} &= -\frac{1}{2 \cos^2 \theta_1}, & Q' \begin{matrix} 78 \\ (-) \ominus_I \end{matrix} &= \frac{1}{2 \cos^2 \theta_1}, \end{aligned}$$

the **vector gauge fields**  $A_m^{1\pm} (= W_m^\pm)$  and  $A_m^{Q'} (= Z_m)$   
 $= \cos \theta_1 A_m^{13} - \sin \theta_1 A_m^Y$  become massive, while  $A_m^Q (= \mathbf{A}_m)$   
 $= \sin \theta_2 A_m^{13} + \cos \theta_1 A_m^Y$  stays massless, if  $\frac{g^1}{g^Y} \tan \theta_1 = 1$ .

- Correspondingly the mass term of the **vector gauge bosons** is

$$(p_{0m} \hat{\Phi}_{\mp}^I)^\dagger (p_0^m \hat{\Phi}_{\mp}^I) \rightarrow$$

$$\left(\frac{1}{2}\right)^2 (g^1)^2 v_I^2 \left( \frac{1}{(\cos \theta_1)^2} Z_m^{Q'} Z^{Q' m} + 2 W_m^+ W^{-m} \right),$$

$$\text{Tr}(\Phi_{\mp}^{vI\dagger} \Phi_{\mp}^{vI}) = \frac{v^2}{2}.$$

# What questions is the spin-charge-family theory able to answer?

The stated urgent questions the answers to which would help to make the right next step beyond the standard model.

- **Why there exist families at all?** Or rather: What is the **origin of families?**... offering answers  
How many families are there? And what are their properties if there are more than the so far observed ones?... offering answers
- **Why family members – quarks and leptons – manifest so different properties if they all start as massless?** ... offering answers

- How is the **origin of the scalar field** (the Higgs) and the **Yukawa couplings connected with the origin of families?** ... offering answers  
**How many scalar fields** determine properties of the so far (and others possibly to be) observed fermions and masses of bosons? ... offering answers
- **Why are all the scalar fields doublets with respect to the weak charge?** What are their **representations with respect to the family quantum numbers?** ... offering answers
- **Where does the dark matter originate?** ... offering answers
- Where do the **charges and correspondingly the so far (and others possibly be) observed gauge fields originate?** ...

## What predictions does the spin-charge-family theory offer?



- There are **four** in the low energy regime, rather than **three**, coupled families of **quarks and leptons**. **Careful measurments of the mixing matrices will show this up.**
- **Quarks and leptons** manifest the **same symmetries of mass matrices**.
- The existence of **four families** explains the properties of **neutrinos**.
- The theory **predicts the intervals** for the masses of the fourth families, the more accurate are the measured properties of quarks and leptons, the narrower will be intervals.
- There are **several scalar fields** which will be observed at the LHC.



- The **dark matter** origin in the **fifth family**.
- There are more than so far observed vector gauge fields.
- There is no supersymmetric partners, at least not to the observed ones.

- From  $Tr(\Phi_{\mp}^{vl\dagger} \Phi_{\mp}^{vl}) = \frac{v^2}{2}$  we extract from the masses of gauge bosons one information about the vacuum expectation values of the scalar fields, their coupling constants and their masses.
- Mass matrices of quarks and leptons offer additional information about the scalar fields of the *spin-charge-family* theory.
- Measuring charged and neutral currents, decay rates of hadrons, the scalar fields productions in the fermion scattering events and their decay properties provides us with additional in formations.

# What are not yet solved problems in the spin-charge-family theory?

The spin-charge-family theory offers the **explanation for the assumptions of the standard model** and **several predictions**. Yet there are several **proofs** needed and **calculations to be made**.

- Although I see formally that  $SO(4) \times U(1)_{II}$  must break into  $SU(2)_I \times U(1)_I$  leading to the  **$SU(2)_{II}$  massive vector gauge fields and the massless weak  $SU(2)_I$  vector gauge field**, this must be **proven**.
- Although I see that the symmetry is conserved whatever diagram I look at to see whether or not the symmetry of mass matrices on the tree level is conserved in all orders in loop corrections, this is **not yet a proof**.

- Although we have seen that the **loop corrections** of all the contributions **manifest coherence**, this is **not yet a proof** that this coherence really leads to mass matrices, which manifest then the measured properties of quarks and leptons.
- Also the **properties of scalar fields** wait to be **formally derived**.
- Additional numerical evaluation of the mass matrices of the four families of quarks and leptons are needed.
- Carefull study of predictions of the properties of scalar fields, possibly measured at the LHC, are needed.
- And many additional problems to be solved and measurements to be predicted.

## Prediction for the LHC

- **LHC will confirm the existence of several scalar fields.**  
Yukawa couplings by themselves guarantee that there are several!!
- **LHC will confirm the fourth family.**
- **NO desert in the future measurements.**