

Семинар
НИИЯФ МГУ
23 июня 2022



Нейтриный телескоп Baikal-GVD: состояние работ и последние результаты

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(ИЯИ РАН)

* GVD = Gigaton Volume Detector

Содержание доклада

- 1) Нейтринная астрономия высоких энергий
- 2) Установка Baikal-GVD: устройство и состояние работ
- 3) Оценки чувствительности эксперимента и полученные результаты

Часть I

Нейтринная астрономия высоких энергий

Neutrino as astrophysical messenger

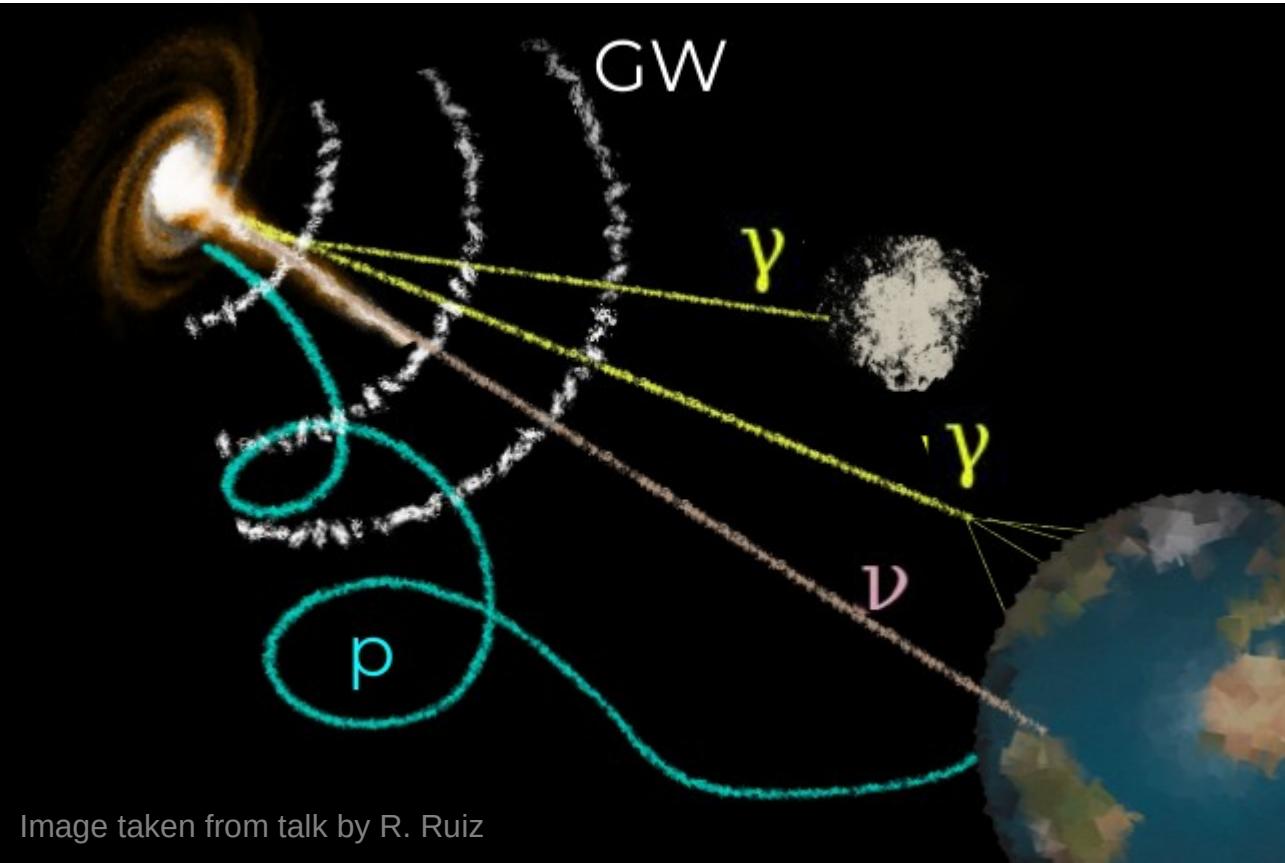
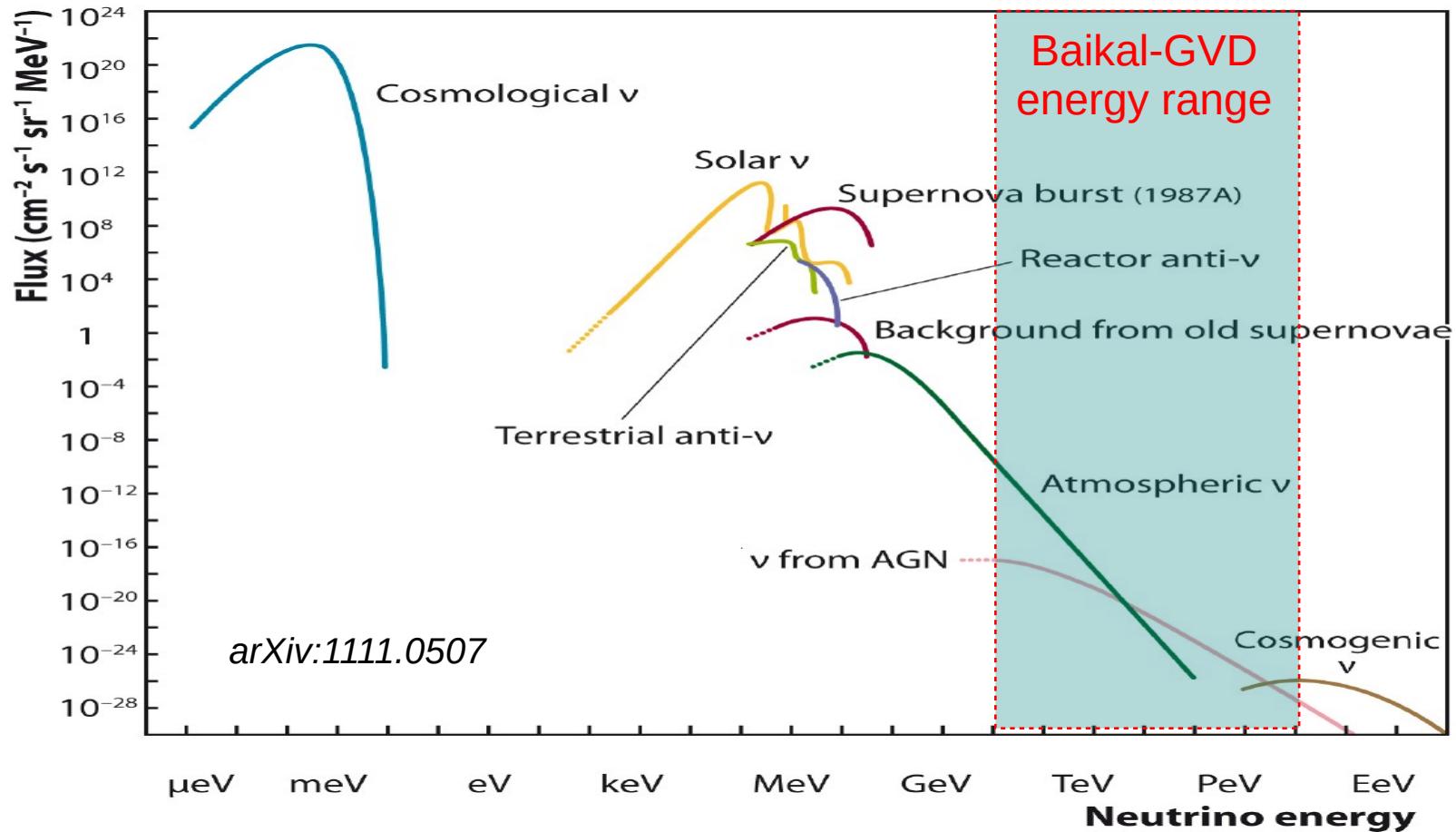


Image taken from talk by R. Ruiz

- Can escape from dense environments
- Travels unimpeded through gas and dust
- Does not interact with CMB and infrared background
- Stable (no decay)
- Not affected by magnetic fields
- Arrival direction points to the source
- High-energy neutrinos trace production and acceleration sites of cosmic rays

Where we are on the energy scale



How to make high energy neutrino

- 1) Accelerate protons
- 2) Have them interact with medium or radiation

In photon-reach environments: $p\gamma \rightarrow \pi$
In proton-reach environments : $p p \rightarrow \pi$

- 3) Decay pions

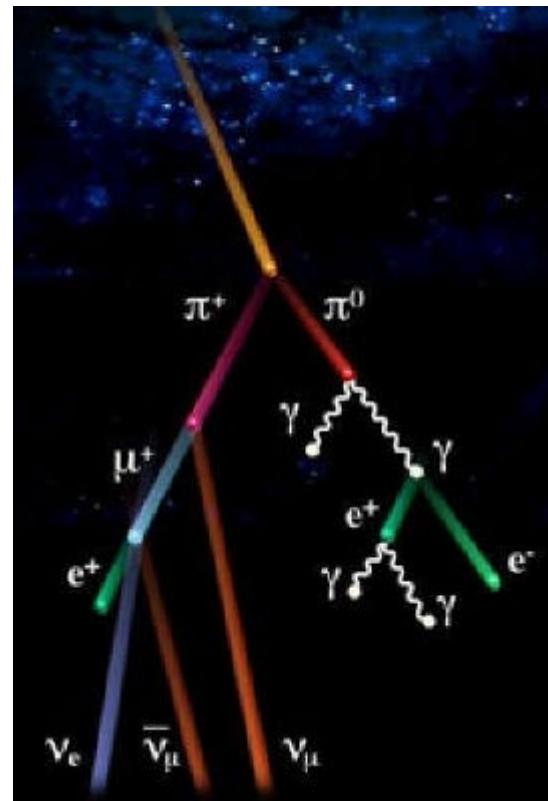
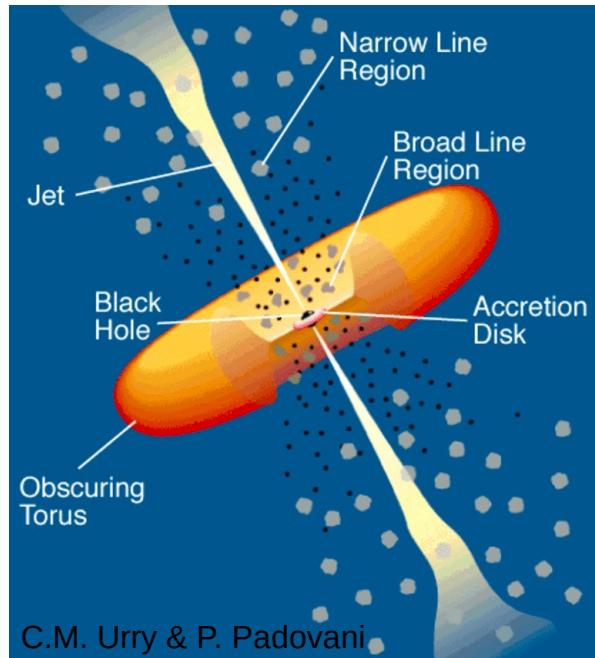
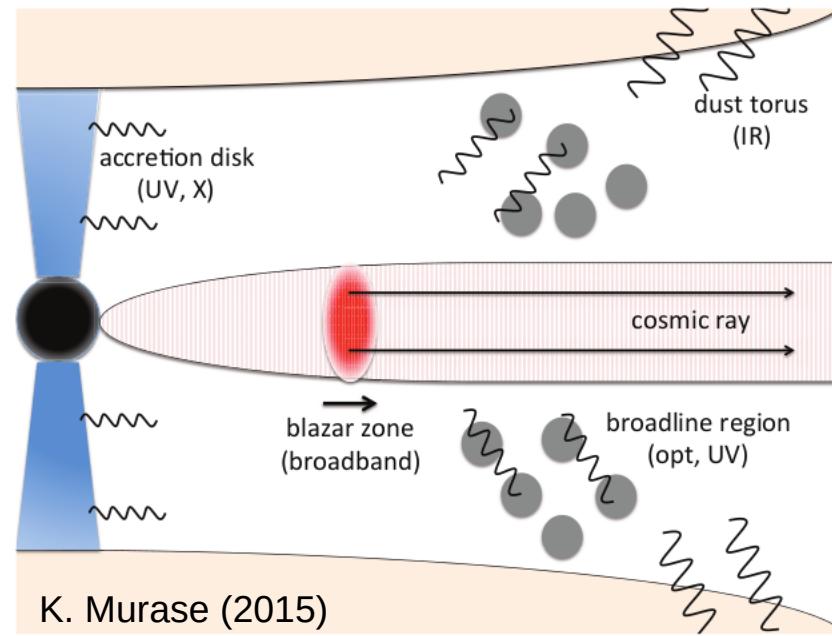


Figure from Reiner et al, PRD (2008)

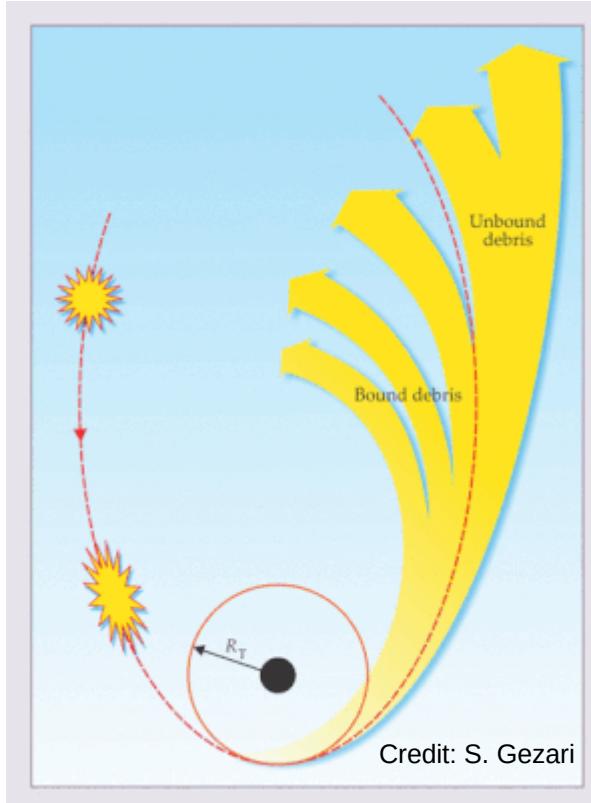
Potential neutrino sources: Active Galactic Nuclei



Example model



Tidal Disruption Events



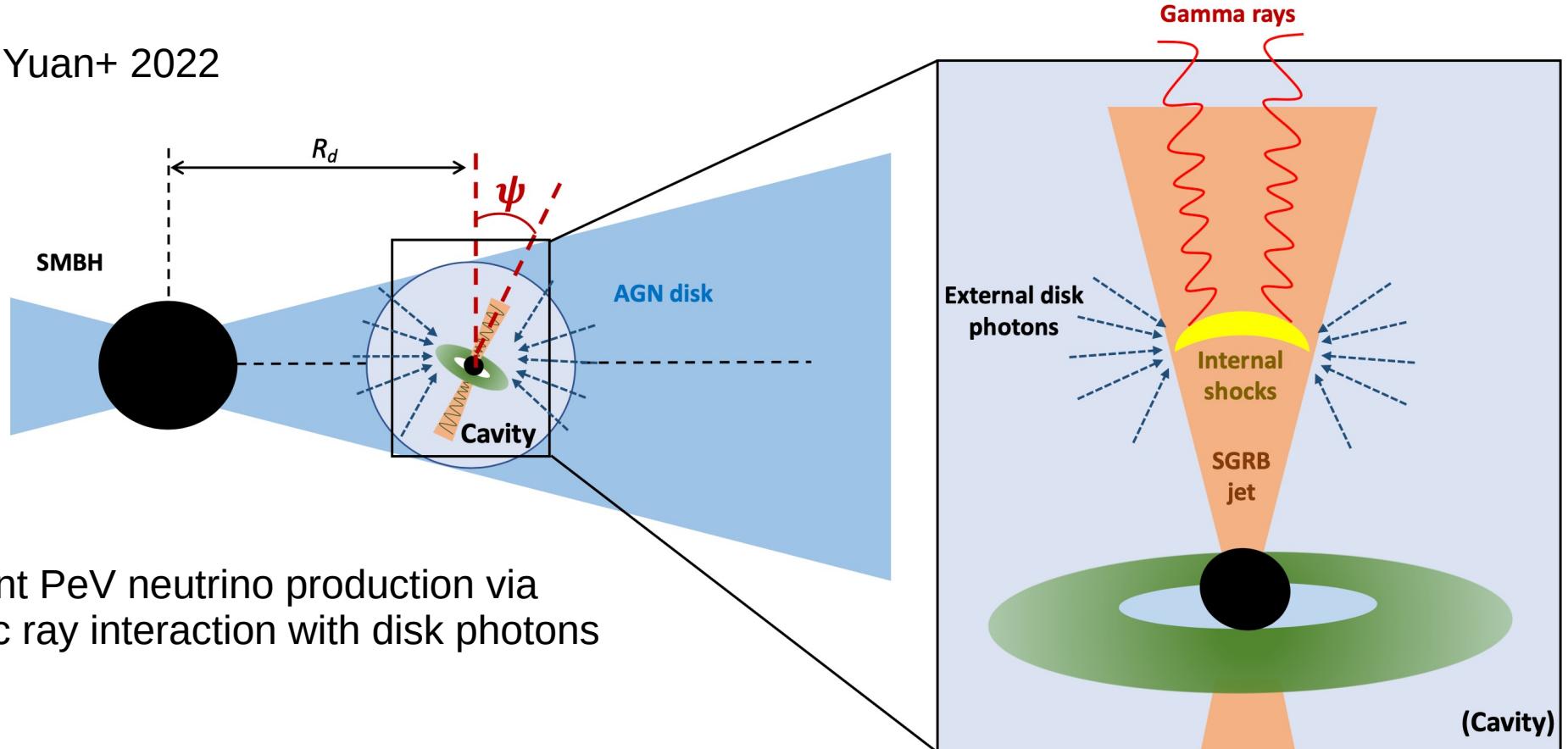
Star disrupted
in gravitational field
of supermassive black hole

R = Roche limit

Also see *R. Stein et al.,
Nat. Astron. 5, 510 (2021)*

Neutron star mergers in AGN disks

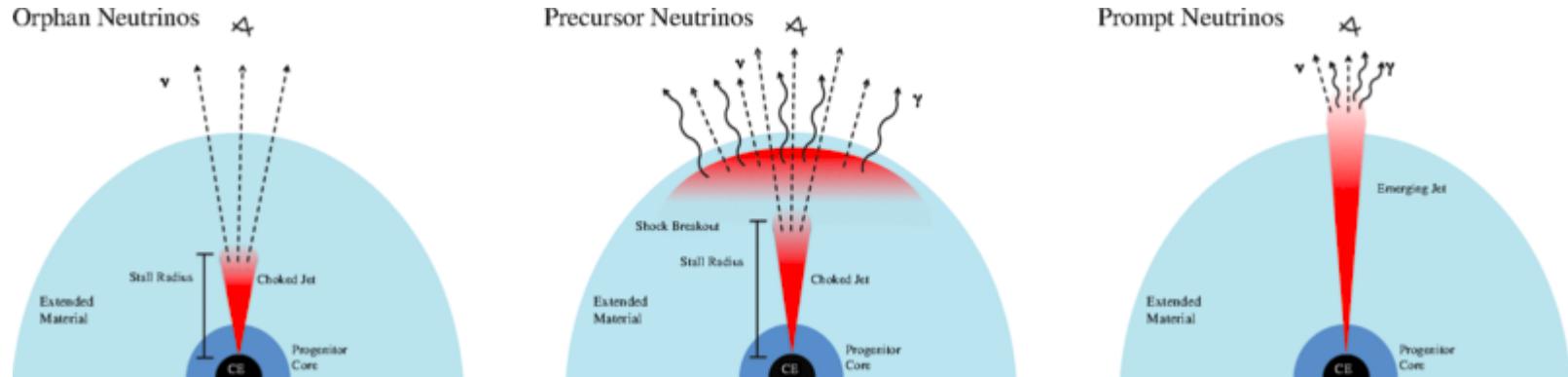
Yuan+ 2022



Efficient PeV neutrino production via
cosmic ray interaction with disk photons

Also possible with black hole mergers (Kimura et al., 2021)

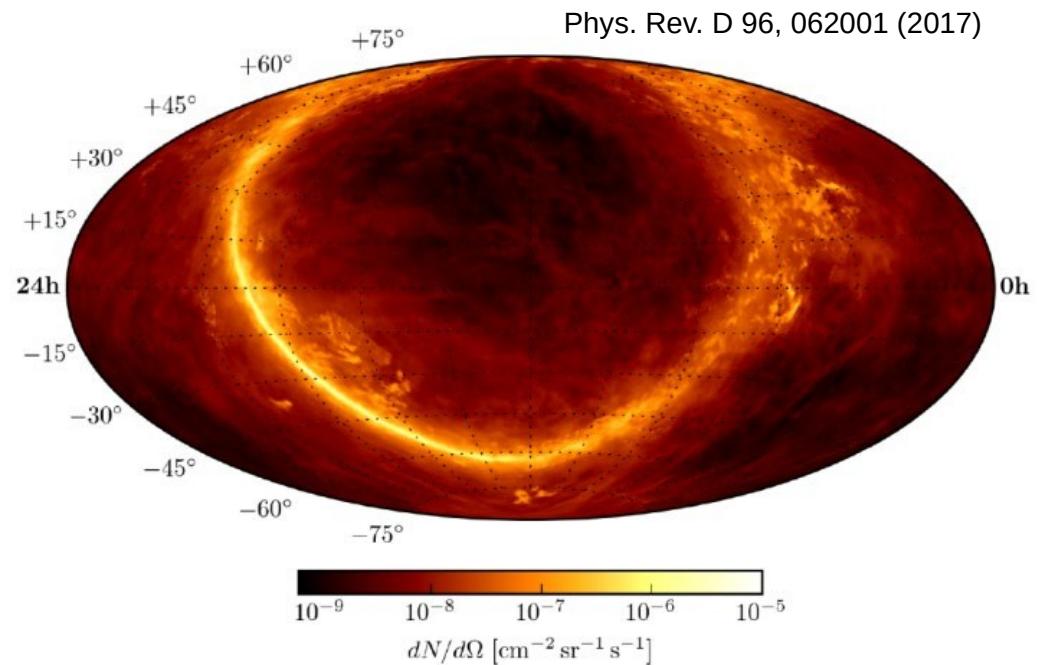
GRBs, choked jets (Supernovae)



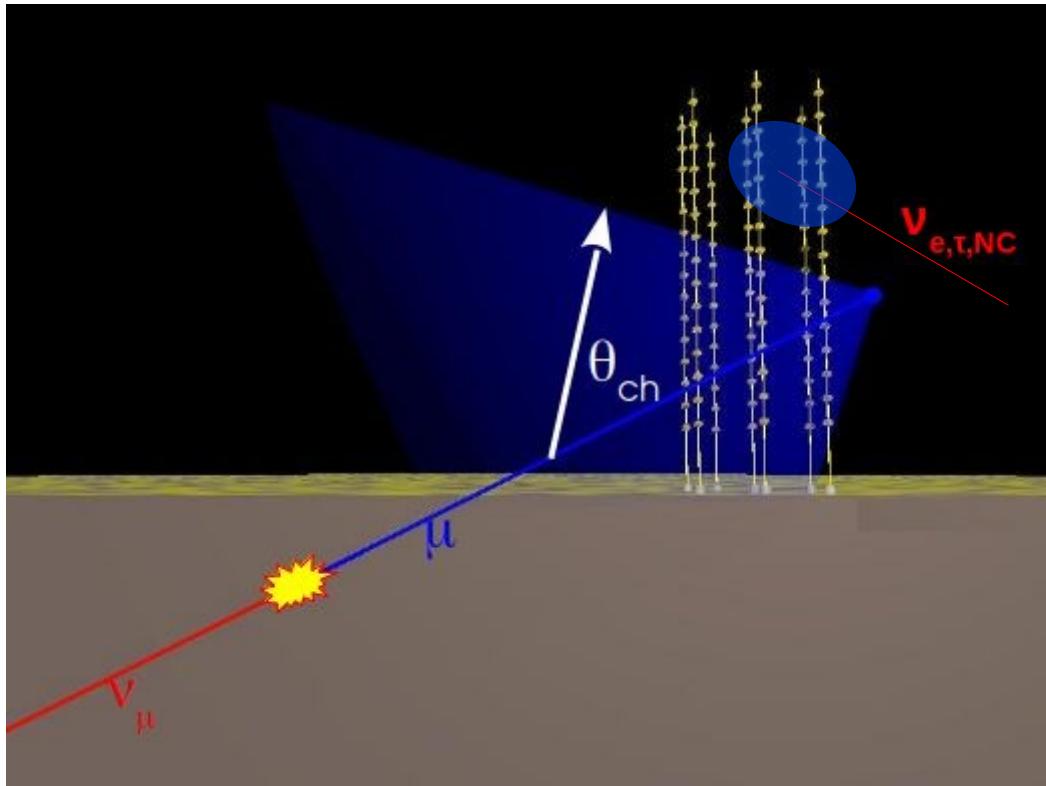
N. Senno, K. Murase, and P. Mészáros (2016)

Possible Galactic neutrino sources

- Galactic Ridge / Galactic diffuse
- Supernova Remnants
- Pulsar Wind Nebulae?
- Microquasars
- Binaries
- Novae
- Galactic center



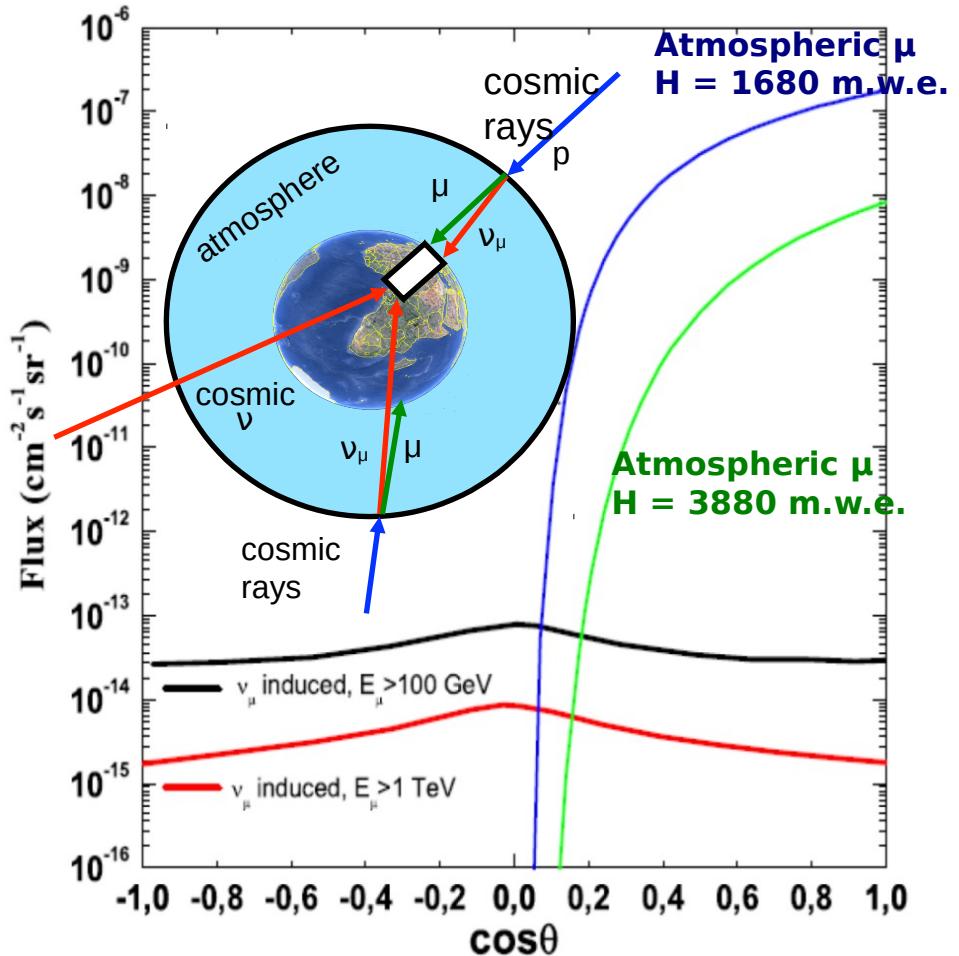
Neutrino telescope : how it works



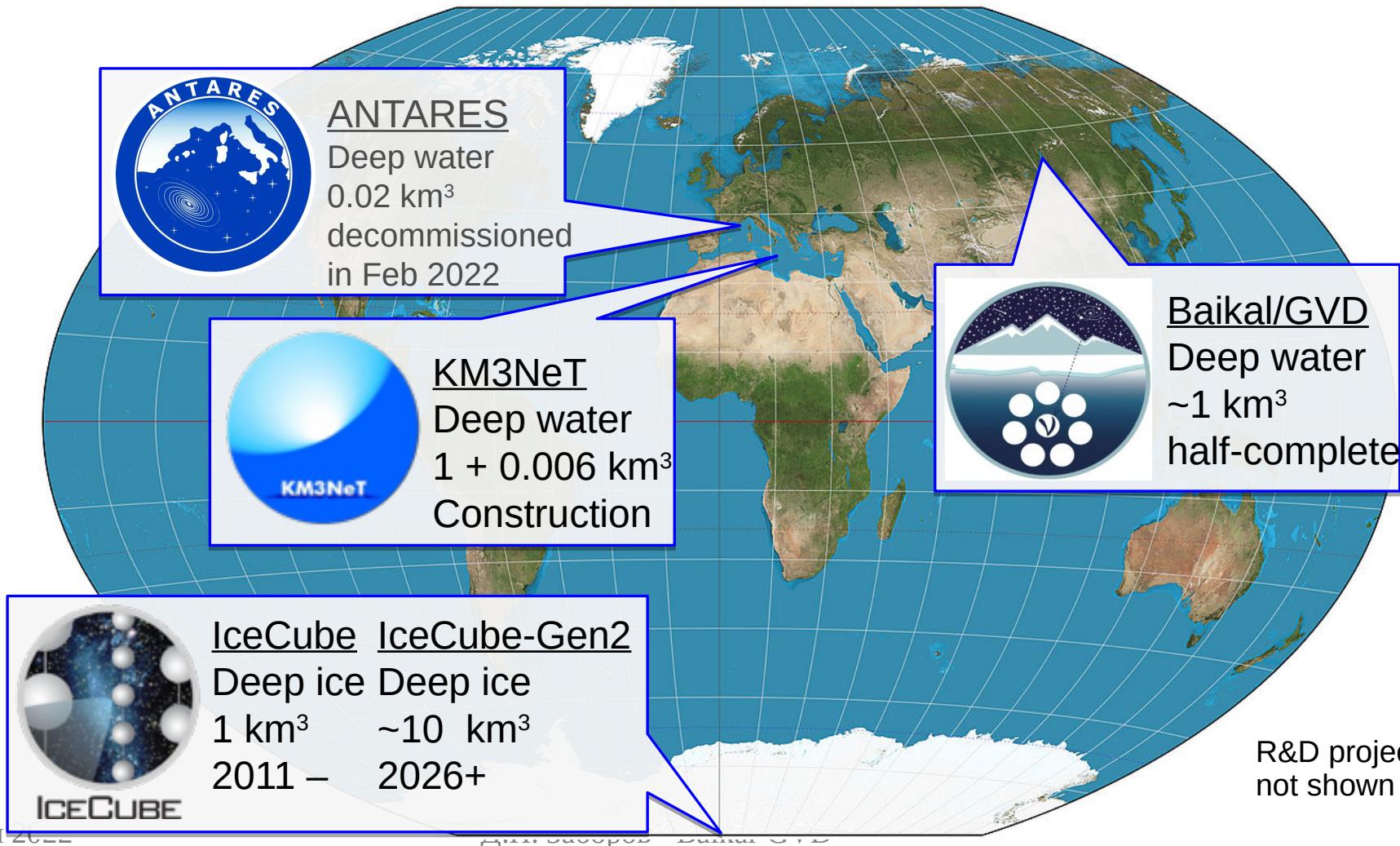
- Large arrays of PMTs in water or ice
- Cherenkov light detected by PMTs
- “Tracks”: ν_μ CC
- “Cascades”: ν_e & ν_τ CC + NC
- Direction reconstructed from hit positions and times
- Energy reconstructed from hit charges

Backgrounds

- Atmospheric neutrinos
 - All-sky, soft spectrum
 - For downgoing events, atmospheric muons can be used as veto (at very high energy)
- Atmospheric muons
 - Downgoing only (Earth acts as filter)
- Environmental background light: natural radioactivity (^{40}K), bioluminescence, chemiluminescence
 - Limits low energy sensitivity



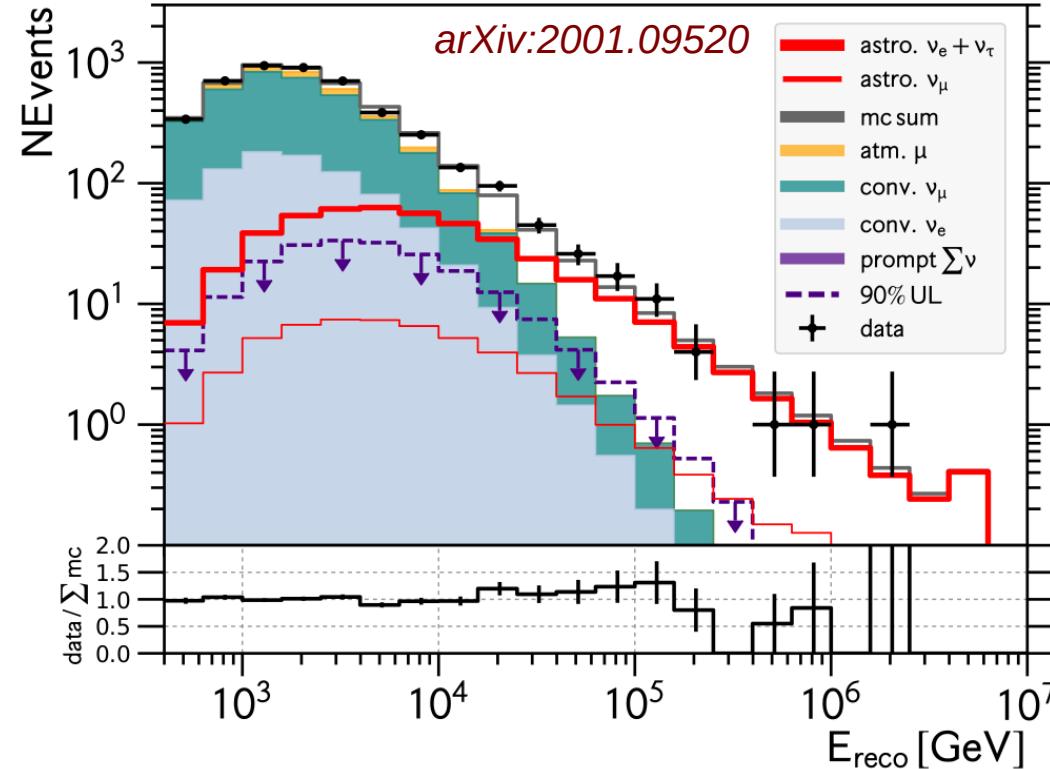
Neutrino telescope world map 2022



Diffuse neutrino flux

IceCube cascades

arXiv:2001.09520



Science 342 (2013)

[4.1 σ]

PRL 113:101101 (2014)

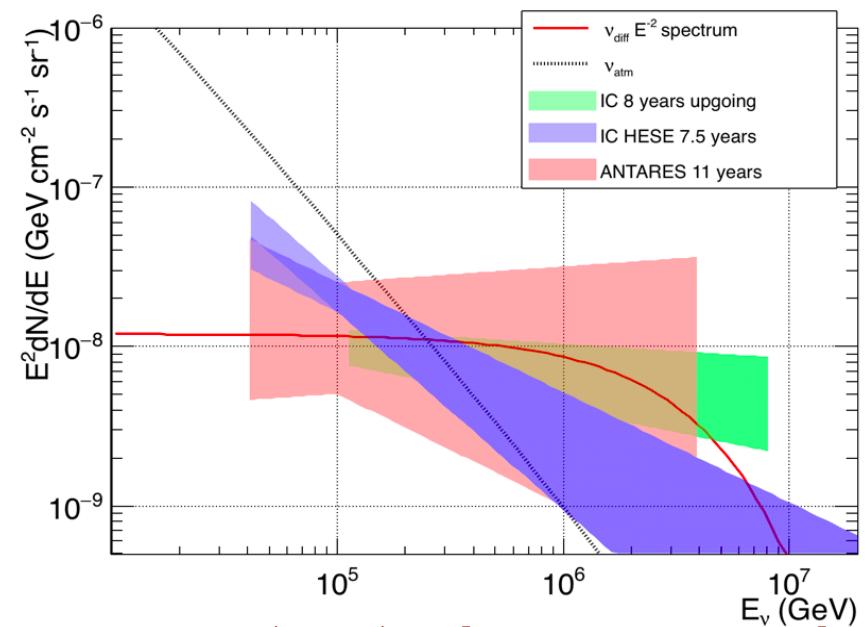
[5.9 σ]

PRL 125:121104 (2020)

[~10 σ]

23 июня 2022

While the existence of a diffuse neutrino flux is firmly established, its origin remains unknown



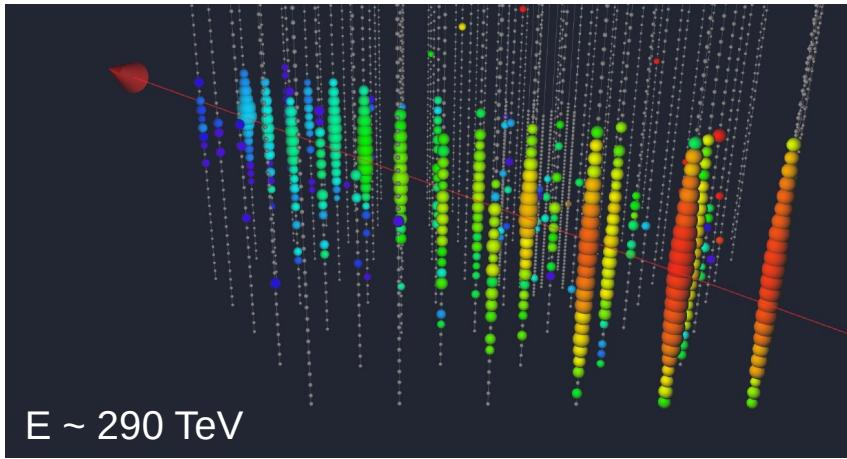
ApJ 853 (2018) L7 [arXiv:1711.07212]

D. Samtleben, Neutrino 2020

15 of 51

Д.Н. Заборов - Baikal-GVD

TXS 0506+056

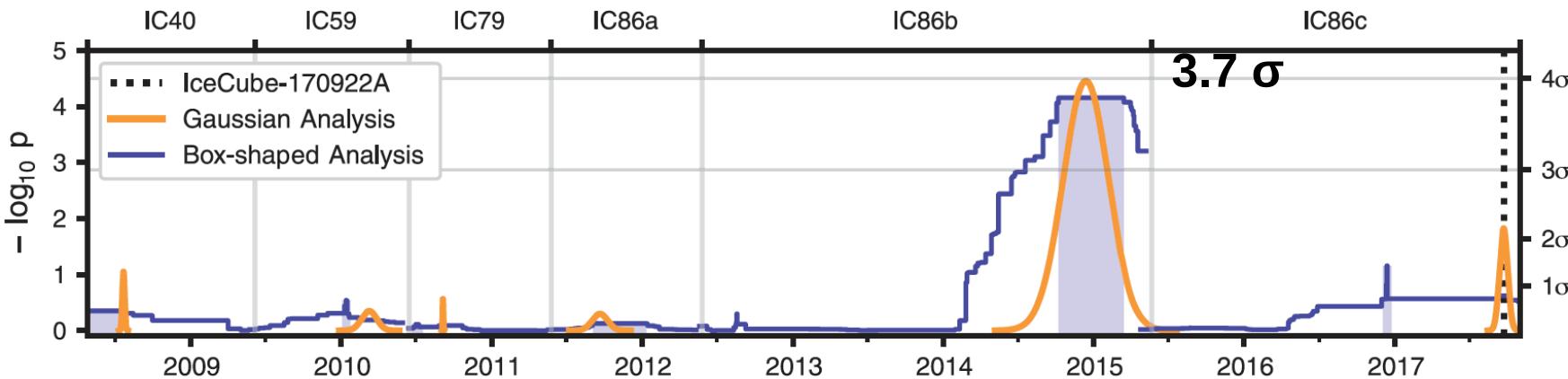


High-energy IceCube ν coincident with a γ-ray flare from the blazar TXS 0506+056 (Sep 22, 2017)

Science 361, 147–151 (2018)

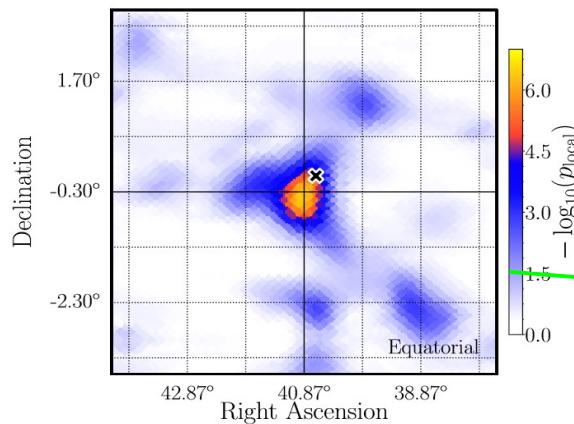
Another, neutrino-only flare found in earlier IceCube data

A. Albert et al., ApJL 863, L30 (2018)

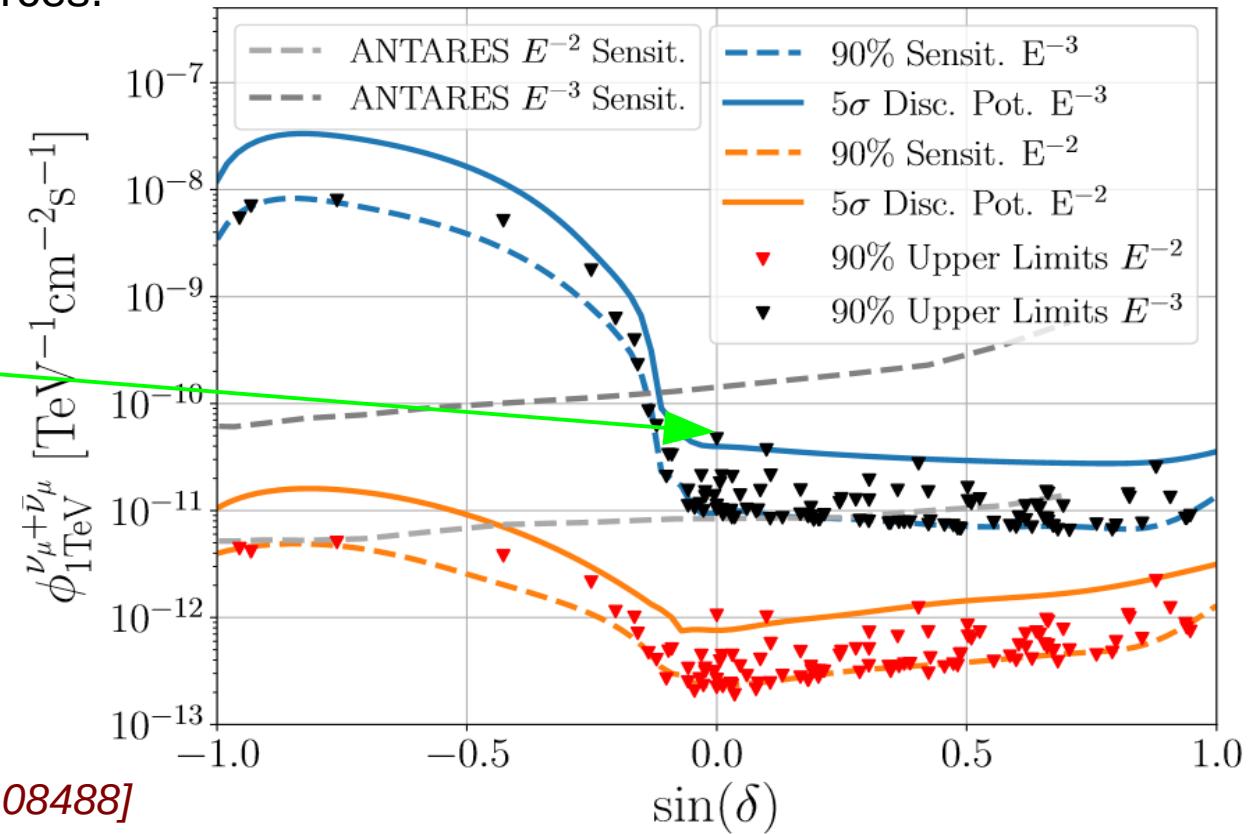


Point-source searches

Some evidence for non-uniform skymap in 10 years of IceCube data (3.3σ).
Mostly resulting from 4 extragalactic source candidates.
No indications for galactic sources.



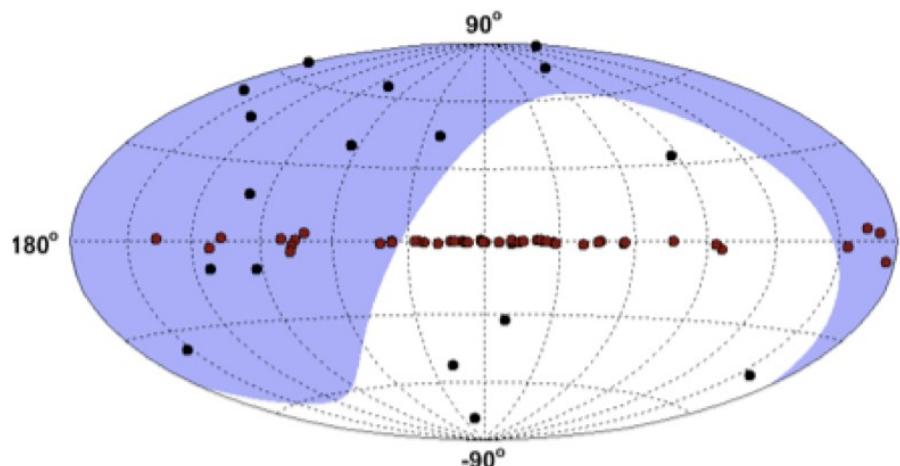
Strongest excess
(2.6σ post trial) close to
galaxy NGC 1068 (cross)



Sky visibility with upgoing tracks

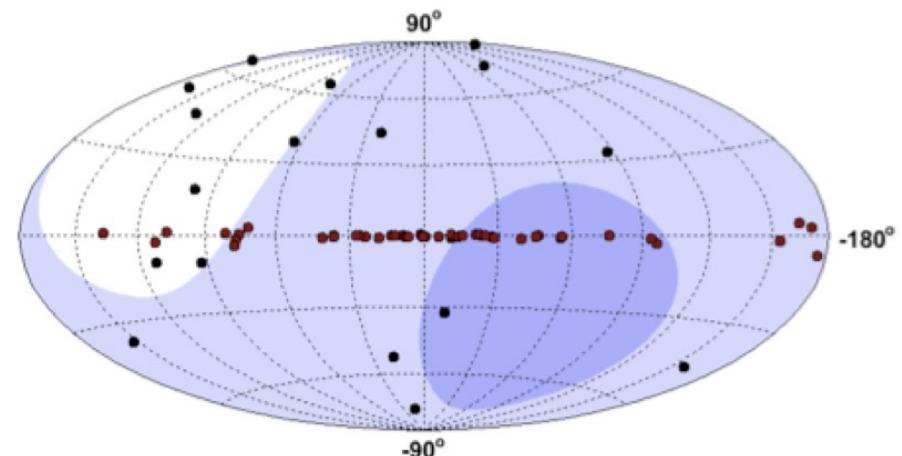
South Pole (IceCube)

0% 100%



Northern hemisphere
(Mediterranean)

< 25% 25% – 75% > 75%



Complementary sky coverage

Galactic center better viewed from Northern hemisphere (through the Earth)

Часть II

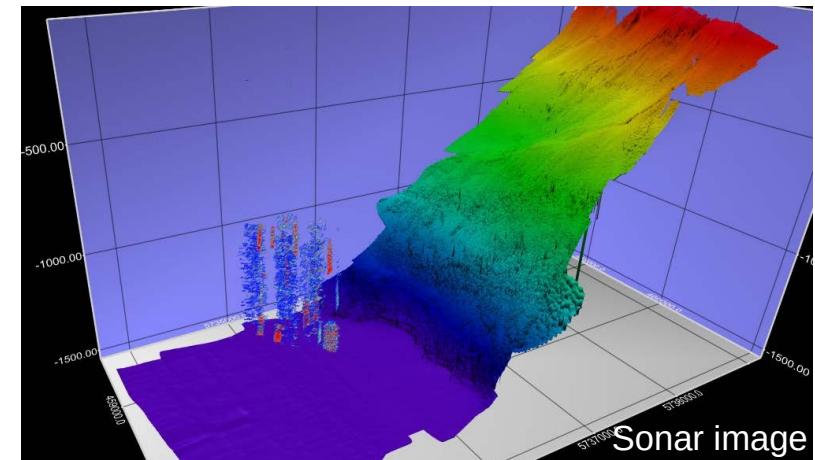
Baikal-GVD

Baikal-GVD site

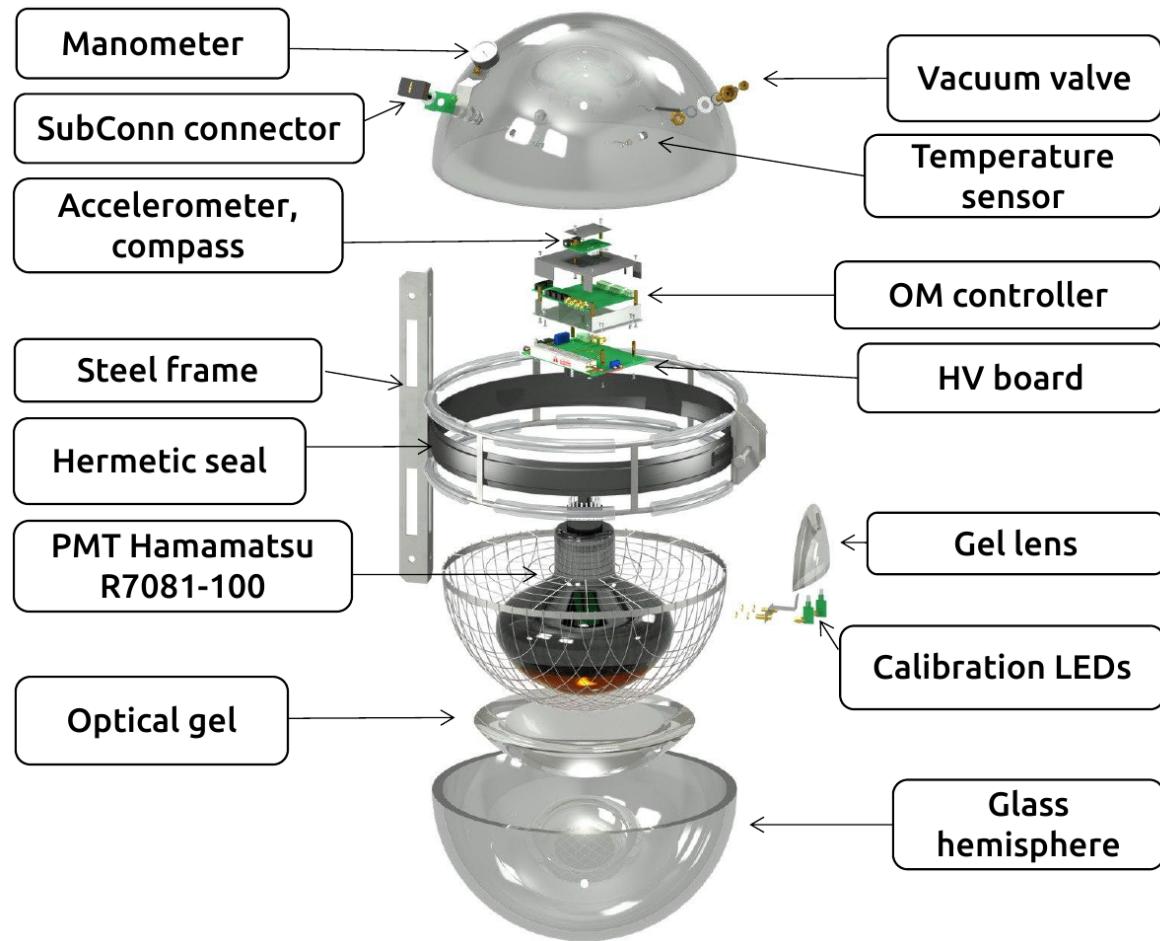


- High water transparency
 - ✓ Absorption length: 22 m
 - ✓ Scattering length: 30 – 50 m ($L_{\text{eff}} \approx 480$ m)
- Moderately low optical background: 15–40 kHz (PMT R7081-100 Ø10")

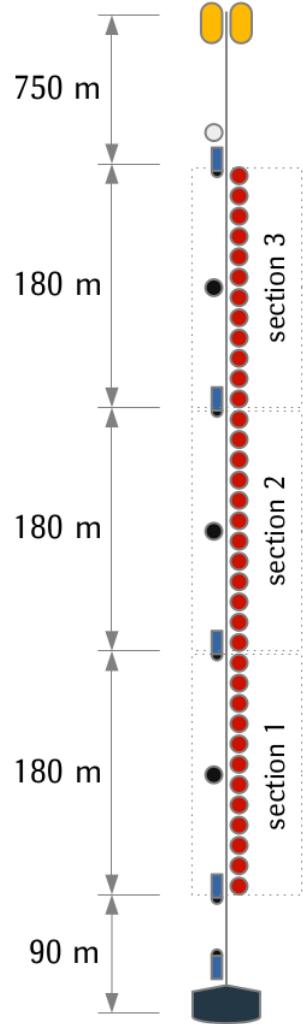
- 51° 46' N 104° 24' E
- Southern basin of Lake Baikal
- ~ 4 km away from shore
- Flat area at depths 1366 – 1367 m
- Stable ice cover for 6–8 weeks in February – April: detector deployment & maintenance



Baikal-GVD optical module



GVD string

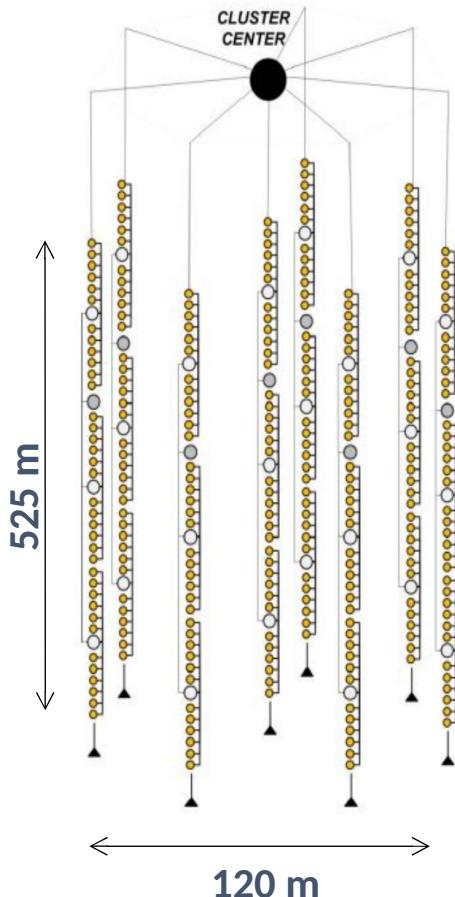


- **36 OMs**, 15 m spacing, all PMTs look downward
- **4 acoustic modems (AM)** of the positioning system
- **3 section modules**, each serving 12 OMs (12-channel ADC, 200 MHz sampling; waveform measurement + trigger logic, events forming, data filtration)
- **1 string module** (a communication hub)
- Depths from 750 m to 1275 m



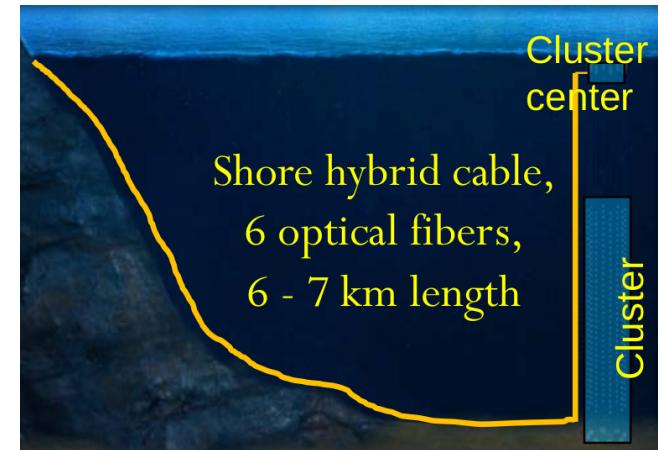
GVD cluster

Cluster:
8 strings



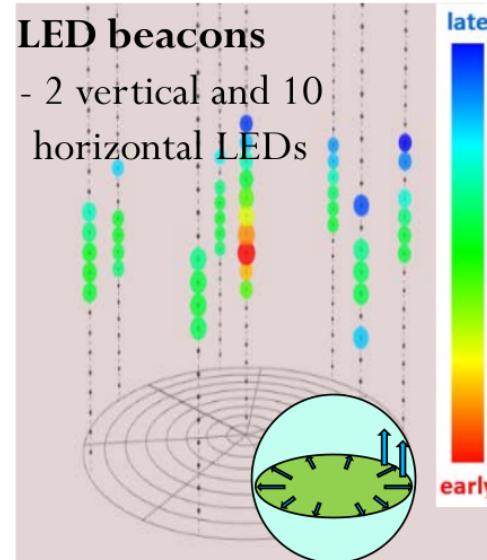
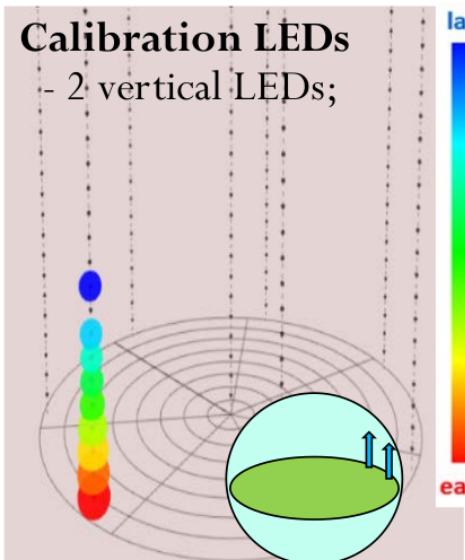
Cluster

- 8 strings (288 OM)s)
- 60 m step between strings
- Central electronics (power, trigger, data transmission) located at 30 m depth
- Hardware trigger: 4.5 p.e. + 1.5 p.e. on adjacent OM's in 100 ns window
- Inter-section synchronisation by common trigger (~ 2 ns accuracy)
- Internal network: shDSL Ethernet extenders 5.7 Mbit
- Connection to shore: Ethernet / optic fiber

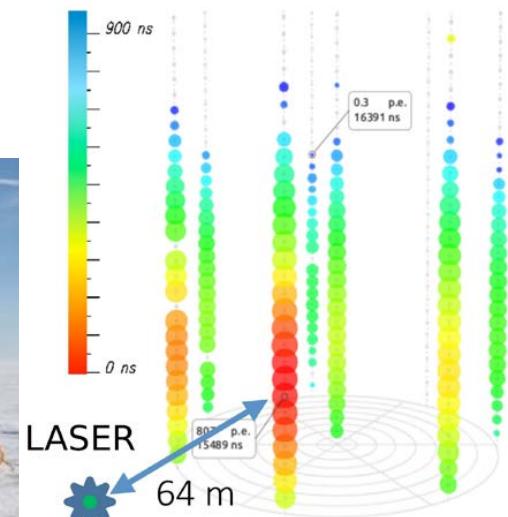


Calibration devices

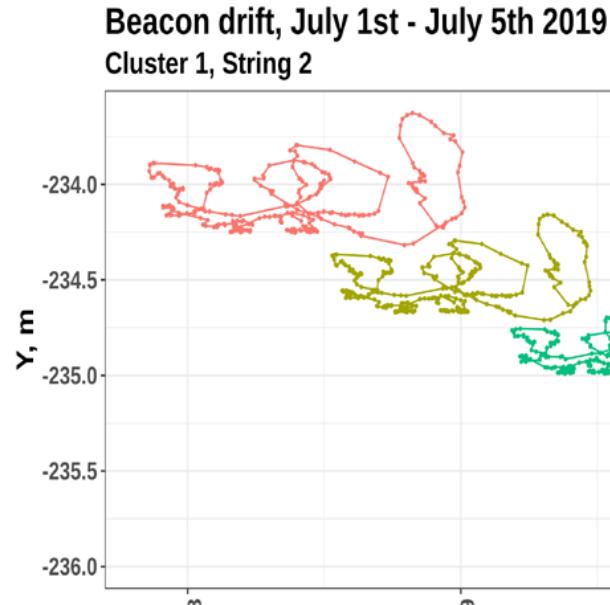
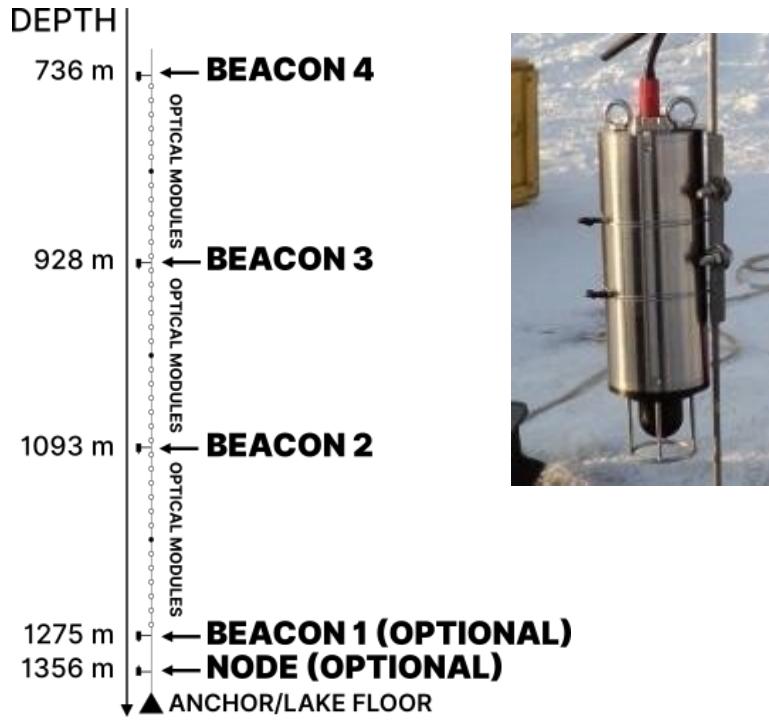
- Section calibration: 2 LEDs in each OM, 470 nm, $1 - 10^8$ ph., 5 ns
- String calibration: LED beacons in 12 OMs of the cluster
- Cluster calibration: 2 lasers per station, 532 nm, $10^{12} - 10^{15}$ ph., 1 ns



Calibration accuracy ~2 ns



Acoustic positioning



Depth ■ 736 m ■ 826 m ■ 928 m ■ 1093 m ■ 1274 m

OM drift can reach tens of meters, depending on season and elevation
String geometry monitored with acoustic modems (4 AMs per string)
OM coordinates are obtained by interpolating AM coordinates, accuracy ~ 20 cm

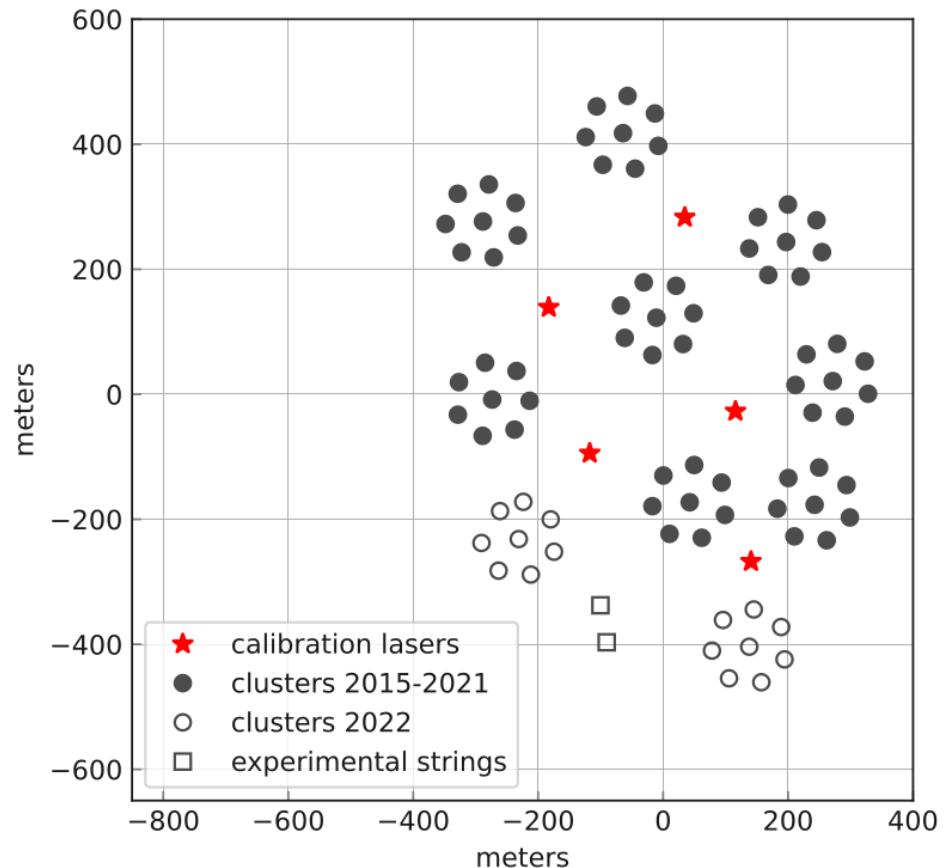
Deployment



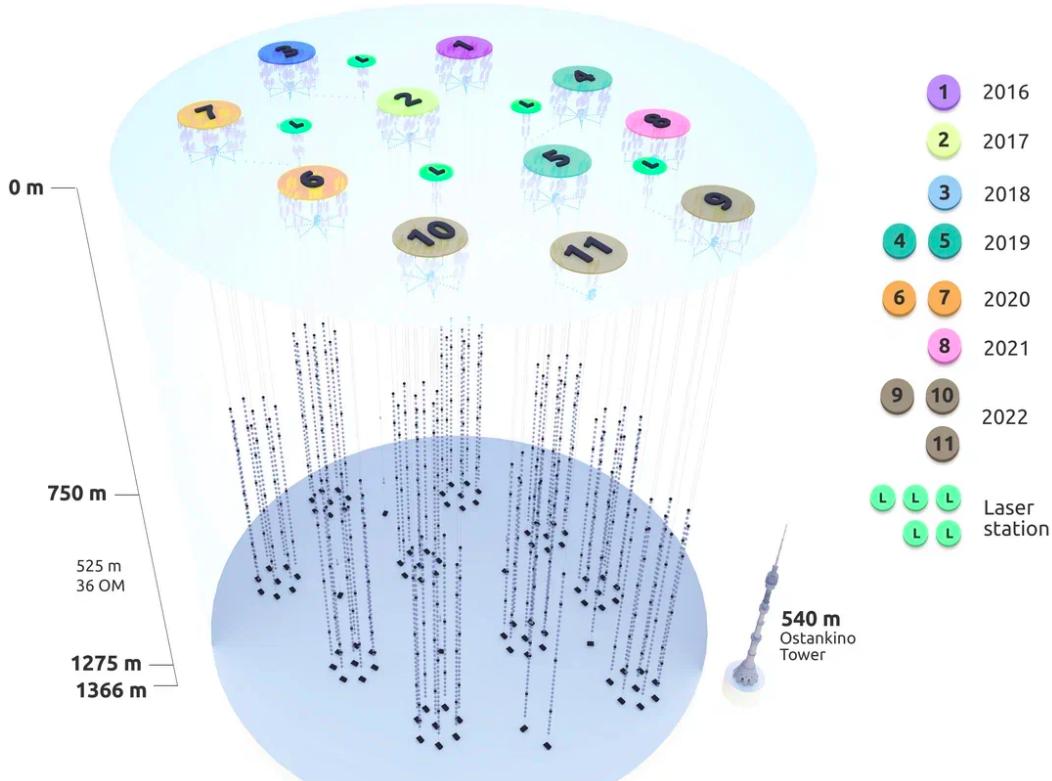
Экспедиция 2022

Установлено:

- два новых кластера (16 гирлянд)
- 2 экспериментальные гирлянды на оптоволоконной технологии связи (активно 48 ОМ)
- 1 дополнительная межклUSTERная гирлянда (36 ОМ + лазер)
- 1 отдельная лазерная станция
- Проведён плановый ремонт ранее установленного оборудования



Baikal-GVD construction status 2022 and schedule



10 clusters + 1 special string (laser+36 OM)
+ 2 experimental strings + 4 laser stations

Deployment schedule

Year	Number of clusters	Number of strings	Number of OMs
2016	1	8	288
2017	2	16	576
2018	3	24	864
2019	5	40	1440
2020	7	56	2016
2021	8	64	2304
2022	10	80 + 3	2880 + 84
2023	12	96	3456
2024	14	112	4032

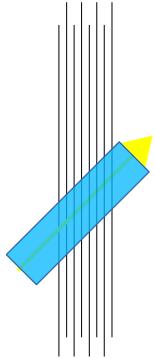
Effective volume 2022: 0.40 km³ (cascades 100 TeV)

Часть III

Характеристики детектора Baikal-GVD и первые результаты

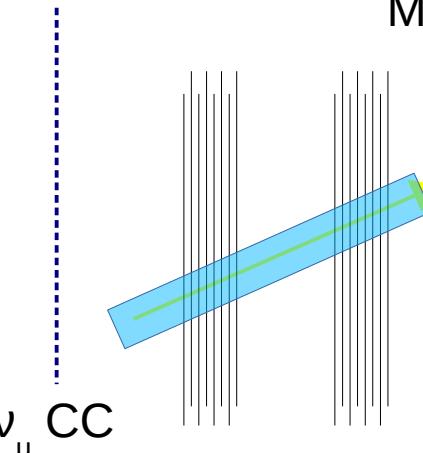
Event types

Single-cluster tracks



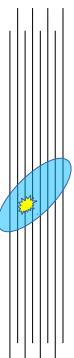
- ✓ Low energy threshold
- ✓ Optimal sensitivity to nearly vertical tracks
- ✓ 90% of recorded track events

Multi-cluster tracks



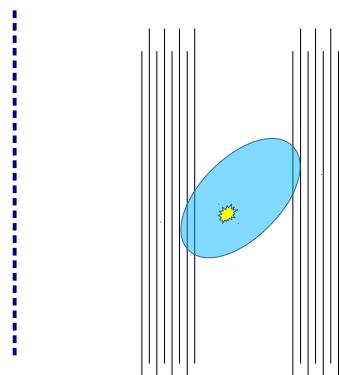
- ✓ Moderately low energy threshold
- ✓ Optimal sensitivity to inclined tracks
- ✓ 10% of recorded track events

Single-cluster cascades



- ✓ High energy threshold
- ✓ Good energy resolution
- ✓ Relatively rare events

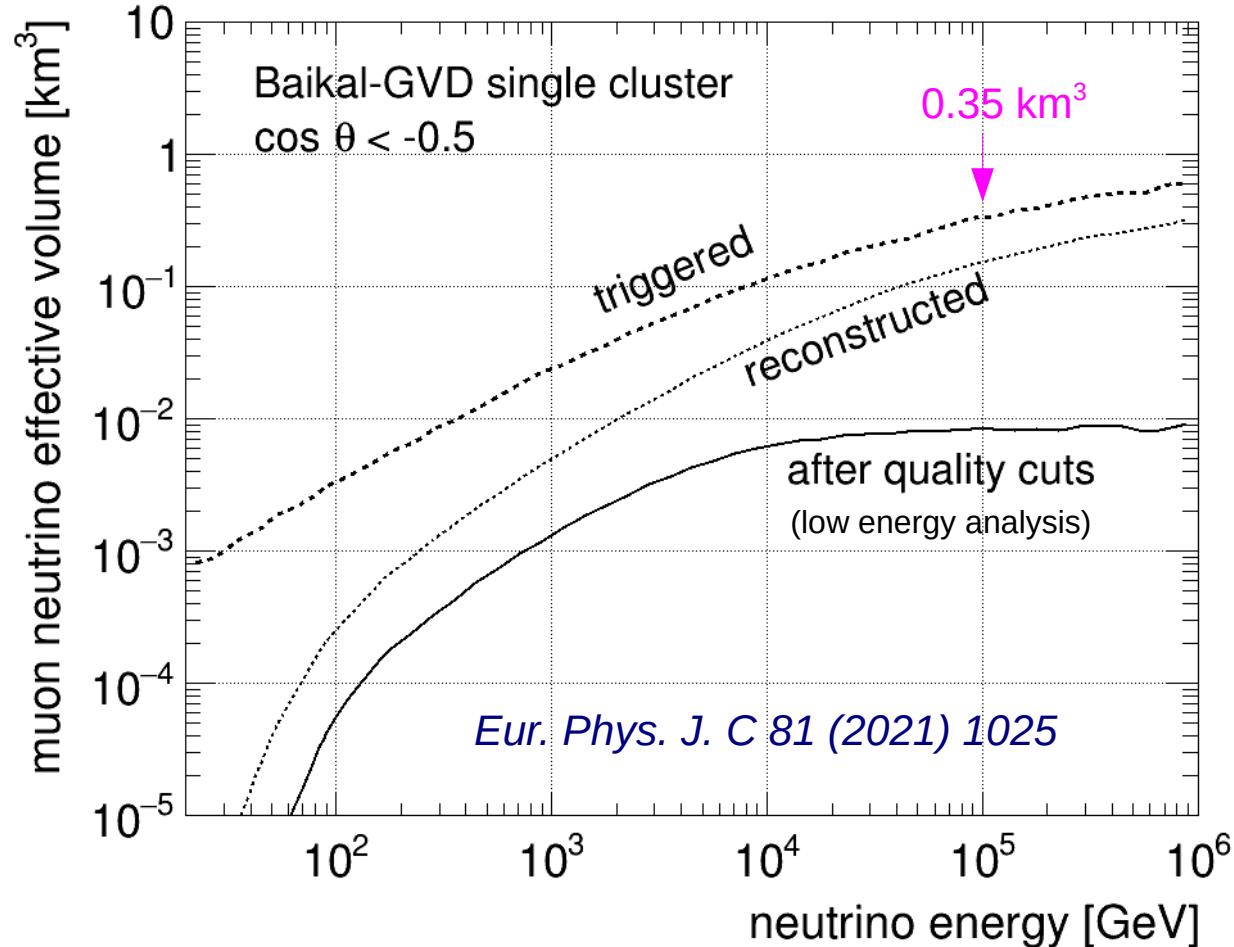
NC, ν_e , ν_τ CC



Multi-cluster cascades

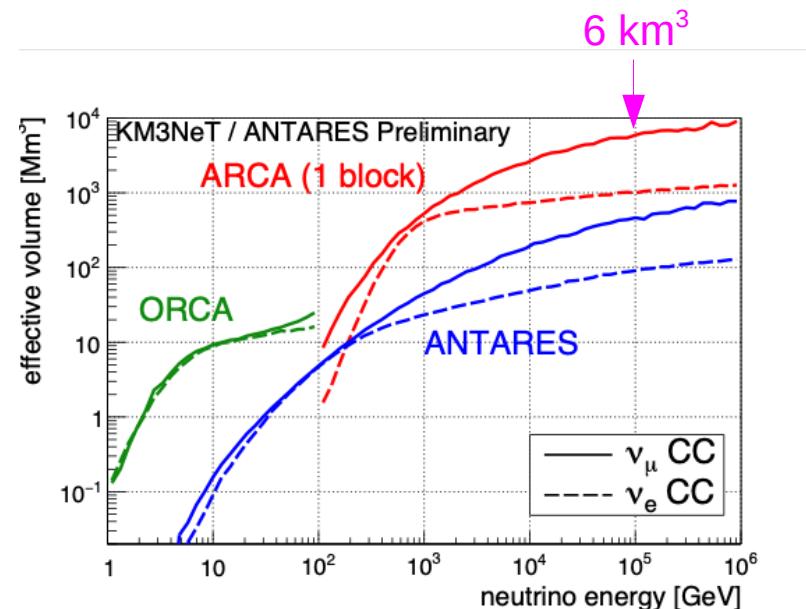
- ✓ Very high energy threshold
- ✓ Excellent energy resolution
- ✓ Very rare events

Neutrino effective volume for tracks (one GVD cluster)



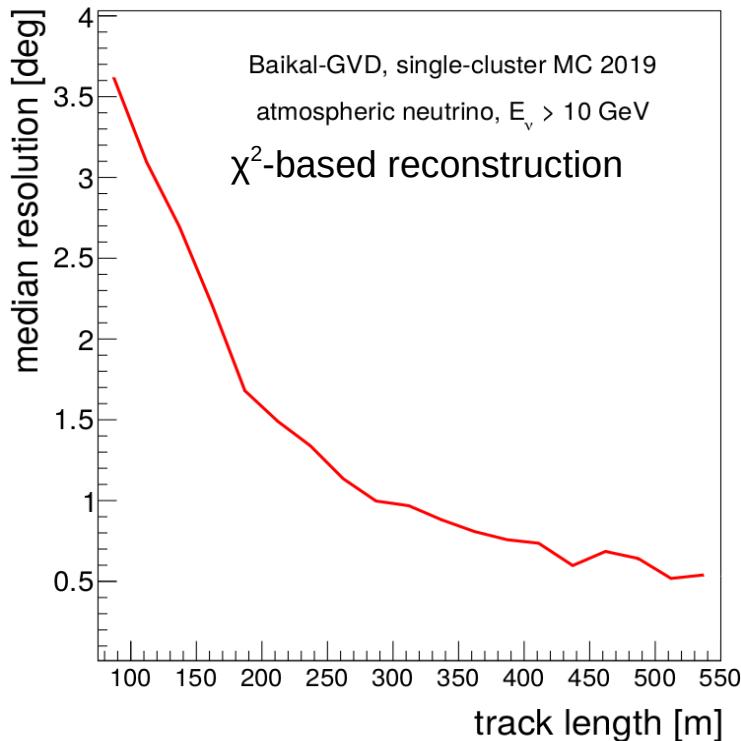
Energy threshold ~ 200 GeV
(higher than in ANTARES)

Fully efficient at $E > 100$ TeV



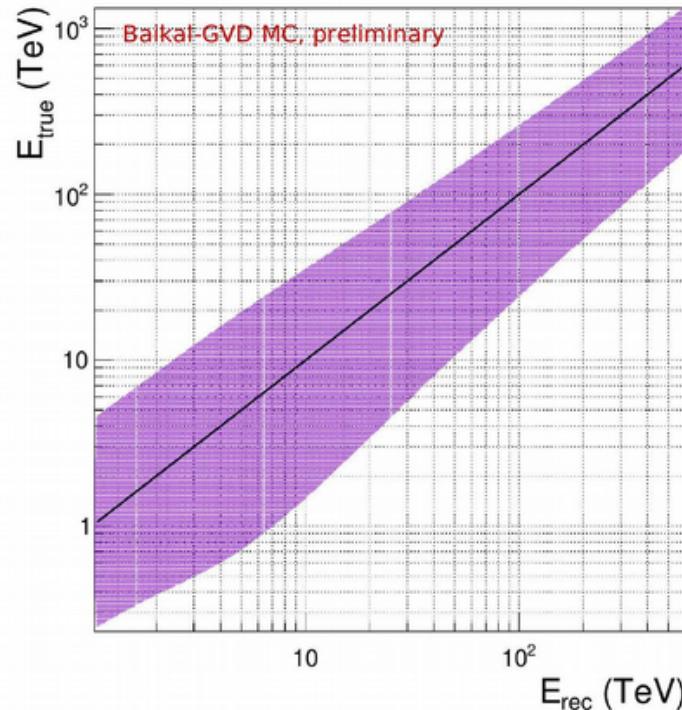
Expected performance for tracks

Angular resolution



Improvements expected from likelihood-based reconstruction (under development)

Energy reconstruction

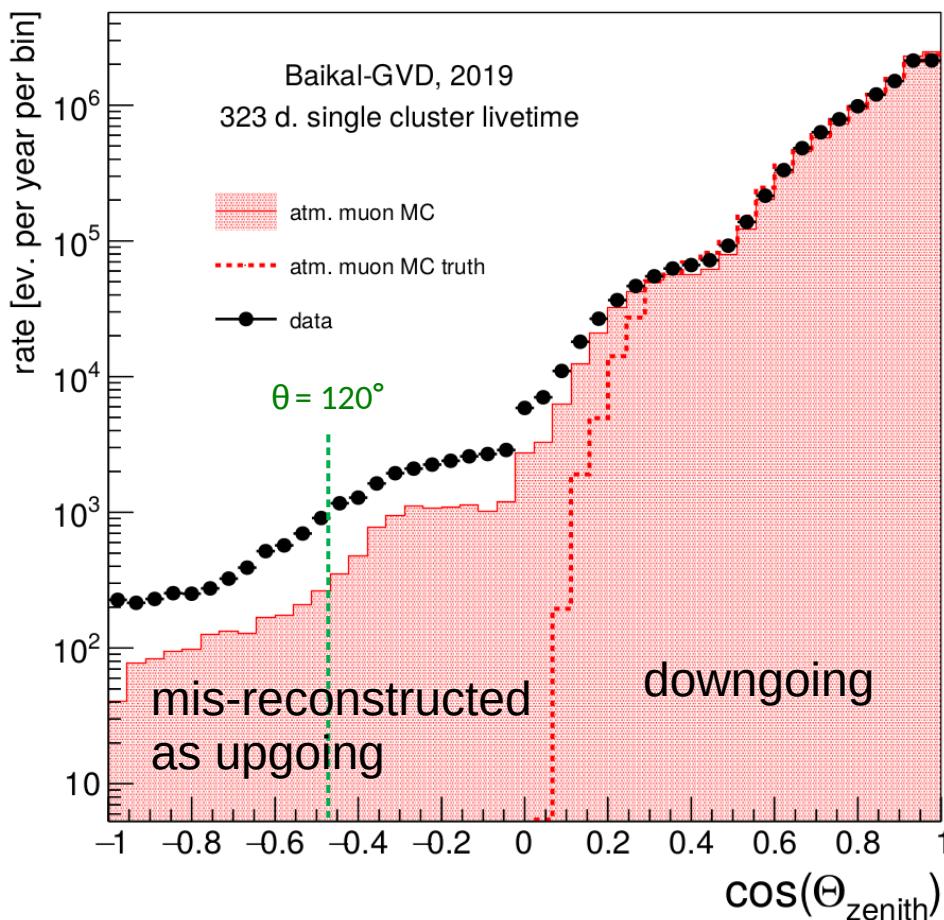


energy resolution ~ factor 3 at $E \sim 100$ TeV
(±34% containment band)

G. Safronov @ ICRC 2021

Atmospheric muons with Baikal-GVD (single cluster)

Before quality cuts



Data taken between Apr 1 and Jun 30, 2019 with 5 clusters

~ 9 800 000 events reconstructed with at least 8 hits on at least 2 strings

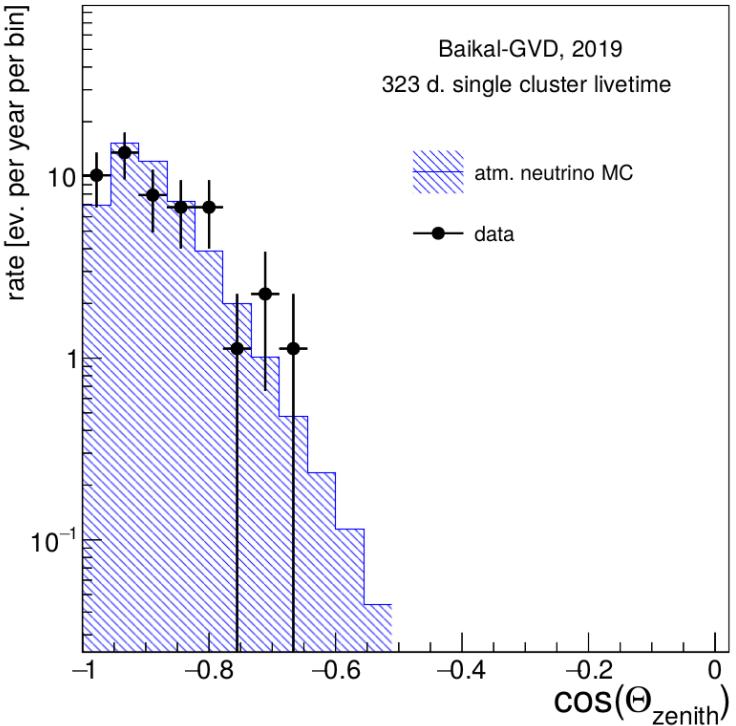
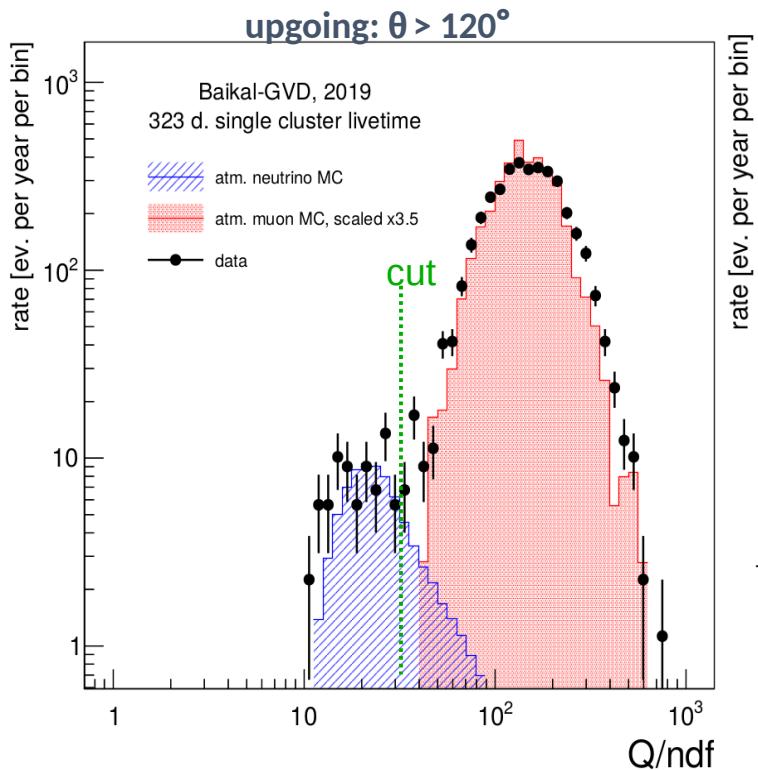
Good agreement for $\cos(\text{zenith}) > 0.2$

MC underpredicts the rate of misreconstructed events in the upgoing region by a factor of 3.5 (under study)

NB: most of these events are muon bundles (average multiplicity ~ 10)

Eur. Phys. J. C 81 (2021) 1025

Atmospheric neutrinos with Baikal-GVD (single cluster)



MC expected: 43.6

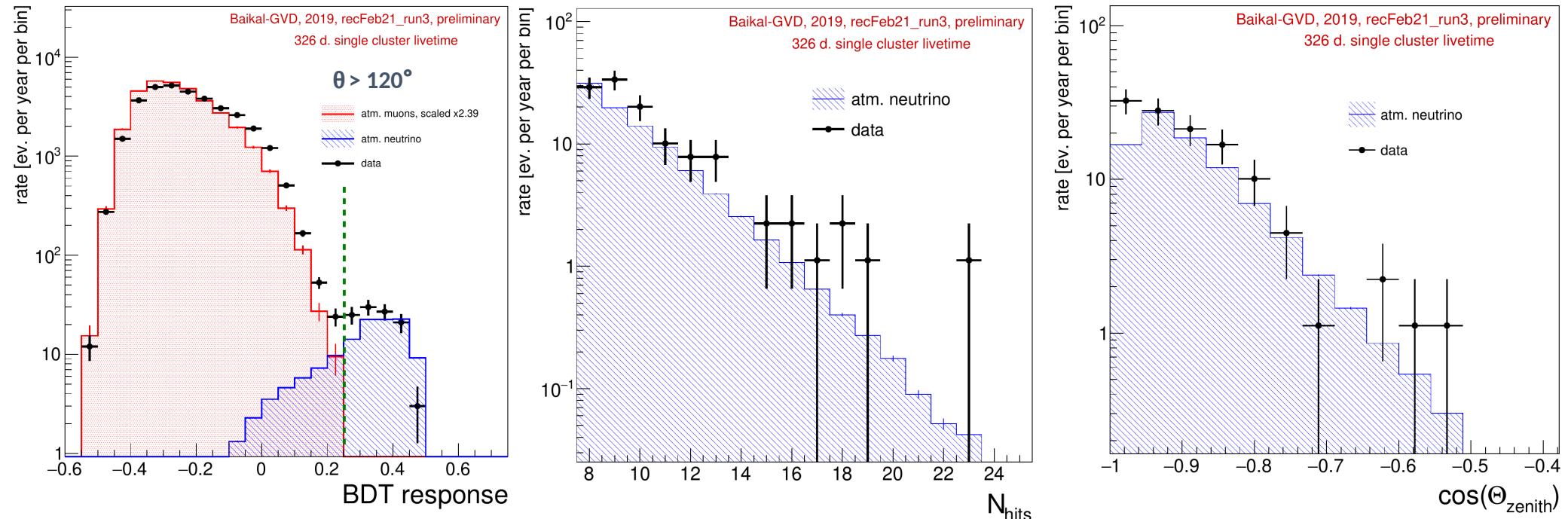
- atm. neutrino : 43.6
- atm. muons: $< \sim 1$

Observed events: 44

Median energy of this sample ≈ 500 GeV

Eur. Phys. J. C 81 (2021) 1025

Atmospheric neutrinos : improved analysis



Hit finder: efficient hit-finding algorithm [PoS-ICRC2021-1063]

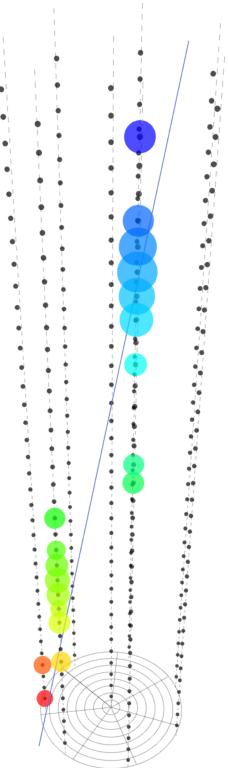
Track fit: $\chi^2(t)$ - based fitter

Neutrino selection: boosted decision tree classifier (BDT)
based on 15 track quality variables

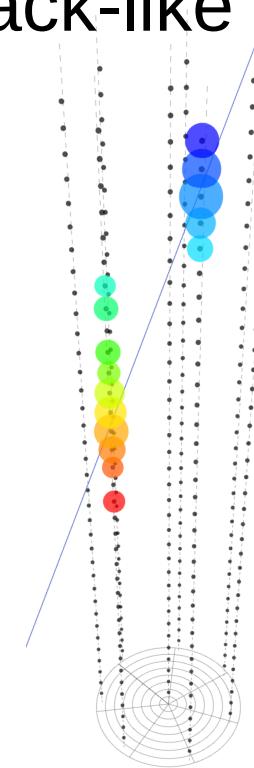
G. Safronov, Neutrino 2022

MC expected: 81.2
Observed events: 106
possible background
contamination under study

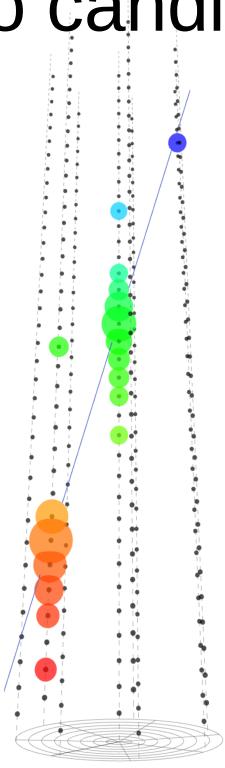
Track-like neutrino candidate events



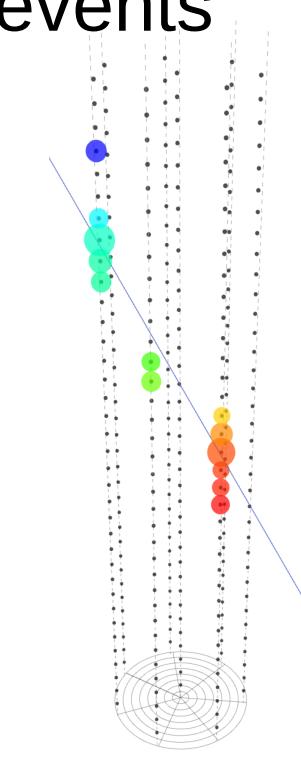
cluster 3, run 122
evt. 1549343
 $\theta_{\text{zenith}} = 169.78^\circ$
 $N_{\text{strings}} = 3$
 $N_{\text{hits}} = 19$



cluster 1, run 157
evt. 1414137
 $\theta_{\text{zenith}} = 161.78^\circ$
 $N_{\text{strings}} = 2$
 $N_{\text{hits}} = 15$



cluster 4, run 99
evt. 438088
 $\theta_{\text{zenith}} = 162.22^\circ$
 $N_{\text{strings}} = 3$
 $N_{\text{hits}} = 18$

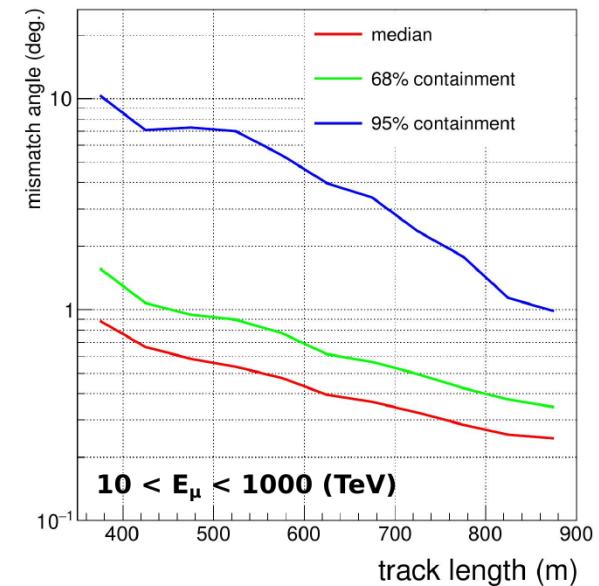
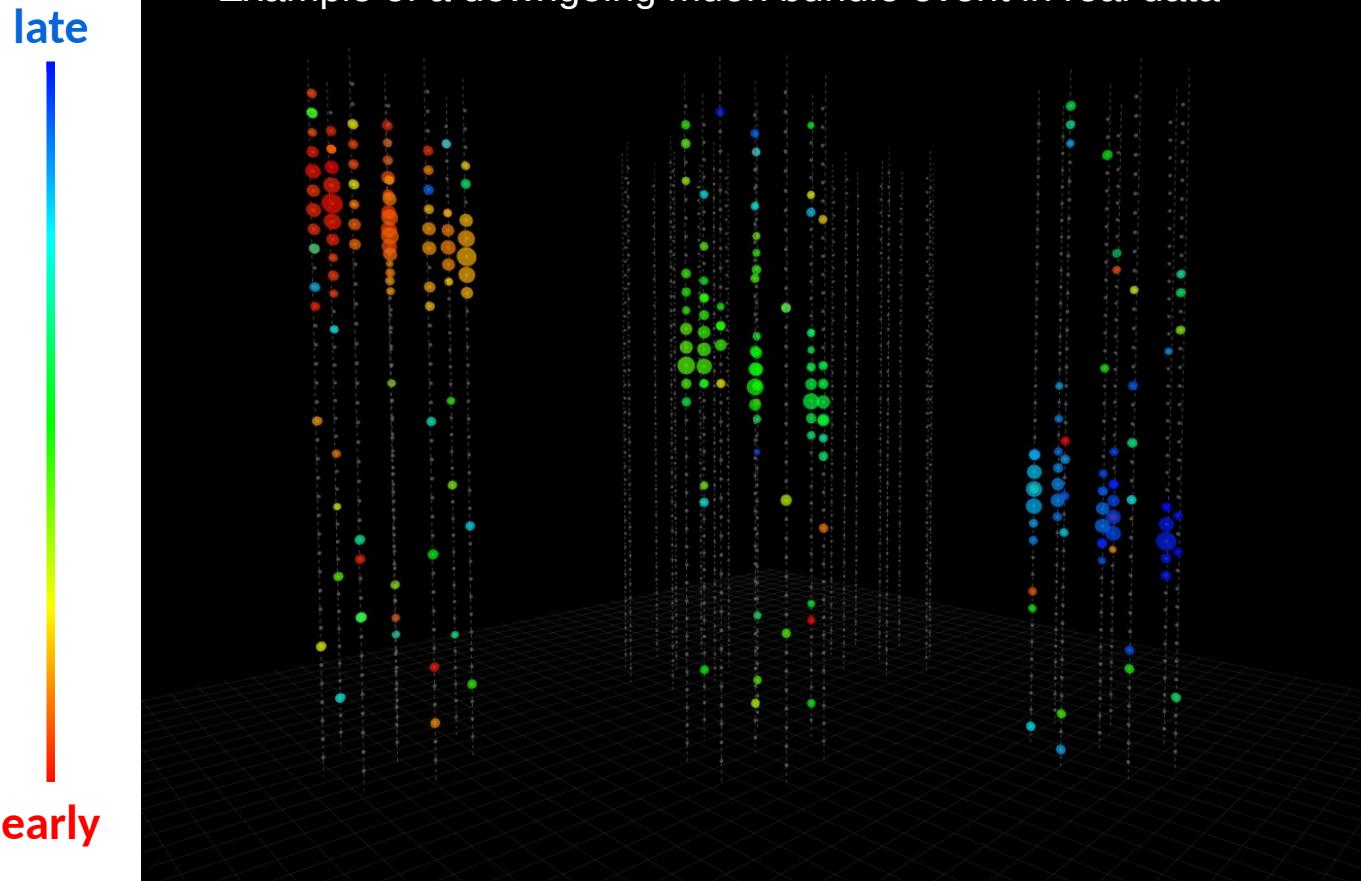


cluster 5, run 162
evt. 1939721
 $\theta_{\text{zenith}} = 148.07^\circ$
 $N_{\text{strings}} = 3$
 $N_{\text{hits}} = 13$



Multi-cluster track events

Example of a downgoing muon bundle event in real data

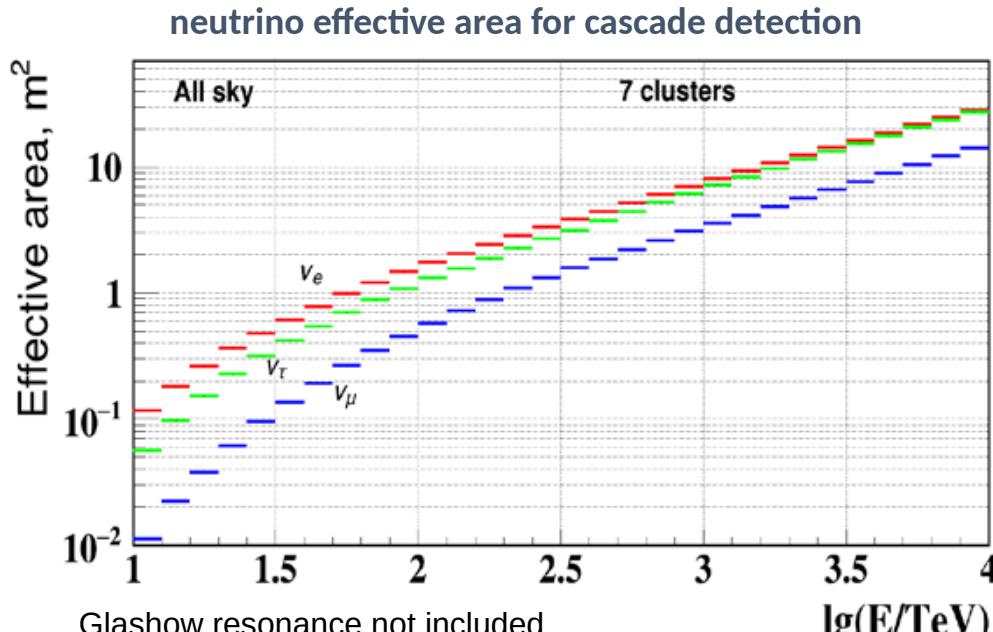


Median energy ~ 4 TeV

Work in progress !

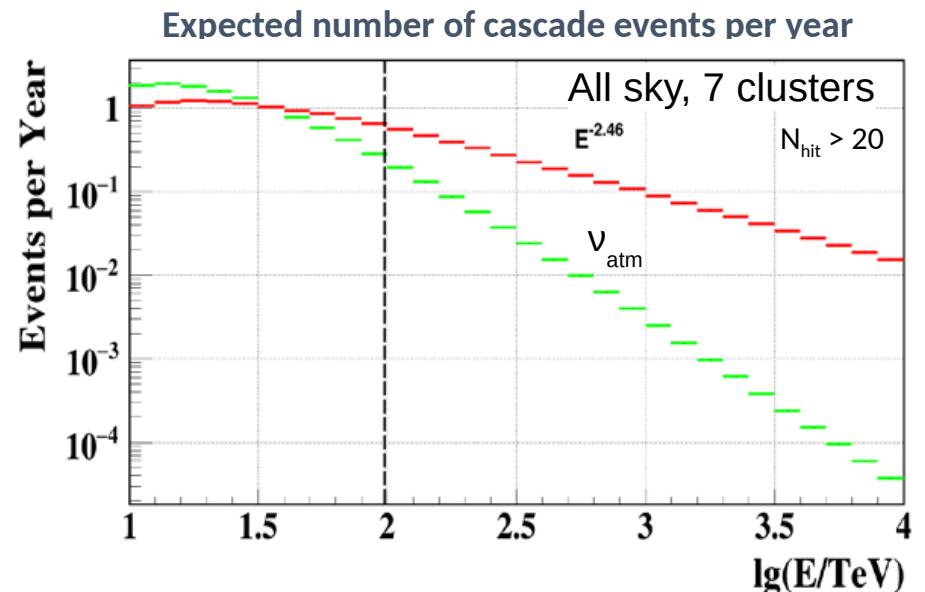
Cascade analysis : effective area and rates

Analysis sensitive to all-flavour CC
and NC interactions over the whole sky



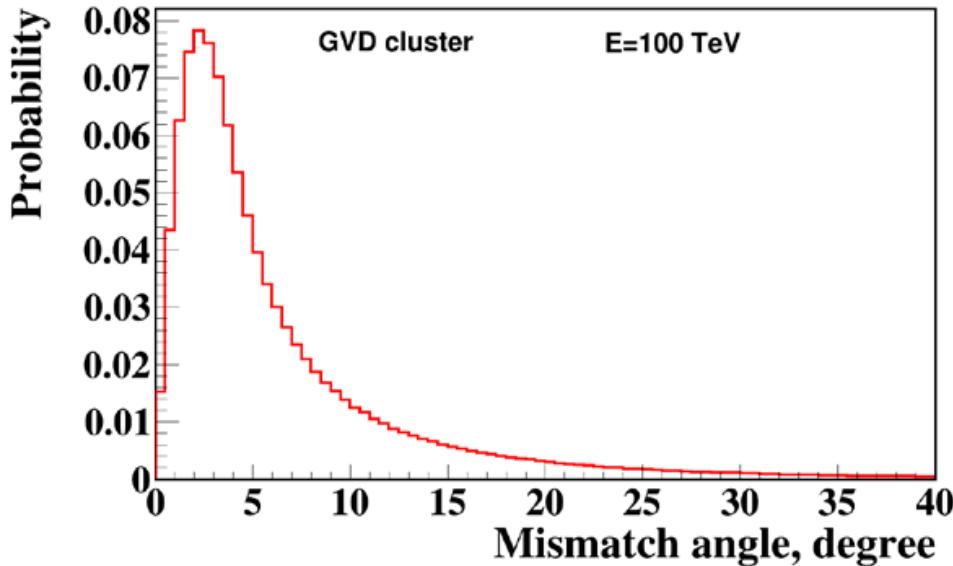
Effective volume for $E > 100$ TeV ~ 0.35 km³

Assumption for astrophysical neutrino energy spectrum (IceCube fit):
 $4.1 \cdot 10^{-6} E^{-2.46}$ GeV⁻¹ cm⁻² s⁻¹ sr⁻¹

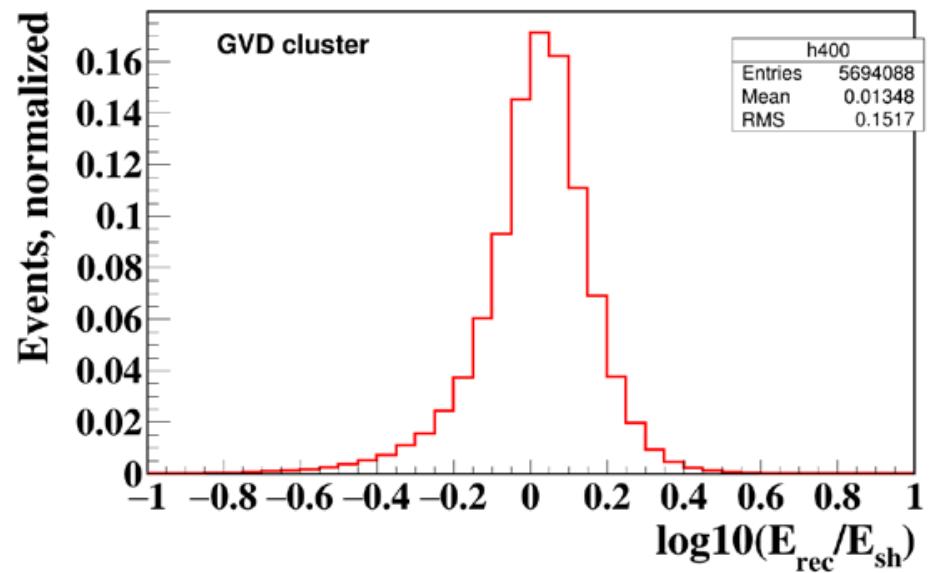


3-4 ev/yr with $E_{sh} > 100$ TeV for 7 clusters

Cascade analysis performance



Directional resolution for cascades:
median mismatch angle $\sim 4.5^\circ$



Energy resolution : $\delta E/E \sim 30\%$

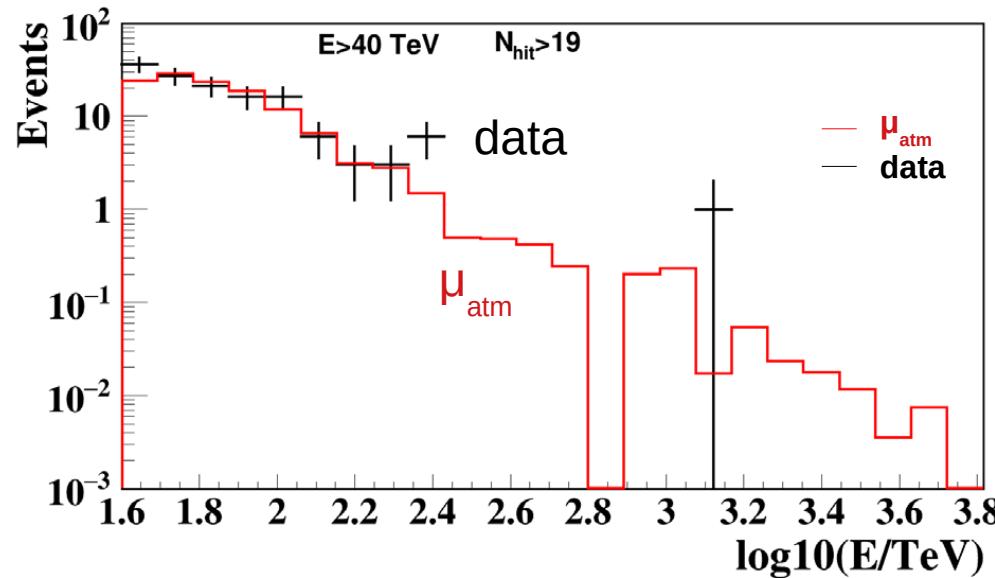
Cascade analysis : data and MC

Preliminary

Data from 2018-2021, livetime: 5522 days single-cluster equivalent

MC atmospheric muons - Corsika 7.74, Sybill 2.3c, protons, $E_p > 100$ TeV

MC atmospheric neutrinos – L.Volkova (1980)



135 events with $E > 40$ TeV
23 events with $E > 100$ TeV

JETP, 134 (2022) 399

All-sky search for HE cascades

Preliminary!

Additional selection requirements:

(N Type_2 = 0, $E_{rec} \geq 70$ TeV) or

(N Type_2 = 1, $E_{rec} \geq 100$ TeV),

(N Type_2 – number of hits in time interval where hits from muons are expected)

Expected:

8.7 events from atm. muons

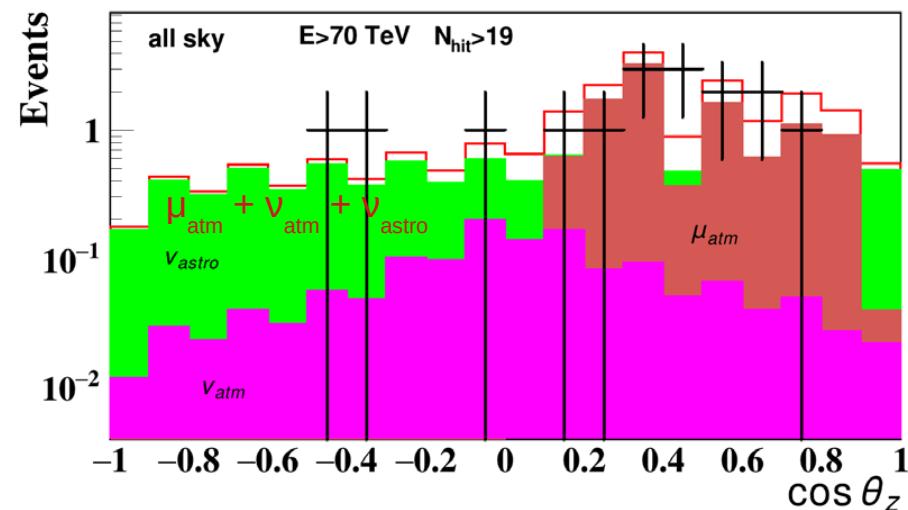
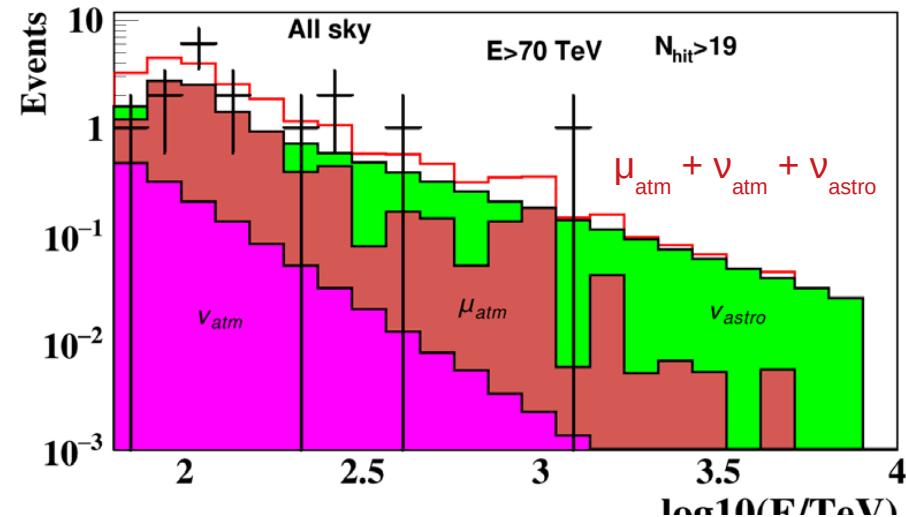
0.8 events from atm. neutrinos

7.8 events for IceCube's $E^{-2.46}$ astrophysical flux

Found in real data: 16 events

Probability for the background-only hypothesis (stat. errors only)

P-value = 0.033 (2.13 σ)



Search for upward moving events

Preliminary!

Additional selection requirements:

$E > 15 \text{ TeV}$ & $N_{\text{hit}} > 11$ & $\cos \theta_z < -0.25$

Expected:

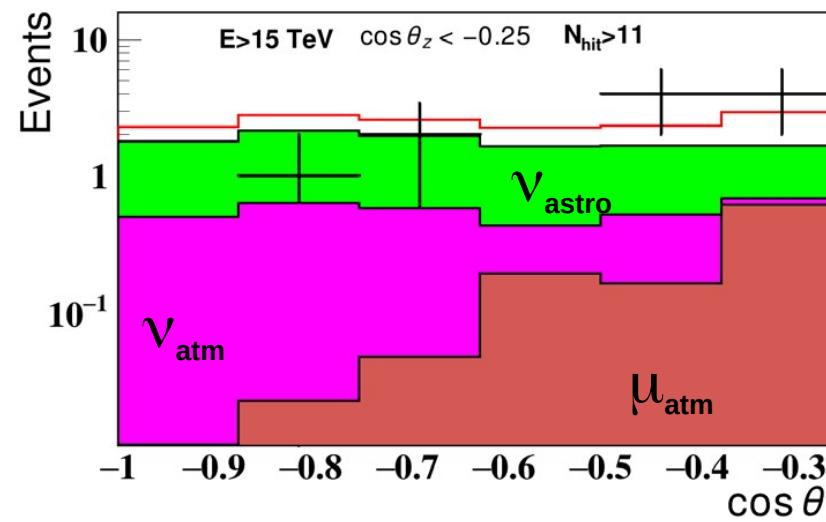
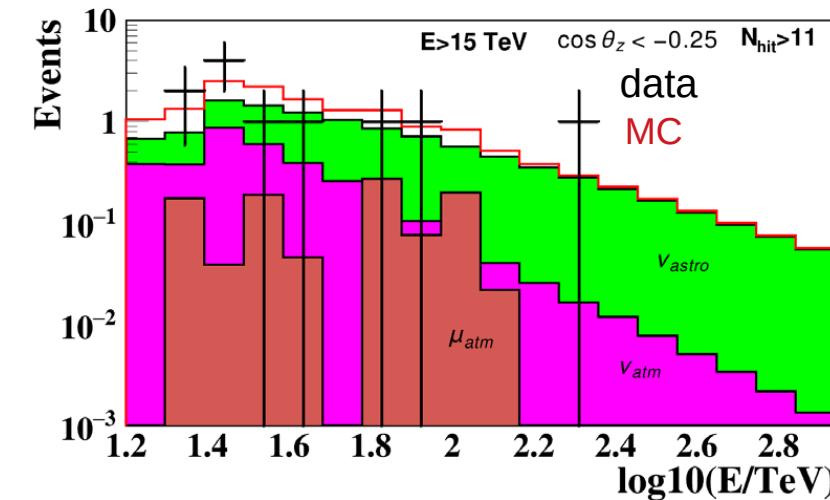
0.95 events from atm. muons

3 events from atm. neutrinos

10 events for IceCube's $E^{-2.46}$
astrophysical flux

Found in data: 11 events

P-value = 0.00268 (3 σ)



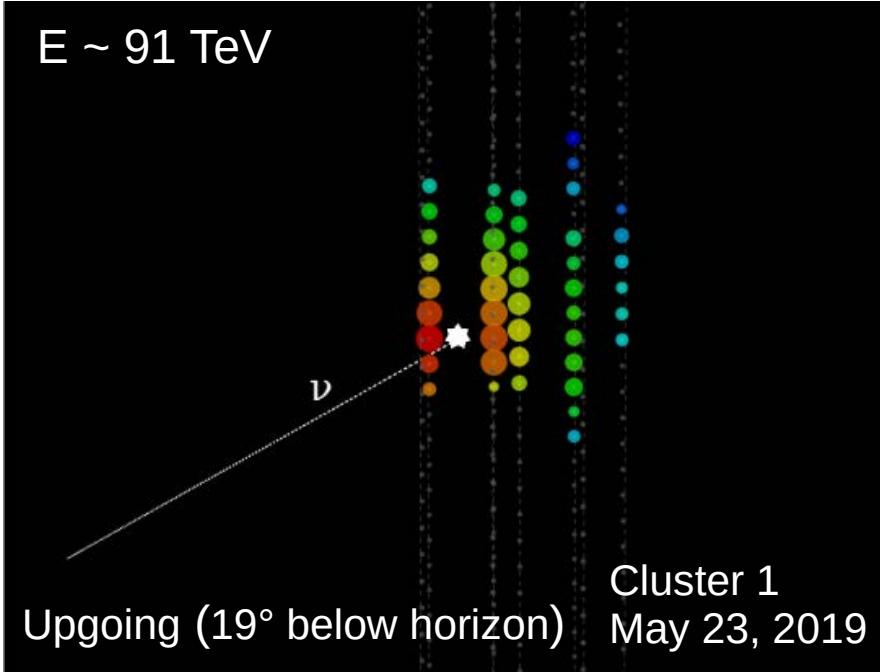


First upward-going cascade event

Preliminary

GVD2019_1_114_N

$E \sim 91 \text{ TeV}$



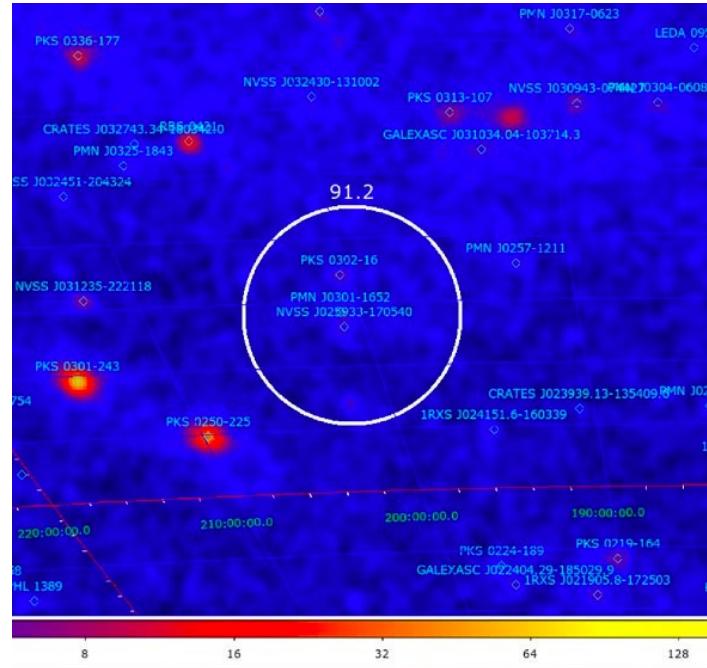
Contained event (50 m off central string)

Excellent candidate for a neutrino event of astrophysical origin

23 июня 2022

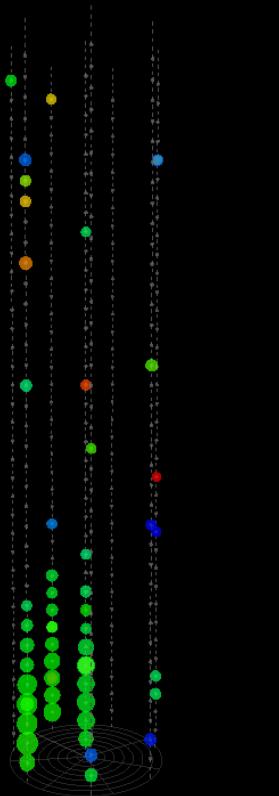
Д.Н. Заборов - Baikal-GVD

Sky plot of γ-ray sources
(credit: D.Semikoz, A.Neronov)



known sources in 3 degree circle:
PKS 0302-16 : unknown type of source
PMN J0301-1652 : unknown type of source

Second upward-going cascade event

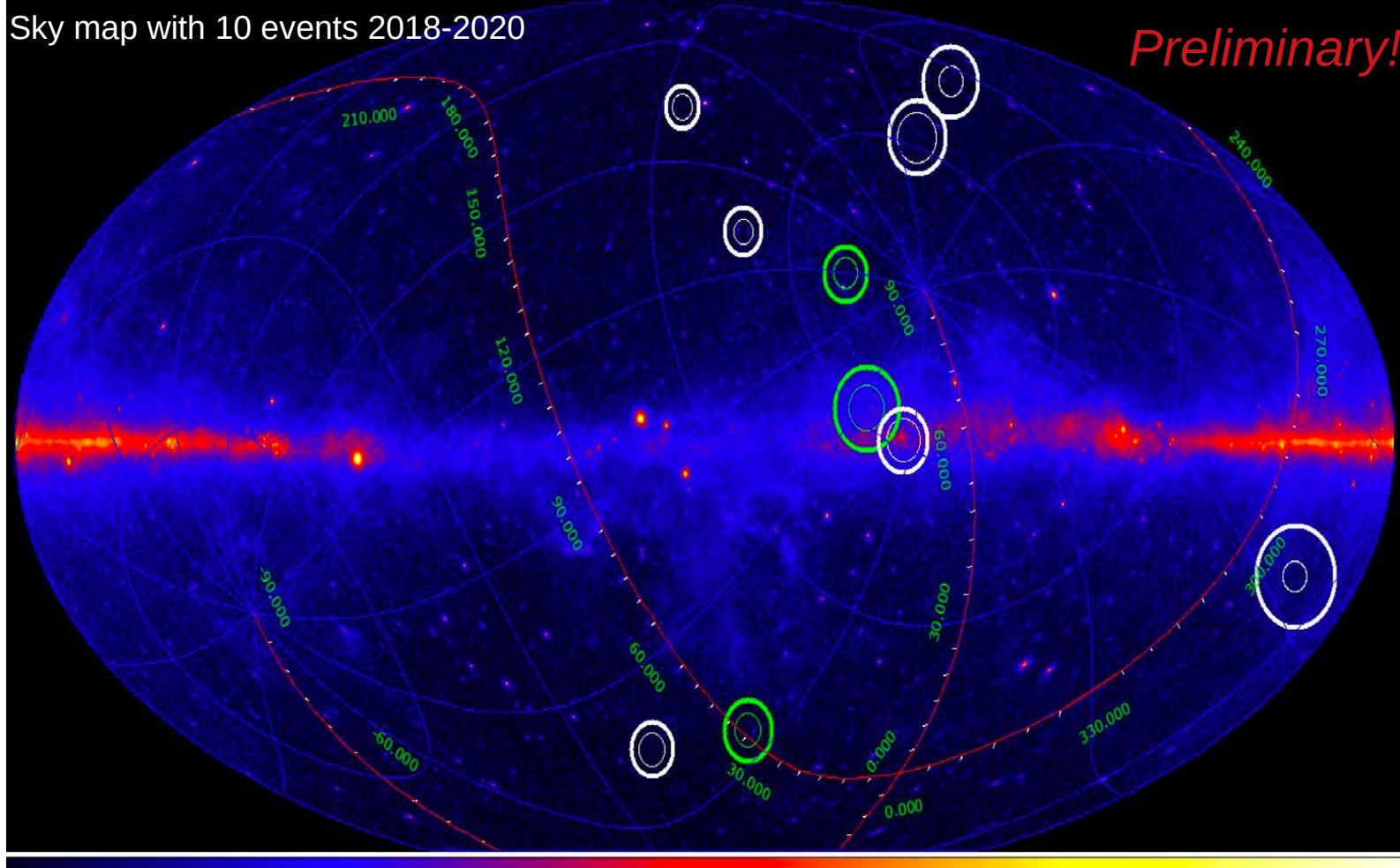


Energy $E = 224 \text{ TeV} (\pm 30\%);$
distance from central string
 $r = 70 \text{ m};$
Zenith angle = 115°

Sky map with 10 Baikal-GVD cascade events

Sky map with 10 events 2018-2020

Preliminary!



Background image:
Fermi LAT

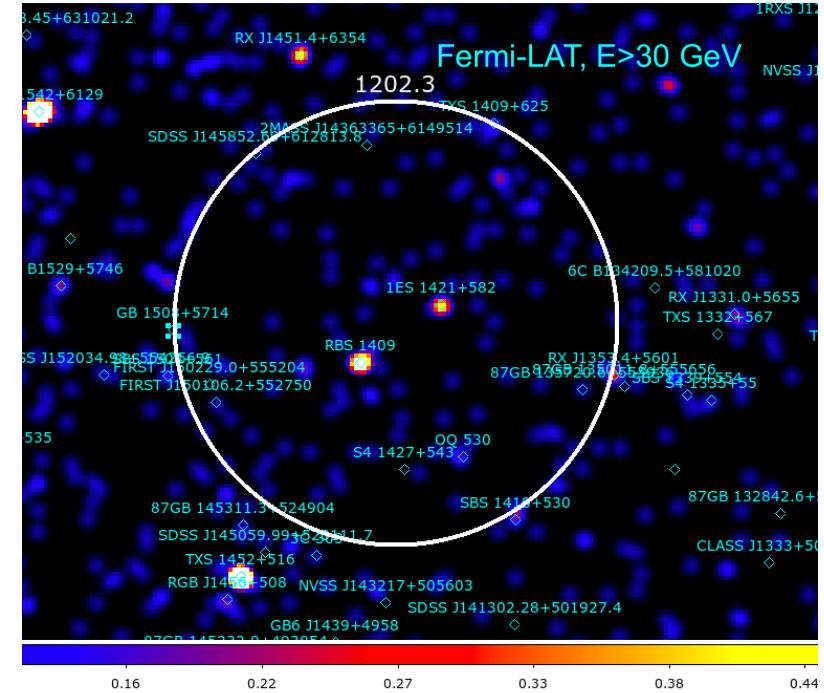
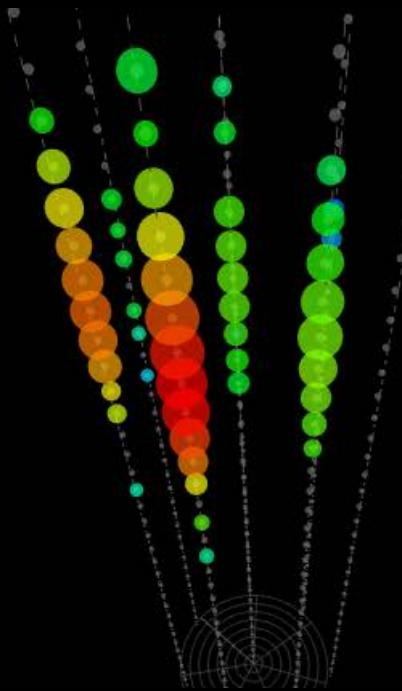
Green circles:
Baikal-GVD
events 2018
(50% and 90%
C.L. regions)

White circles:
Baikal-GVD
events
2019-2020

A 1 PeV cascade event (downgoing)

Preliminary

GVD_2019_112_N

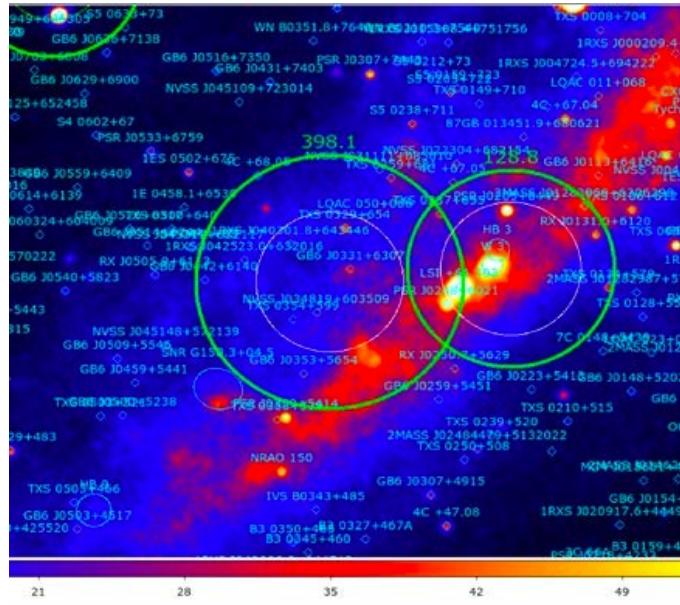


Fermi sources in 5° circle:
RBS 1409 BL Lac z=unknown
1ES 1421+582 z=unknown
both with hard spectrum

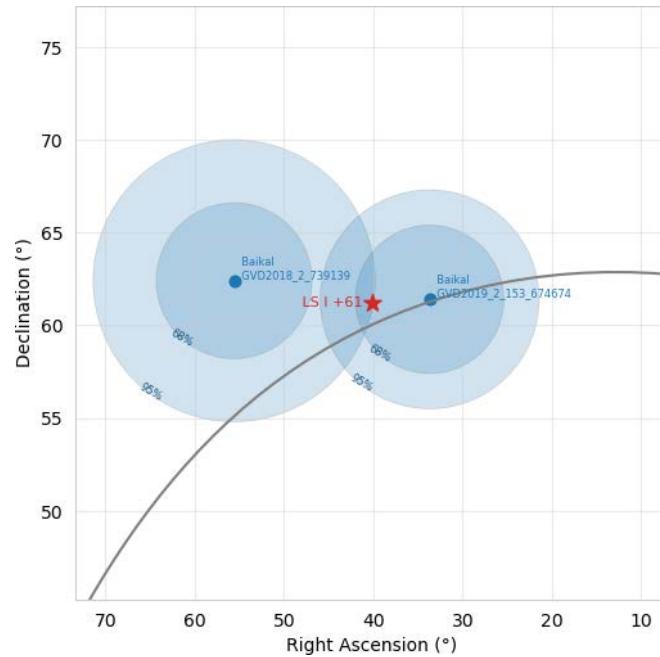
Event doublet near Galactic plane

Preliminary

Sky map of Fermi sources



LSI +61 303 and the two Baikal-GVD events



LSI +61 303 – γ -ray active microquasar

3.1° from GVD_2019_153_N and 7.4° from GVD_2018_656_N

Using PSFs of all 10 events the chance probability to observe such a doublet near LSI +61 303 was estimated: p-value = 0.007 or 2.7 σ (preliminary)

GVD follow up of ANTARES alerts

Following ANTARES upgoing μ alerts ($\langle E \rangle = 7$ TeV)

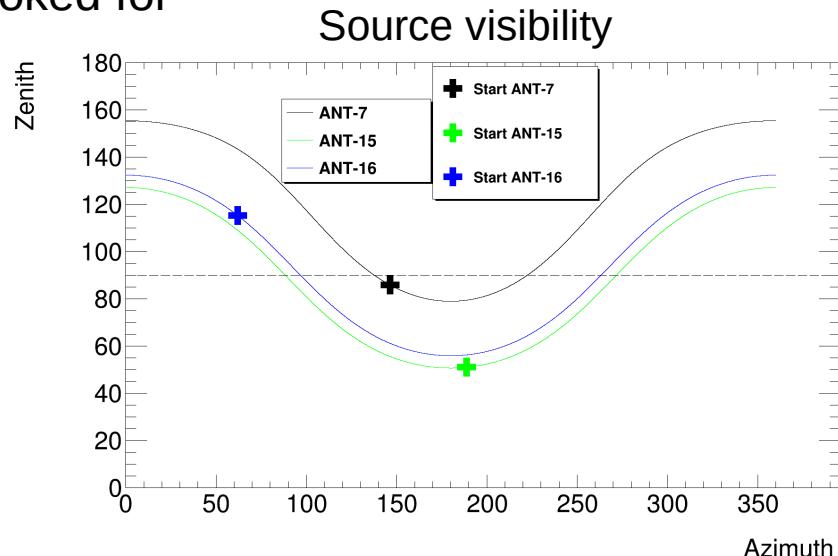
Time windows: ± 500 sec, ± 1 hour and ± 1 day

Both upgoing and downgoing cascades are looked for

Since Dec 2018, 60 alerts
have been analysed

3 potentially interesting events

ANT alert	GVD cluster	$T - T_{\text{alert}}$, hours	Energy, TeV
A7	3	+20.8	13.5
A7	3	-23.2	158
A7	2	-3.2	2.9
A15	2	+20.4	3.0
A15	3	-0.64	3.98
A16	2	-18.7	3.99
A16	4	-14.35	3.89



No prompt coincidence in time and direction was found

O. Suvorova et al. @ Neutrino 2022

O. Suvorova and A. Garre @ ICRC 2021

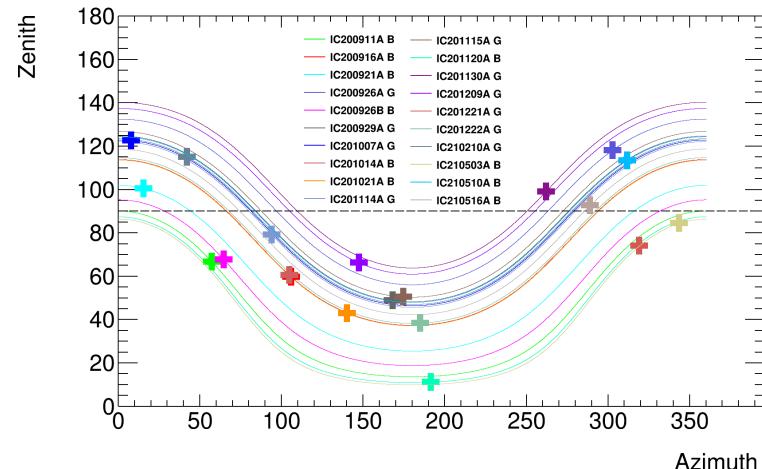
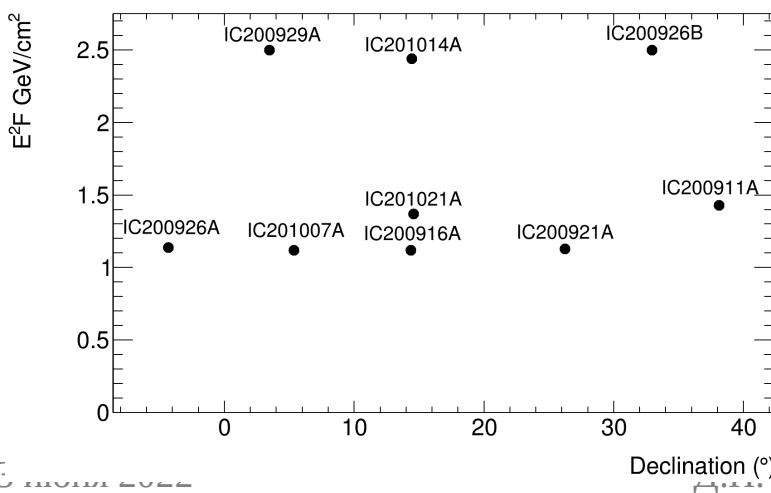
GVD follow up of IceCube alerts

Since Sep 2020, following IC alerts (GCN / upgoing muons)

No statistically significant coincidence was found in this analysis, except possibly IceCube-211208A (see next slide)

90% upper limits derived for E-2 spectrum, equal fluence in all flavors, for $E \sim 1 \text{ TeV} - 10 \text{ PeV}$ and $\pm 12 \text{ hr}$ interval

Baikal-GVD upper limits



A.D. Avrorin et al., Astronomy Letters, Vol. 47, N 2, 114 (2021)

<http://dx.doi.org/10.1134/S1063773721020018>

V.Y. Dik et al., JINST 16 (2021) C11008

<https://doi.org/10.1088/1748-0221/16/11/C11008>

Baikal-GVD follow up of IceCube-211208A / PKS 0735+17

Dec 8, 2021 20:02: IceCube “Astrotrack Bronze” neutrino event

Dec 9, 2021: MASTER reports optical activity of PKS 0735+17
(slightly outside the 90% IceCube uncertainty region)

... PKS 0735+17 observed in HE gamma-rays (Fermi LAT), X-rays
(Swift XRT) and radio

... ANTARES reports upper limits for PKS 0735+17 (no detection)

... KM3Net reports a neutrino with a background p-value = 0.14

... **Baikal-GVD** reports a downward-going (30° above horizon)
cascade-like event 4 hr after the IceCube event from the direction
RA=119.44°, Dec=18.00°, that is **4.68° from PKS 0735+17** and 5.30°
from the best-fit direction of IceCube-211208A

Estimated energy = 43 TeV

PSF 50% (68%) containment radius = 5.5 deg (8.1 deg)

Background estimate: 0.0044 events in the 5.5 deg cone in 24 hr
(2.85 σ). Trail factors to be scrutinized

* PKS 0735+17 is a bright blazar very similar to TXS 0506+056

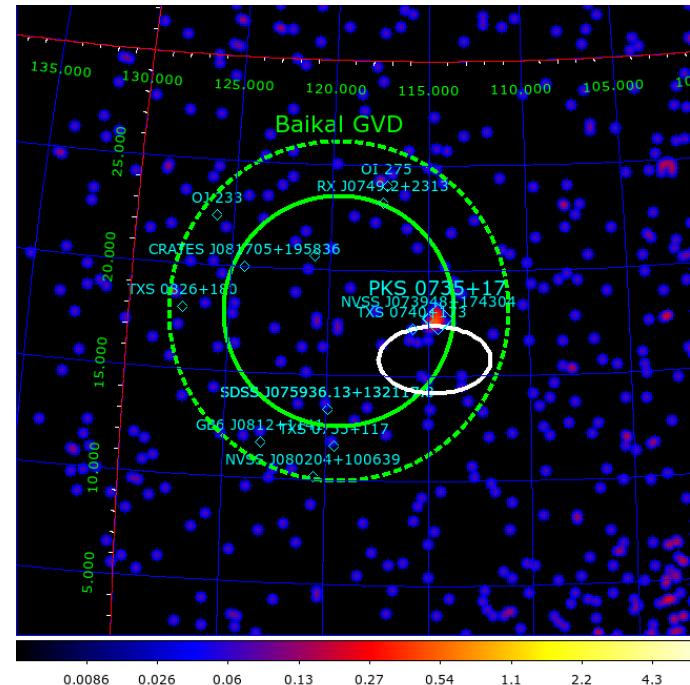


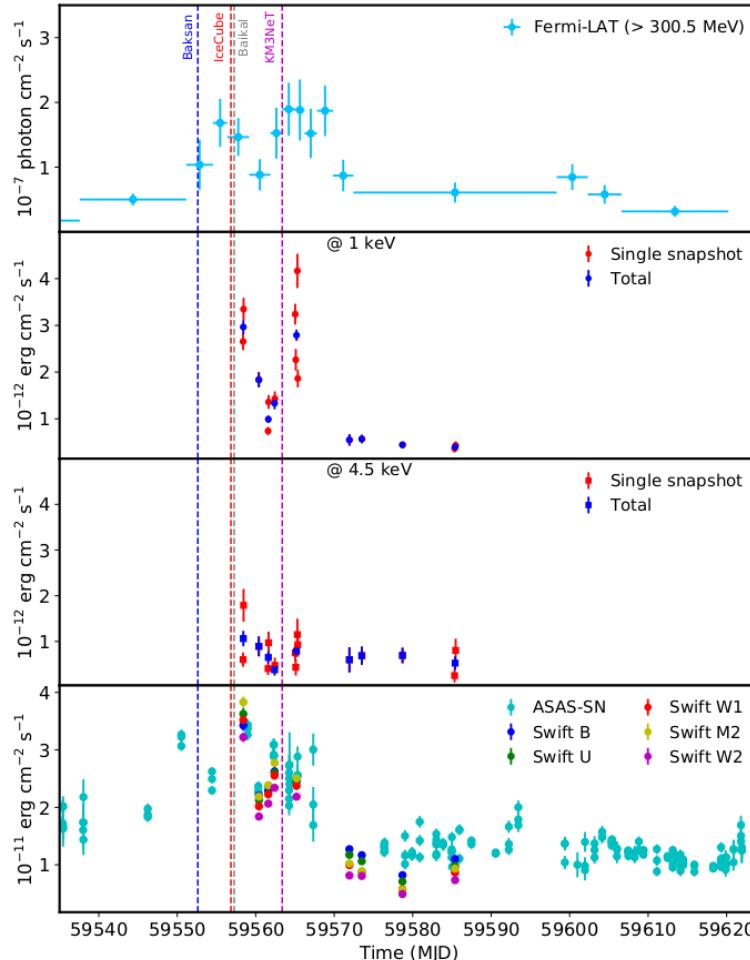
Image by D.Semikoz & A.Neronov

Заключение

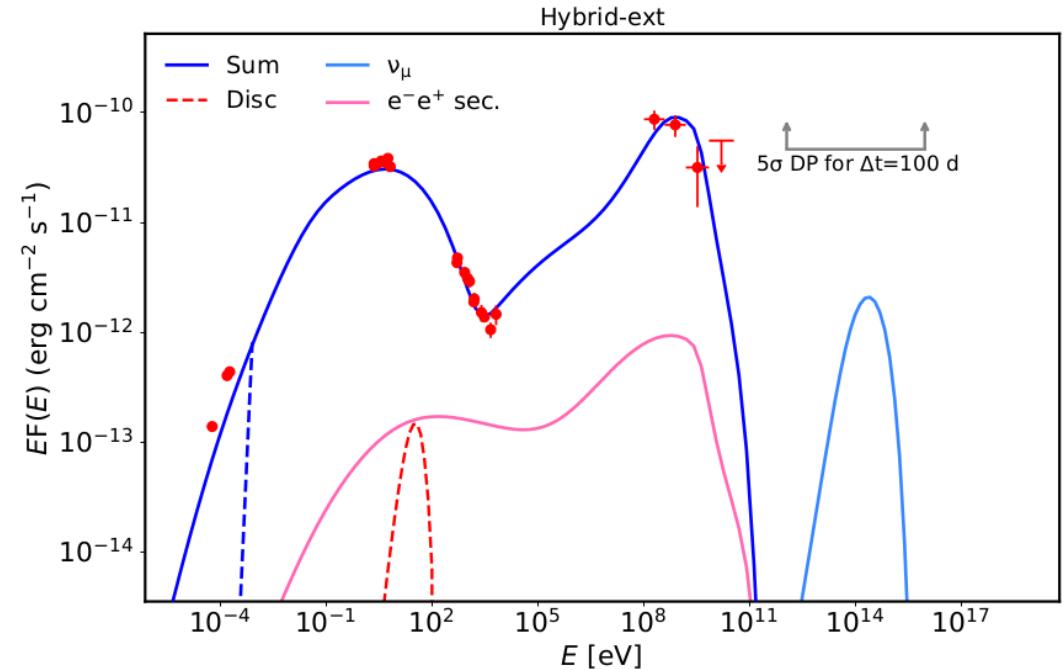
- Baikal-GVD – новый нейтринный телескоп в озере Байкал
 - Объём порядка 1 км³ (по завершении строительства)
 - Угловое разрешение лучше 1° (для треков)
 - Область зрения эффективно дополняет IceCube
- Обнаружены первые намеки на ранее неизвестные источники нейтрино
- Идет набор данных с 10 кластерами (~ 0.5 км³)

Backup slides

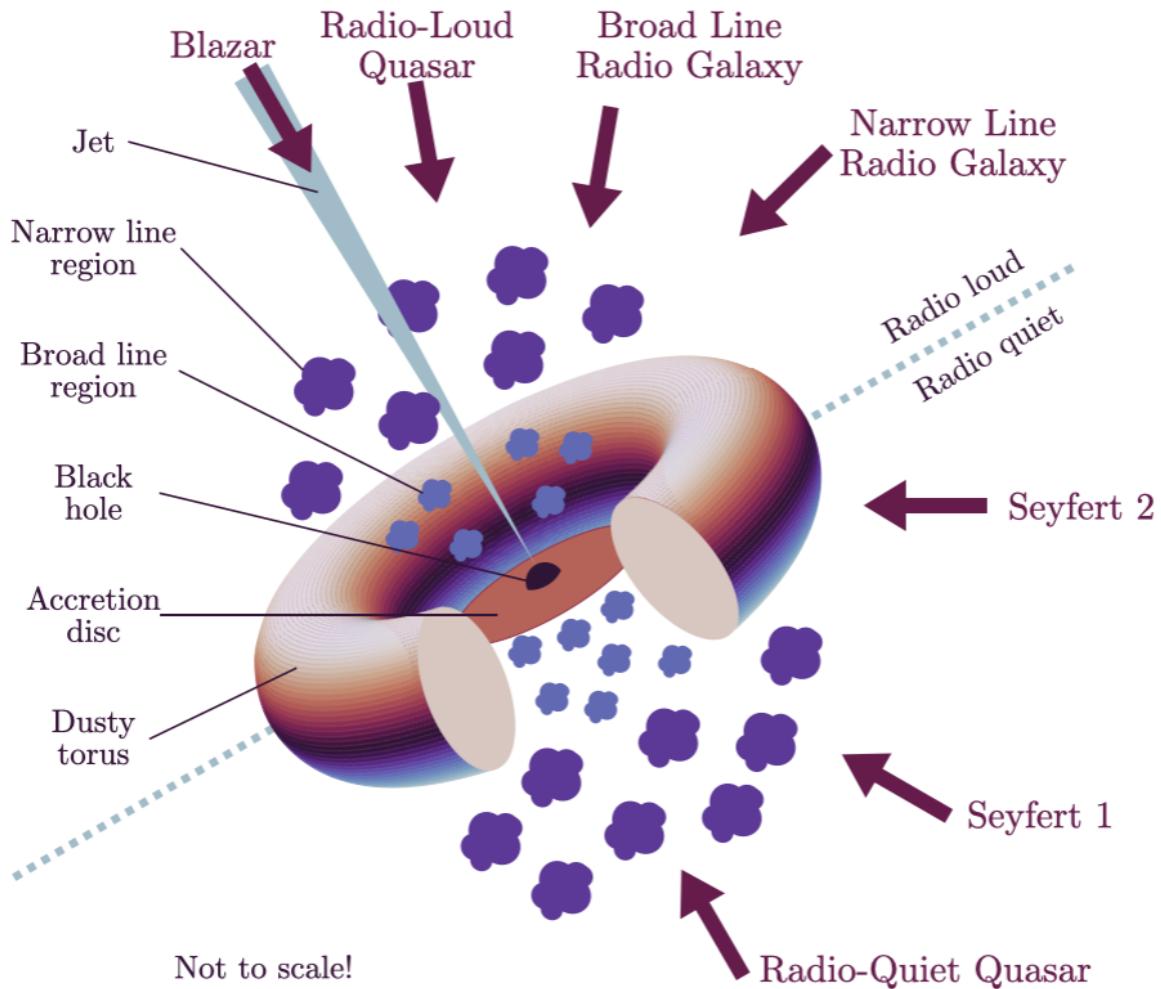
PKS 0735+17 : a neutrino-emitting blazar?



N. Sahakyan et al., arXiv:2204.05060



A model with PeV protons interacting with an external UV photon field predicts ~ 0.067 muon and antimuon neutrinos over the observed 3-week flare.



AGN origin of the diffuse neutrino flux?

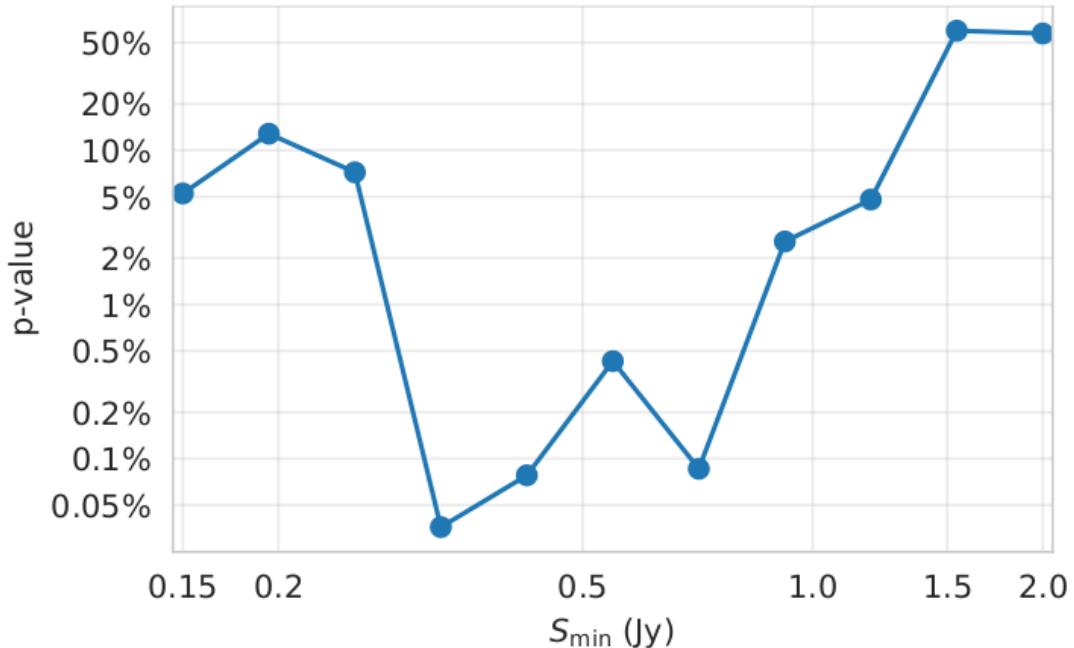
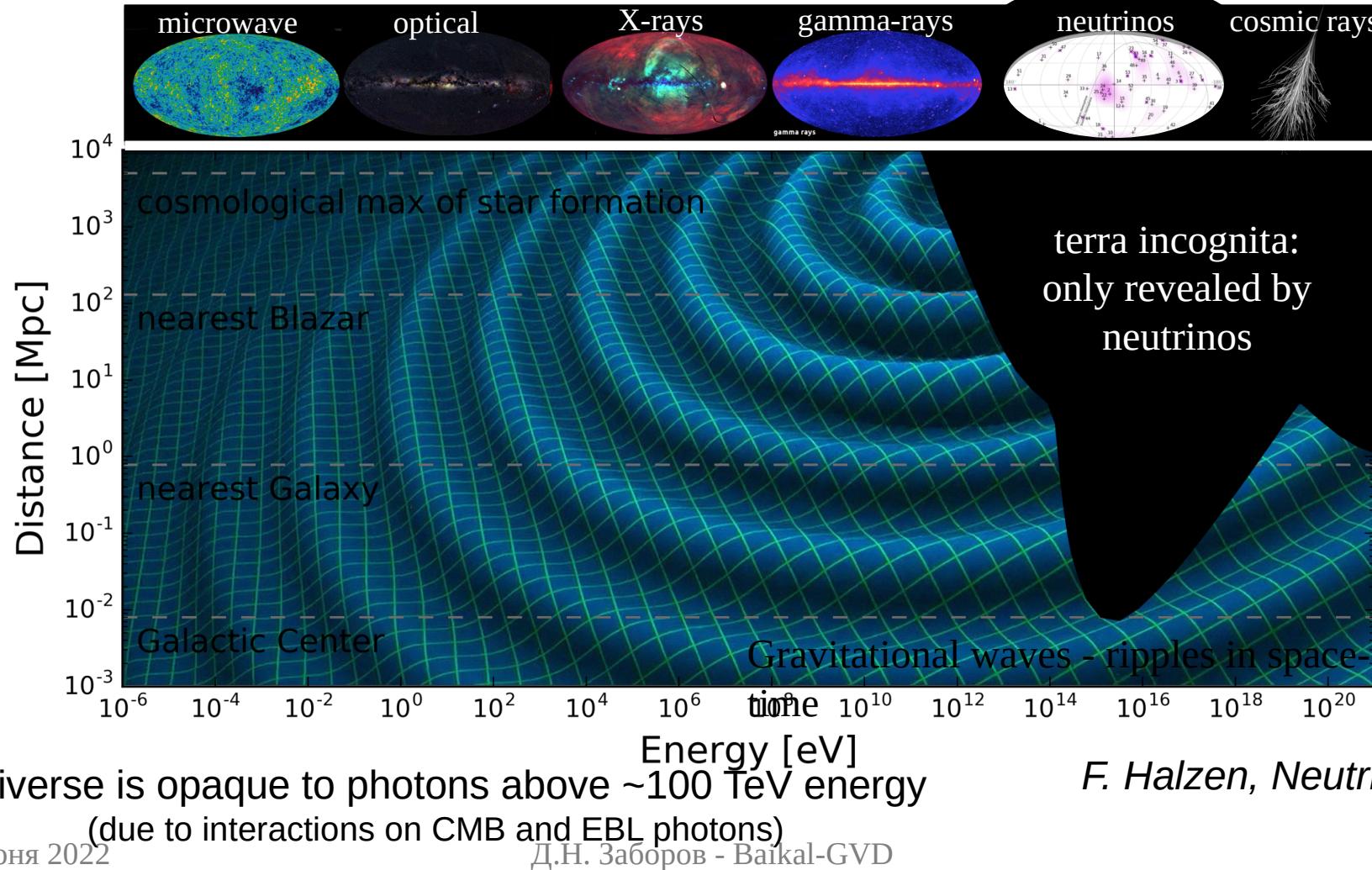


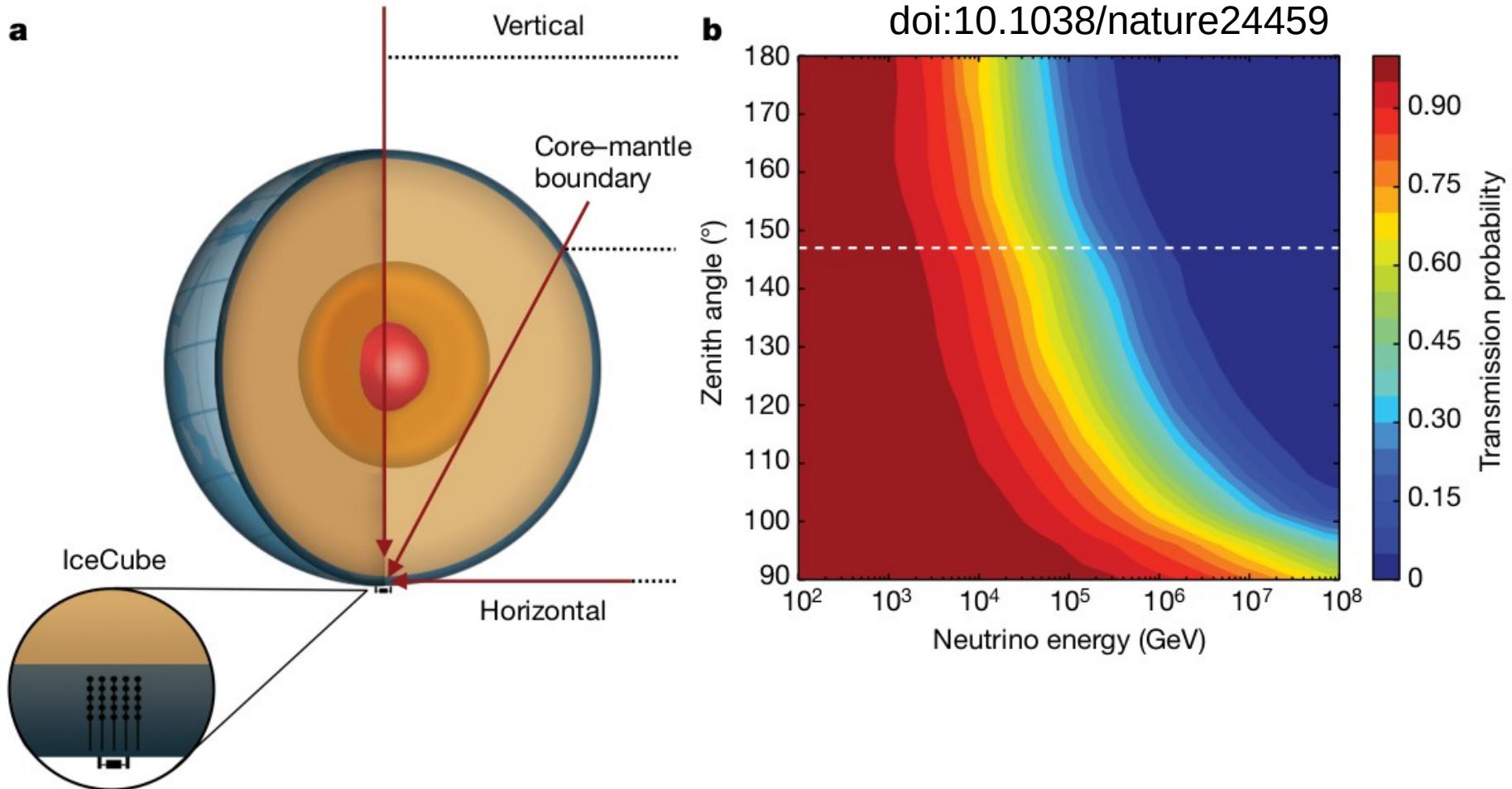
Figure 2. Pre-trial p -values for a range of VLBI flux density cutoffs. The threshold values S_{\min} split the interval 0.15–2 Jy into ten parts uniformly in log-scale. The lowest p -value of $4 \cdot 10^{-4}$ is attained for the threshold of 0.33 Jy.

A. Plavin, Y. Kovalev,
Yu. Kovalev, S. Troitsky:
Directional association of TeV
to PeV astrophysical neutrinos
with active galaxies hosting
compact radio jets,
ApJ 908 (2021) 157
[arXiv:2009.08914]

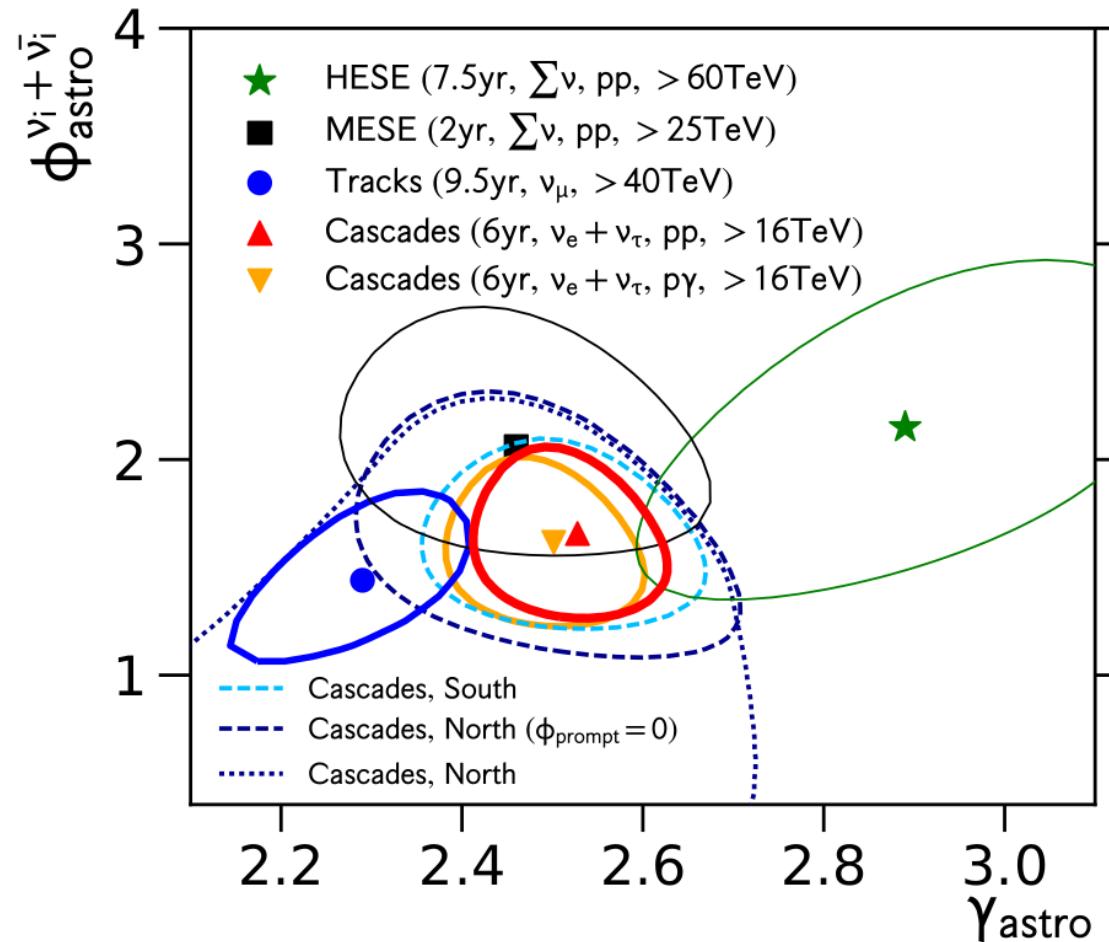
Highest energy radiation in the Universe



Neutrino absorption in the Earth



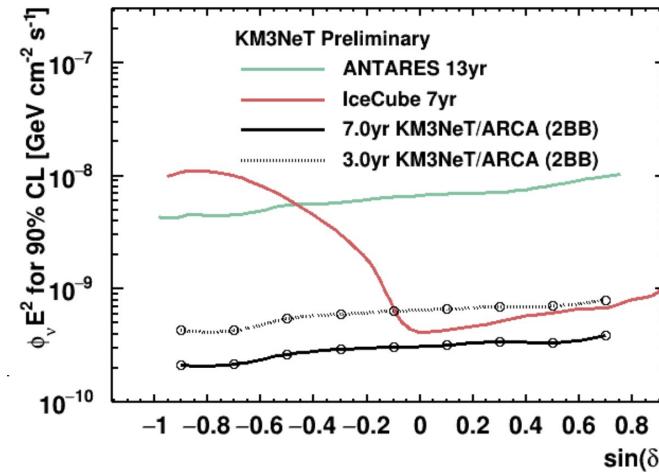
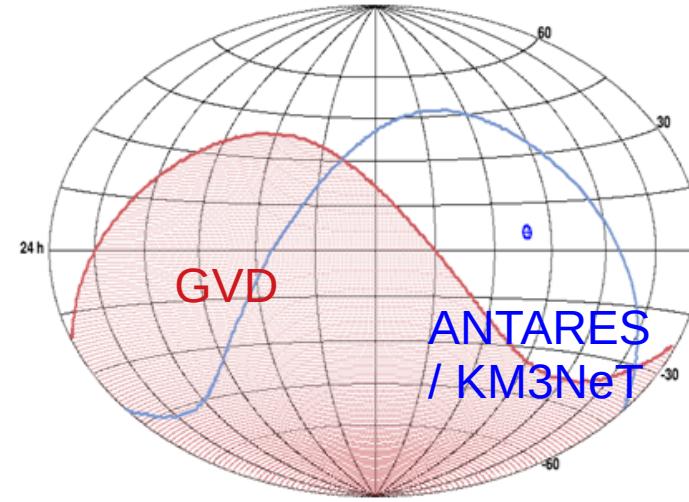
Diffuse neutrino flux



Why two neutrino telescopes in the North

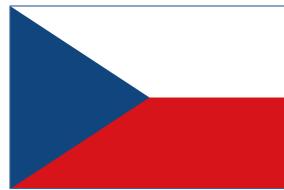
TXS0506+056: IC170922A *S. A. Garre et al.*

- Improved all-sky coverage
 - important for short transients
- Sensitivities add up
 - neutrino astronomy is still limited by low statistics
- Optimize local funding opportunities
 - Funding opportunities often come with geographic restrictions



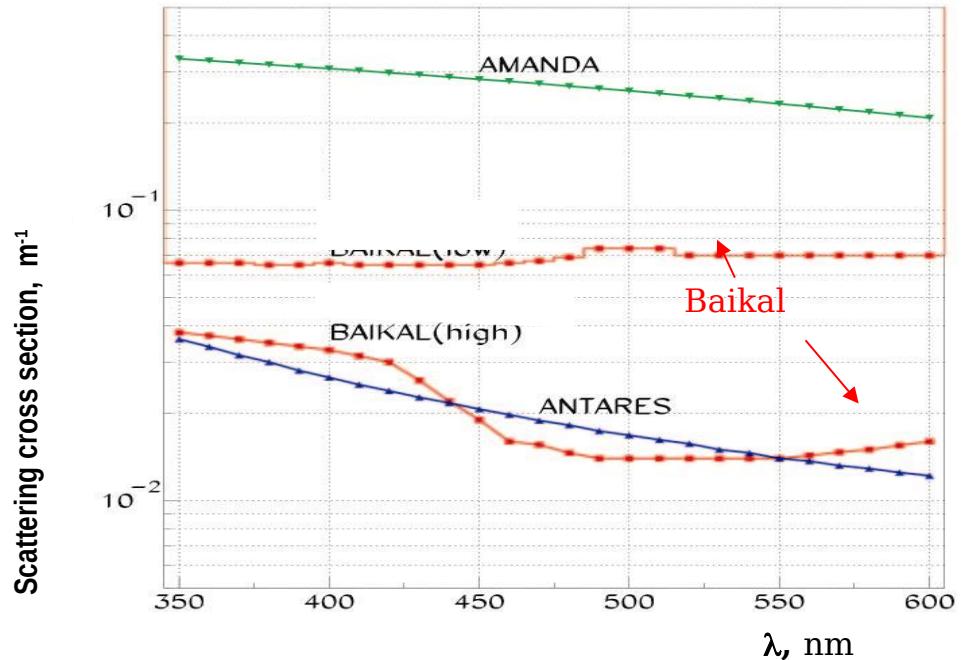
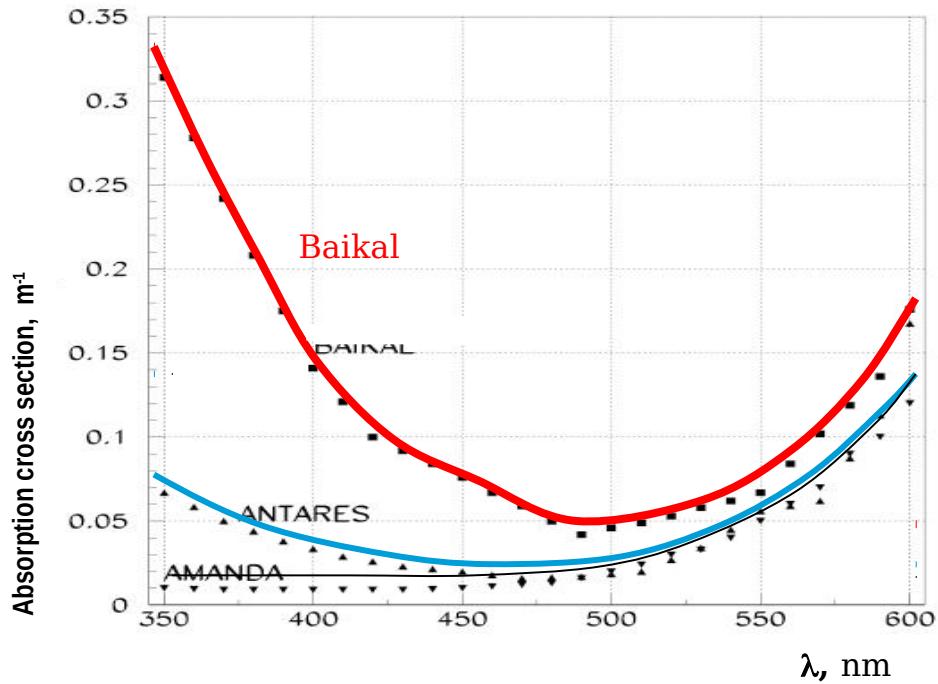
Baikal-GVD collaboration (as of Feb 2022)

11 organisations from 6 countries, ~70 collaboration members

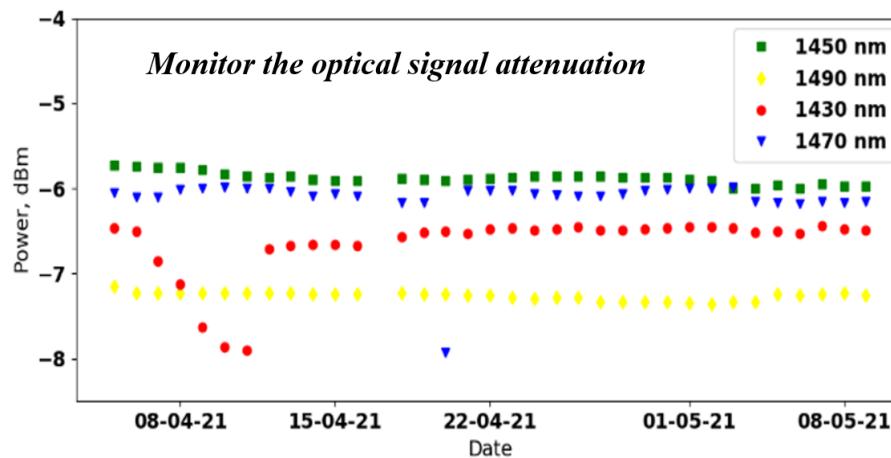
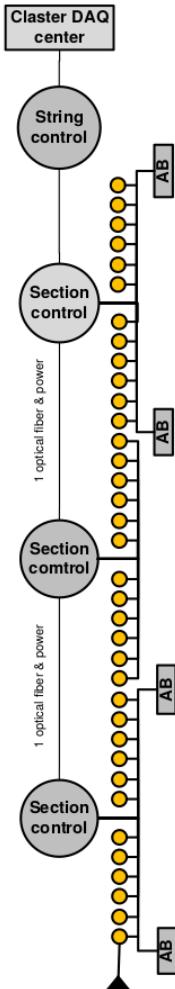


- Institute for Nuclear Research RAS (Moscow)
- Joint Institute for Nuclear Research (Dubna)
- Irkutsk State University (Irkutsk)
- Skobeltsyn Institute for Nuclear Physics MSU (Moscow)
- Nizhny Novgorod State Technical University (Nizhny Novgorod)
- Saint-Petersburg State Marine Technical University (Saint-Petersburg)
- Institute of Experimental and Applied Physics, Czech Technical University (Prague, Czech Republic)
- EvoLogics (Berlin, Germany)
- Comenius University (Bratislava, Slovakia)
- Krakow Institute for Nuclear Research (Krakow, Poland)
- Institute of Nuclear Physics (Almaty, the Republic of Kazakhstan)

Water optical properties



Experimental string with optic fiber DAQ



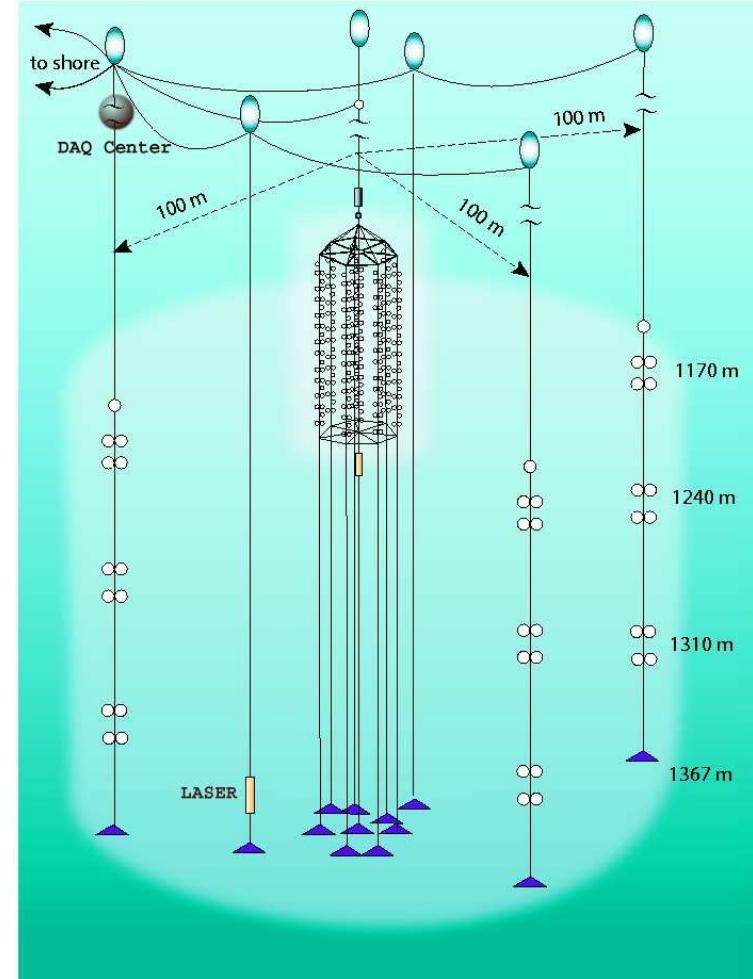
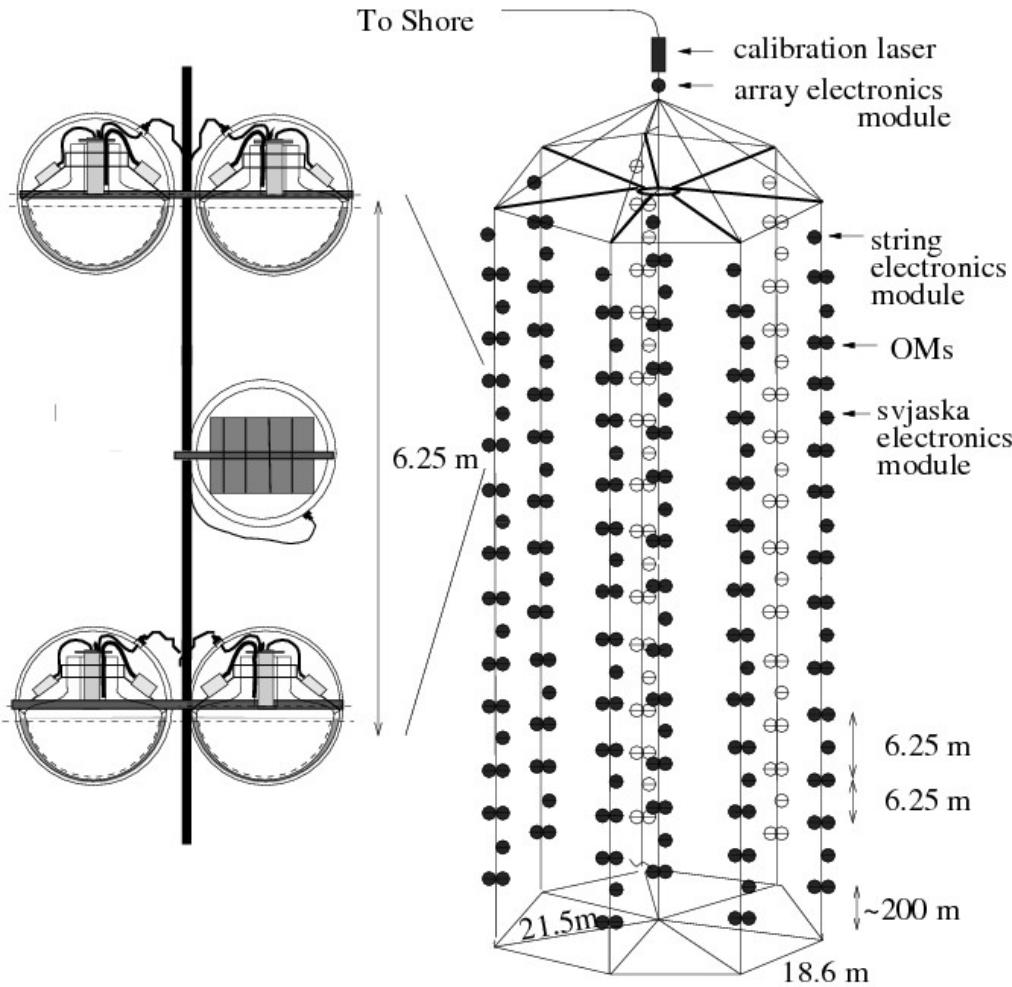
Developing
technological solutions
for second stage of
Baikal-GVD deployment
(2024+)

Advantages:

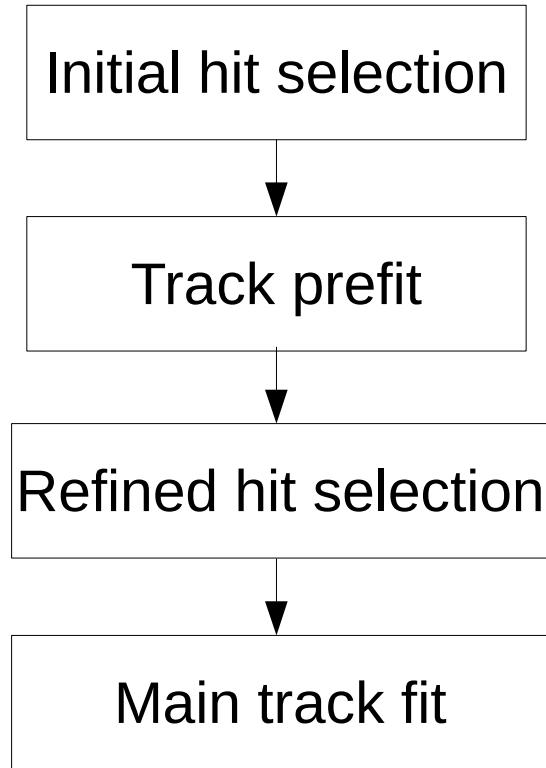
- flexible trigger conditions
- Improved neutrino detection efficiency
- Improved timing accuracy

*See poster by V. Aynutdinov
@ ICRC 2021*

Baikal NT-200 and NT-200+



Track reconstruction with a χ^2 -based algorithm



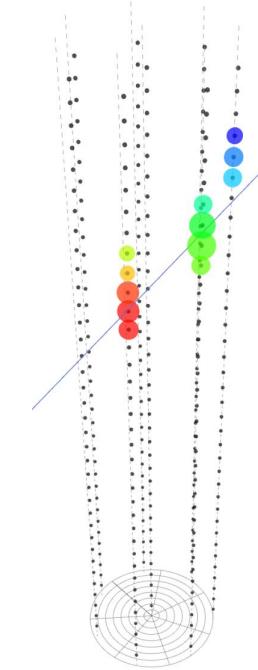
Using vector sum

Minimize quality function

$$Q = \chi^2(t) + f(q, r)$$

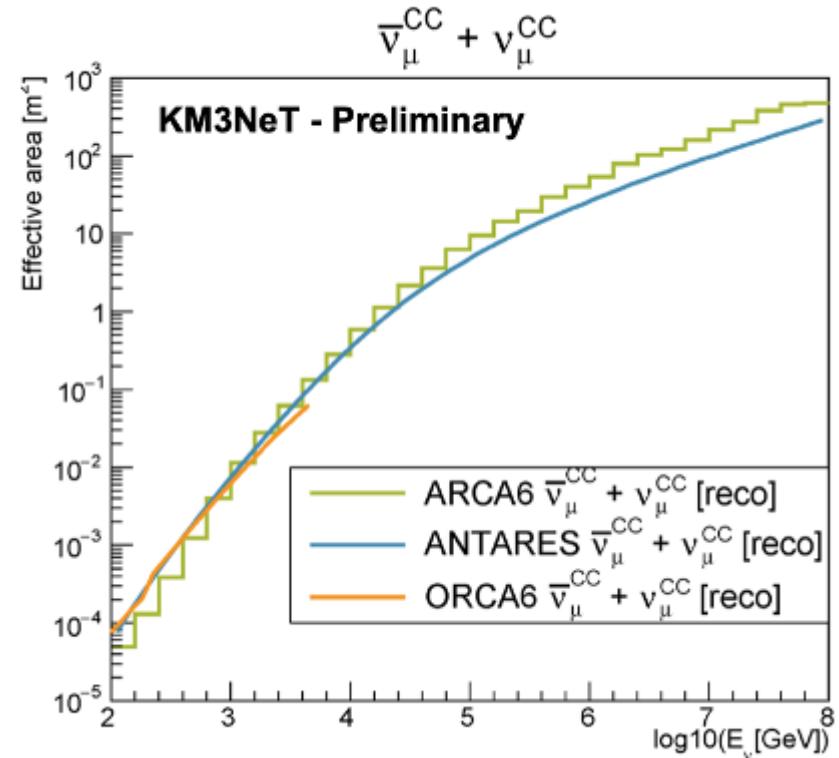
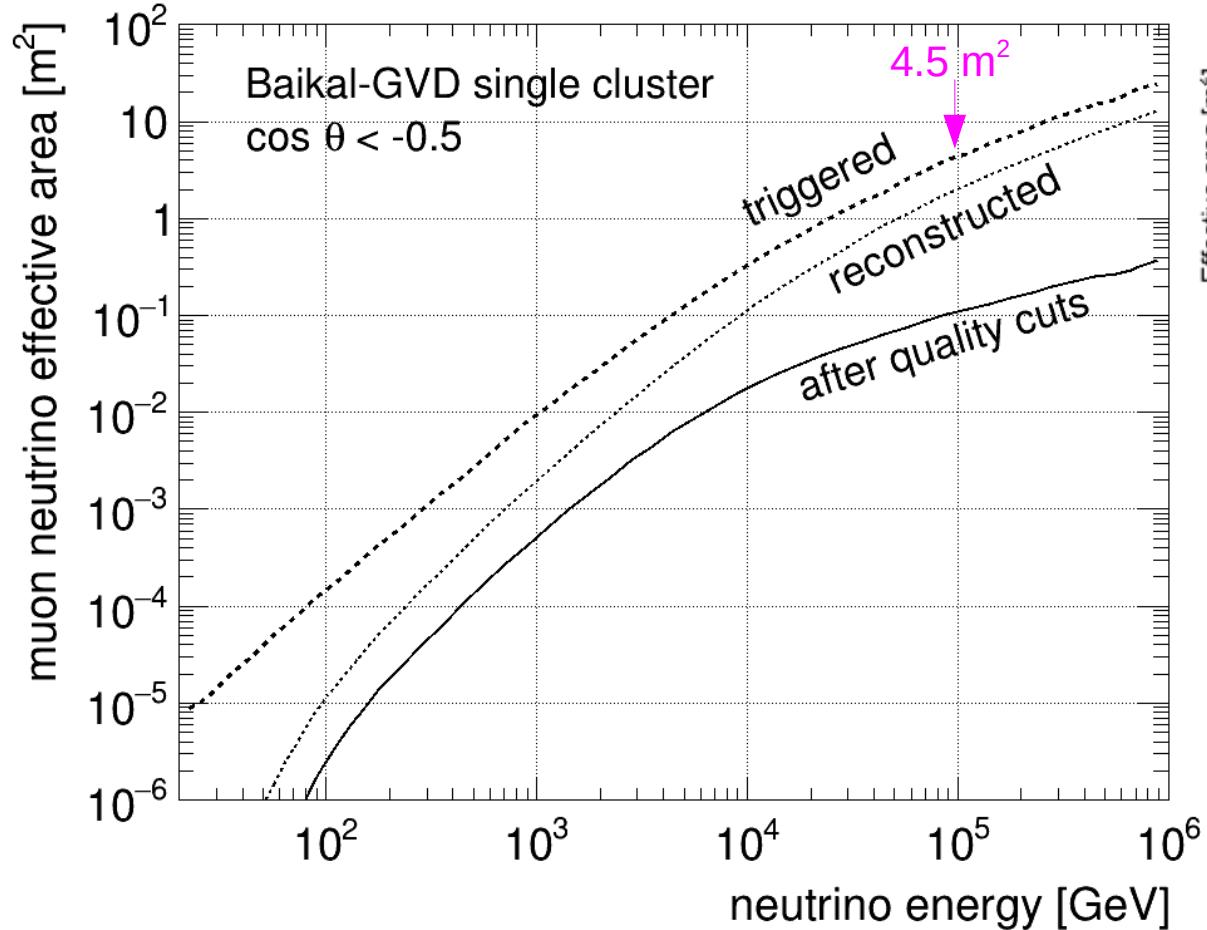
Time residuals

Hit charge and distance



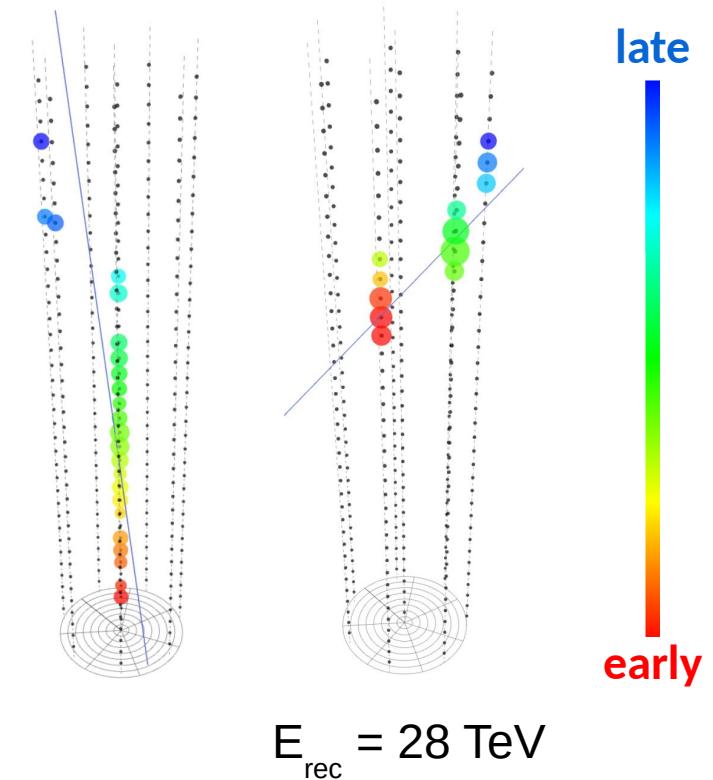
See talk by G. Safronov at ICRC 2021

Neutrino effective area for tracks : one GVD cluster



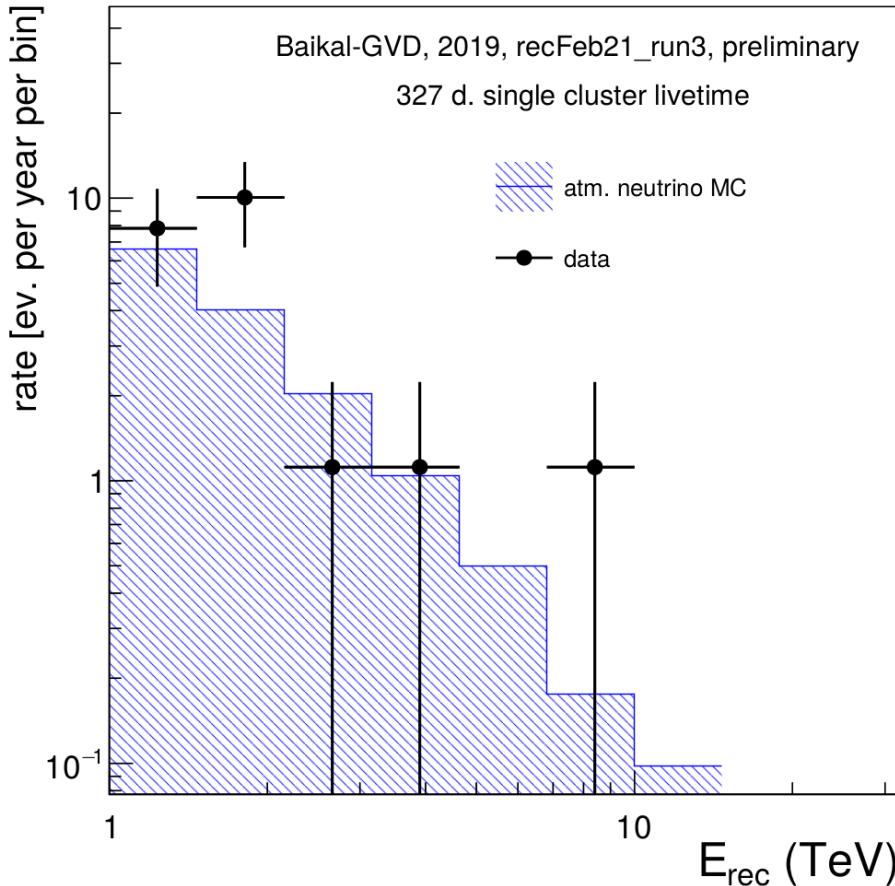
Track reco : ongoing improvements

- Event selection with BDT
→ G. Safronov @ ICRC 2021
- Improved hit selection using clique search → A. Avrorin & B. Shaybonov @ ICRC 2021
- Likelihood fitter
- Machine learning techniques
- ...



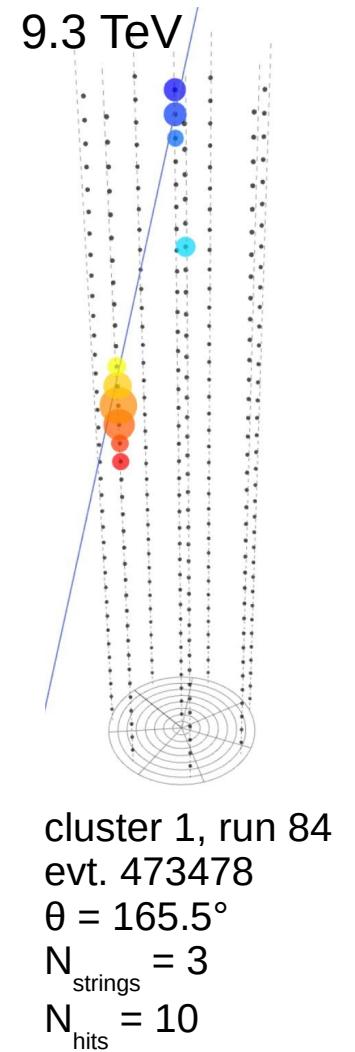
Reconstructed energy for tracks

Example plot for a set of neutrino candidate events

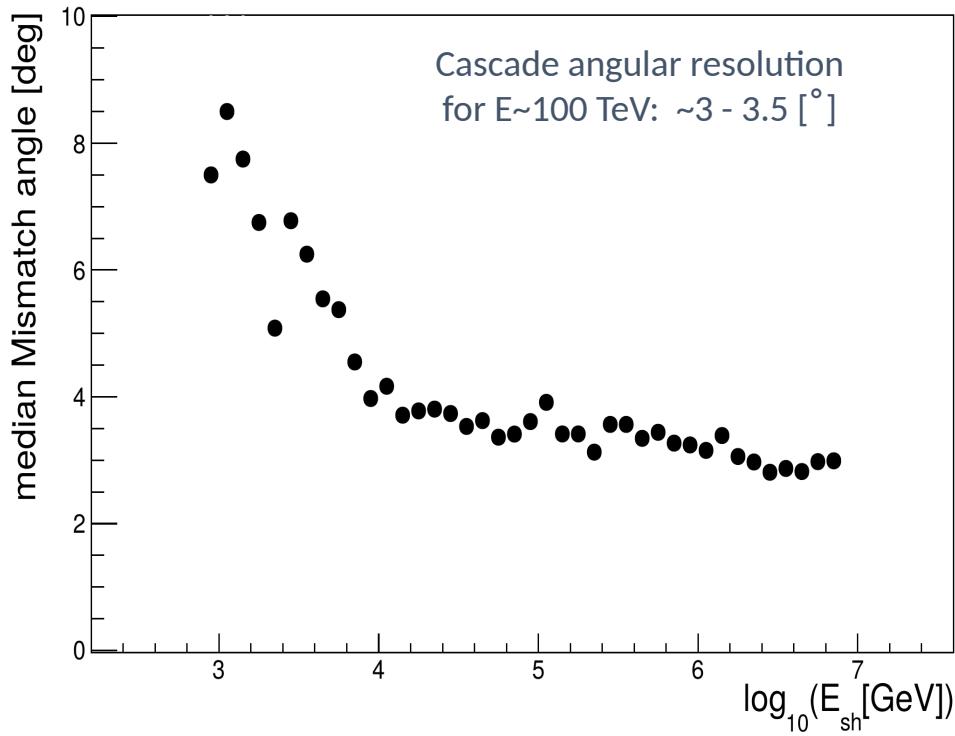


- dE/dx energy estimator -
- Works for $E > 1 \text{ TeV}$
- Largest measured energy in cut-based low-energy neutrino candidate sample:

*see talk by
G. Safronov at ICRC 2021*



Cascade analysis angular resolution



Selected events (2018-2020)

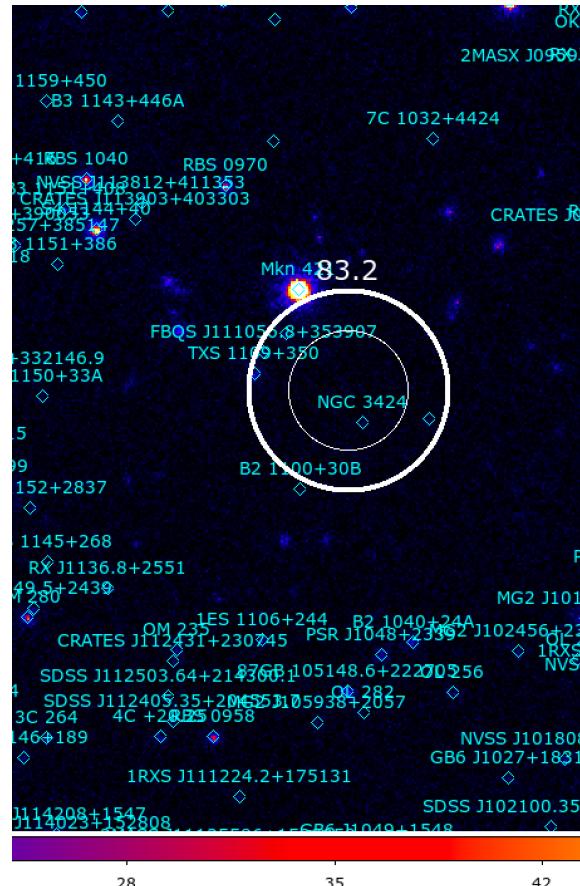
Preliminary

	E, TeV	θ_z , degree	ϕ , degree	R.A.	Dec
GVD2018_354_N	105	37	331	118.2	72.5
GVD2018_383_N	115	73	112	35.4	1.1
GVD2018_656_N	398	64	347	55.6	62.4
GVD2019_112_N	1200	61	329	217.7	57.6
GVD2019_114_N	91	109	92	45.1	-16.7
GVD2019_663_N	83	50	276	163.6	34.2
GVD2019_153_N	129	50	321	33.7	61.4
GVD2020_175_N	110	71	185	295.3	-18.9
GVD2020_332_N	74	92	9	223.0	35.4
GVD2020_399_N	246	57	49	131.9	50.2

Another event of potential interest

GVD_2019_663

Mrk 421 just outside the error circle

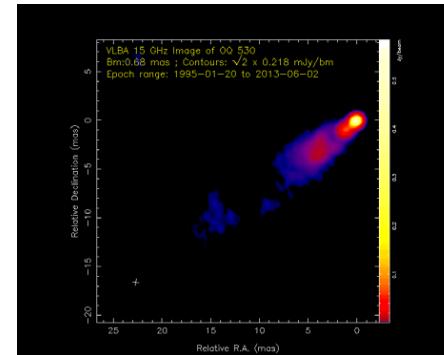
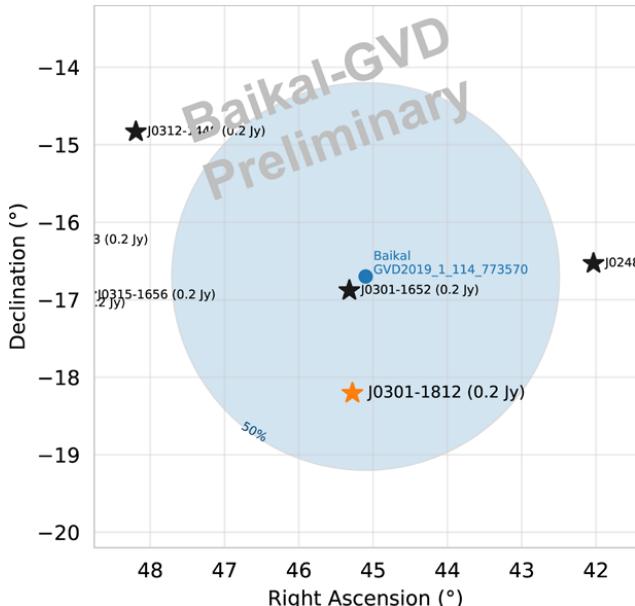


Radio-loud blazars – promising neutrino sources

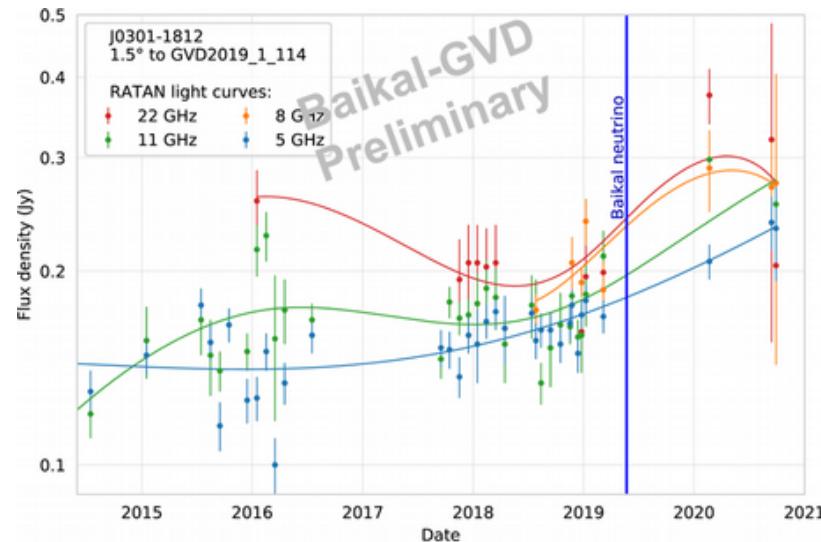
Motivated by

- A. Plavin et al., ApJ 894, 101 (2020)
A. Plavin et al., ApJ 908, 157 (2021)

GVD2019_1_114_N
radio-bright blazars nearby



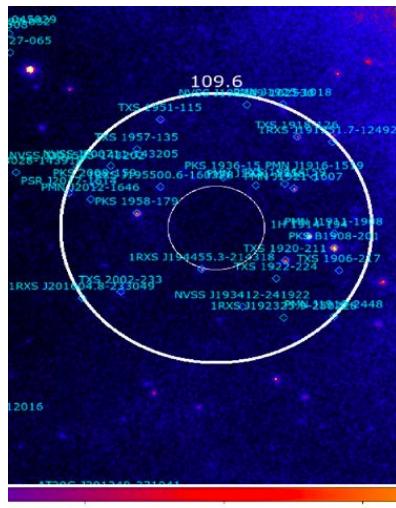
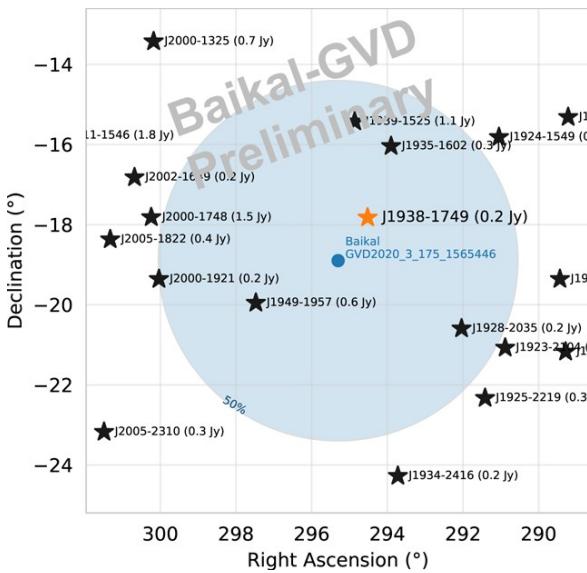
Light curves of J0301-1812 measured by RATAN-600



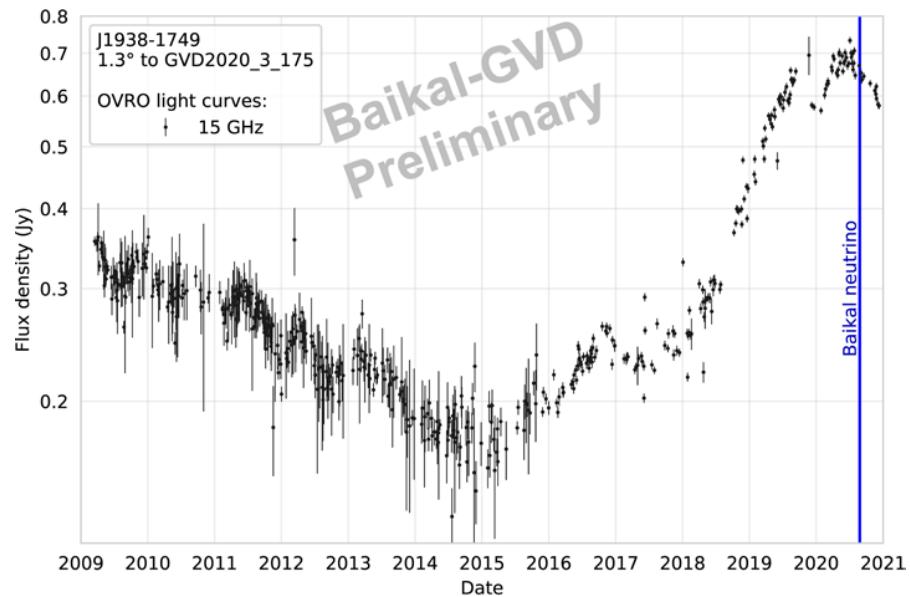
Radio-loud blazars – promising neutrino sources (2)

GVD2020_3_175_N

radio-bright blazars nearby

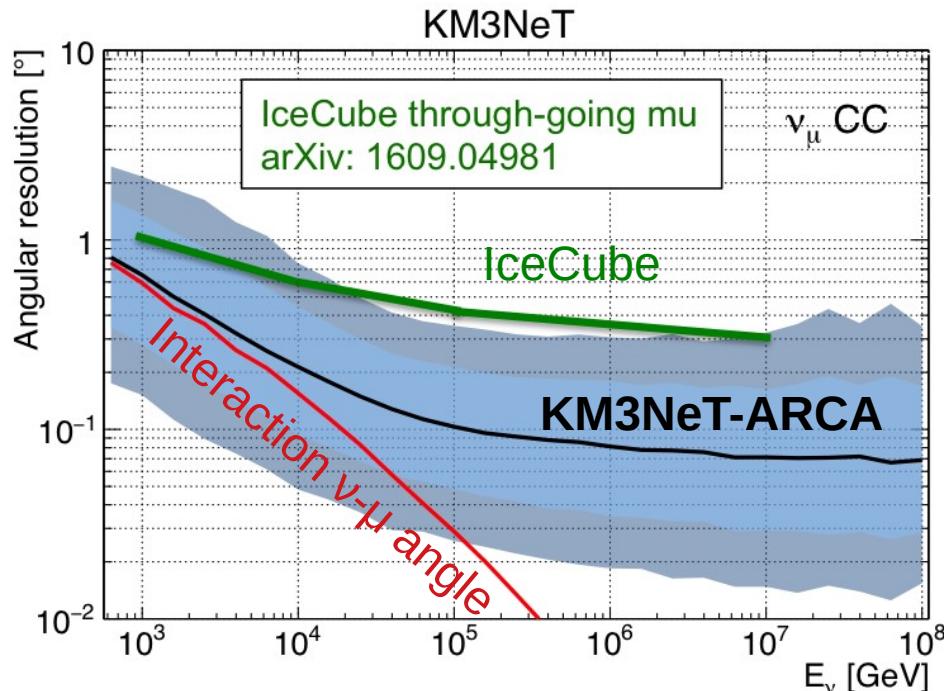


Light curves of J1938-1749 measured by OVRO

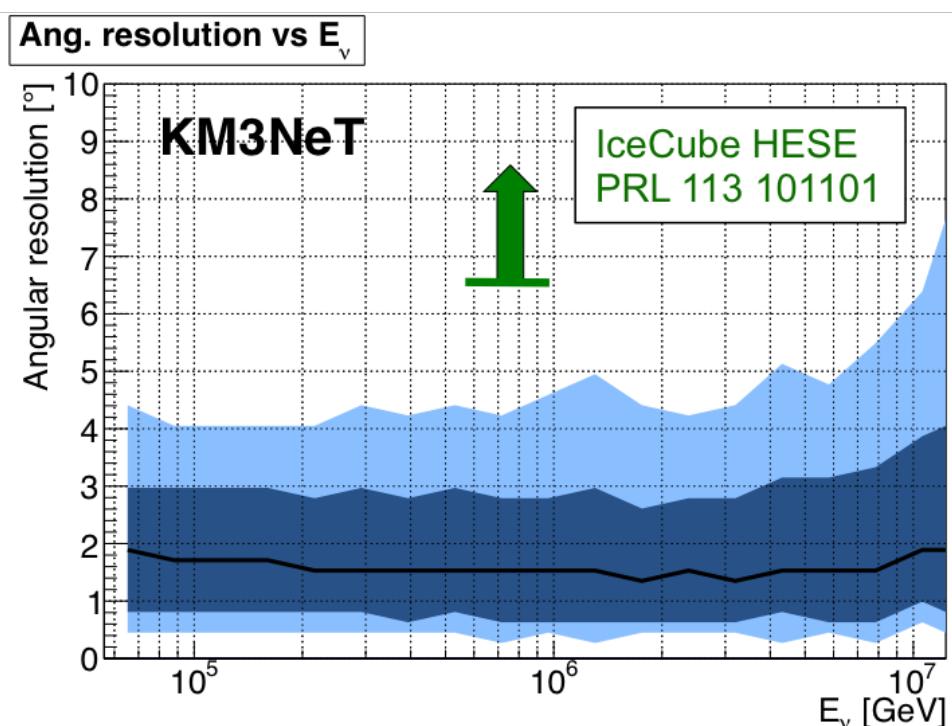


ARCA - angular resolution

Tracks



Showers



$\sim 0.1^{\circ}$ angular resolution for tracks ($E > 100$ TeV); $\sim 2^{\circ}$ for showers